

# Event structure and small- $x$ issues at 100 TeV

Peter Skands (CERN TH)

What does the average collision look like?

How many of them are there? ( $\sigma_{\text{pileup}}$ )

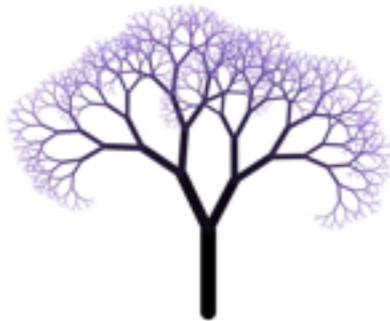
How much energy in the Underlying Event? (UE)

# Event Structure at PP Colliders

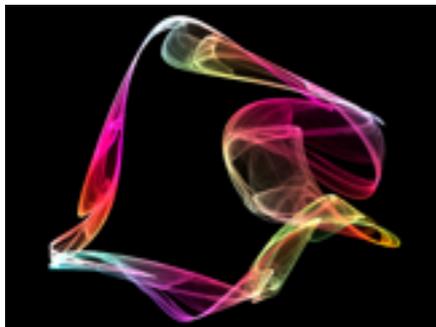
## Dominated by QCD

More than just a perturbative expansion in  $\alpha_s$

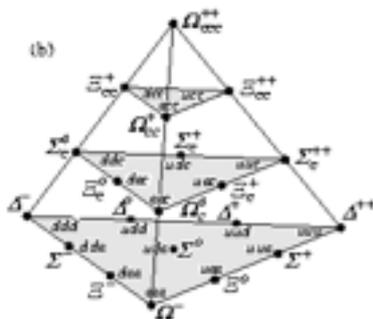
Emergent phenomena:



**Jets** (the QCD fractal)  $\longleftrightarrow$  amplitude structures  
 $\longleftrightarrow$  fundamental quantum field theory.  
Precision jet (structure) studies.



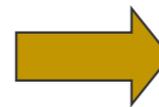
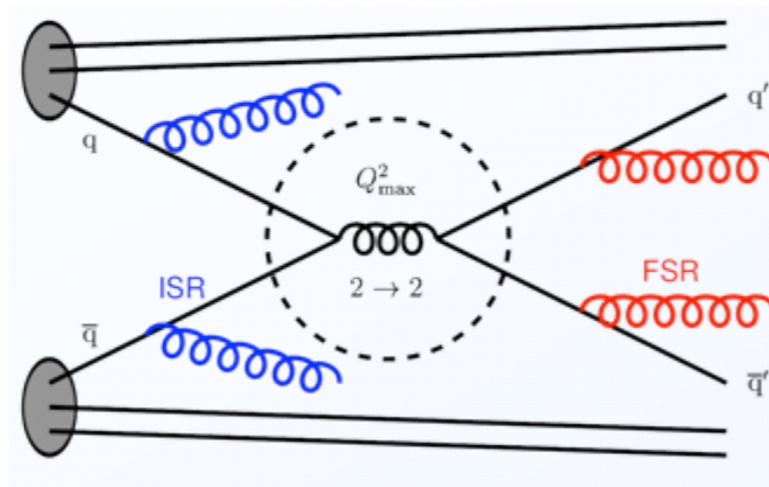
**Strings** (strong gluon fields)  $\longleftrightarrow$  quantum-classical  
correspondence. String physics. Dynamics of  
hadronization phase transition.



**Hadrons**  $\longleftrightarrow$  Spectroscopy (incl excited and exotic  
states), lattice QCD, (rare) decays, mixing, light  
nuclei. Hadron beams  $\rightarrow$  MPI, diffraction, ...

See eg TASI lectures, e-Print: [arXiv:1207.2389](https://arxiv.org/abs/1207.2389)

# Modeling Hadronic Final States



Calculate Everything  $\approx$  solve QCD  $\rightarrow$  requires compromise!

## Monte Carlo Event Generators:

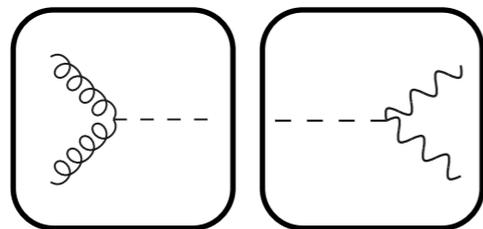
Explicit Dynamical Modeling  $\rightarrow$  **complete events** (can evaluate any observable you want)

Factorization  $\rightarrow$  Split the problem into many (nested) pieces

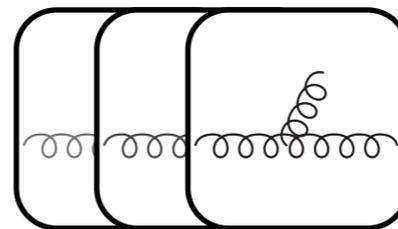
+ Quantum mechanics  $\rightarrow$  Probabilities  $\rightarrow$  Random Numbers (MC)

Soft Physics

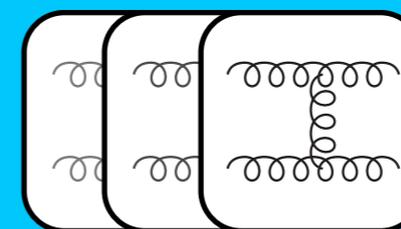
$$\mathcal{P}_{\text{event}} = \mathcal{P}_{\text{hard}} \otimes \mathcal{P}_{\text{dec}} \otimes \mathcal{P}_{\text{ISR}} \otimes \mathcal{P}_{\text{FSR}} \otimes \mathcal{P}_{\text{MPI}} \otimes \mathcal{P}_{\text{Had}} \otimes \dots$$



Matrix Elements  
(+ Sudakov Corrections)



Shower Kernels  
(+ ME corrections)



Multiple Parton Interactions  
Hard + Soft  $\rightarrow$  INEL & UE



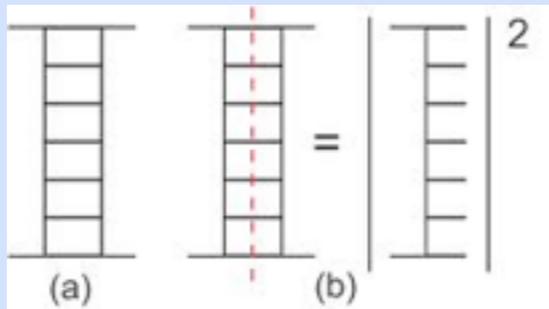
Hadronization, Decays, Soft  
Diffraction, Beam Remnants

# Soft Physics : Theory Models

See e.g. Reviews by MCnet [arXiv:1101.2599] and KMR [arXiv:1102.2844]

**A**

## Regge Theory



Optical Theorem

+ Eikonal multi-Pomeron exchanges

$$\sigma_{\text{tot,inel}} \propto \log^2(s)$$

Cut Pomerons  $\rightarrow$  Flux Tubes (strings)

Uncut Pomerons  $\rightarrow$  Elastic (& eikonalization)

Cuts unify treatment of all soft processes

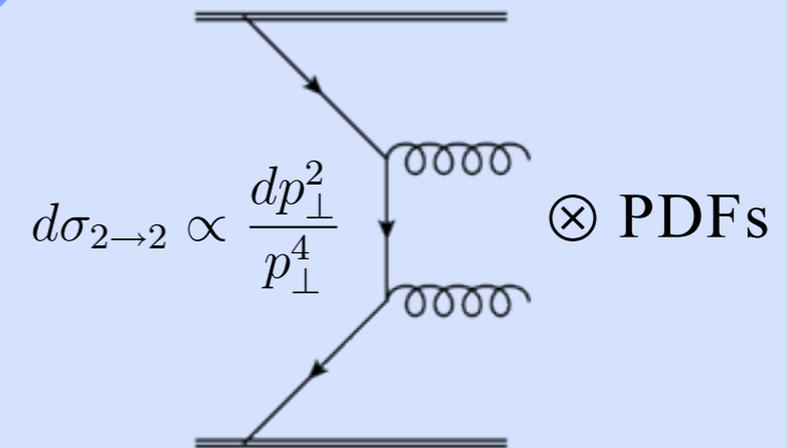
EL, SD, DD, ... , ND

Perturbative contributions added above  $Q_0$

E.g., QGSJET, SIBYLL

**B**

## Parton Based



+ Unitarity & Saturation

$\rightarrow$  Multi-parton interactions (MPI)

+ Parton Showers & Hadronization

Regulate  $d\sigma$  at low  $p_{T0} \sim$  few GeV

Screening/Saturation  $\rightarrow$  energy-dependent  $p_{T0}$

Total cross sections from Regge Theory  
(Donnachie-Landshoff + Parametrizations)

E.g., PYTHIA,  
HERWIG, SHERPA

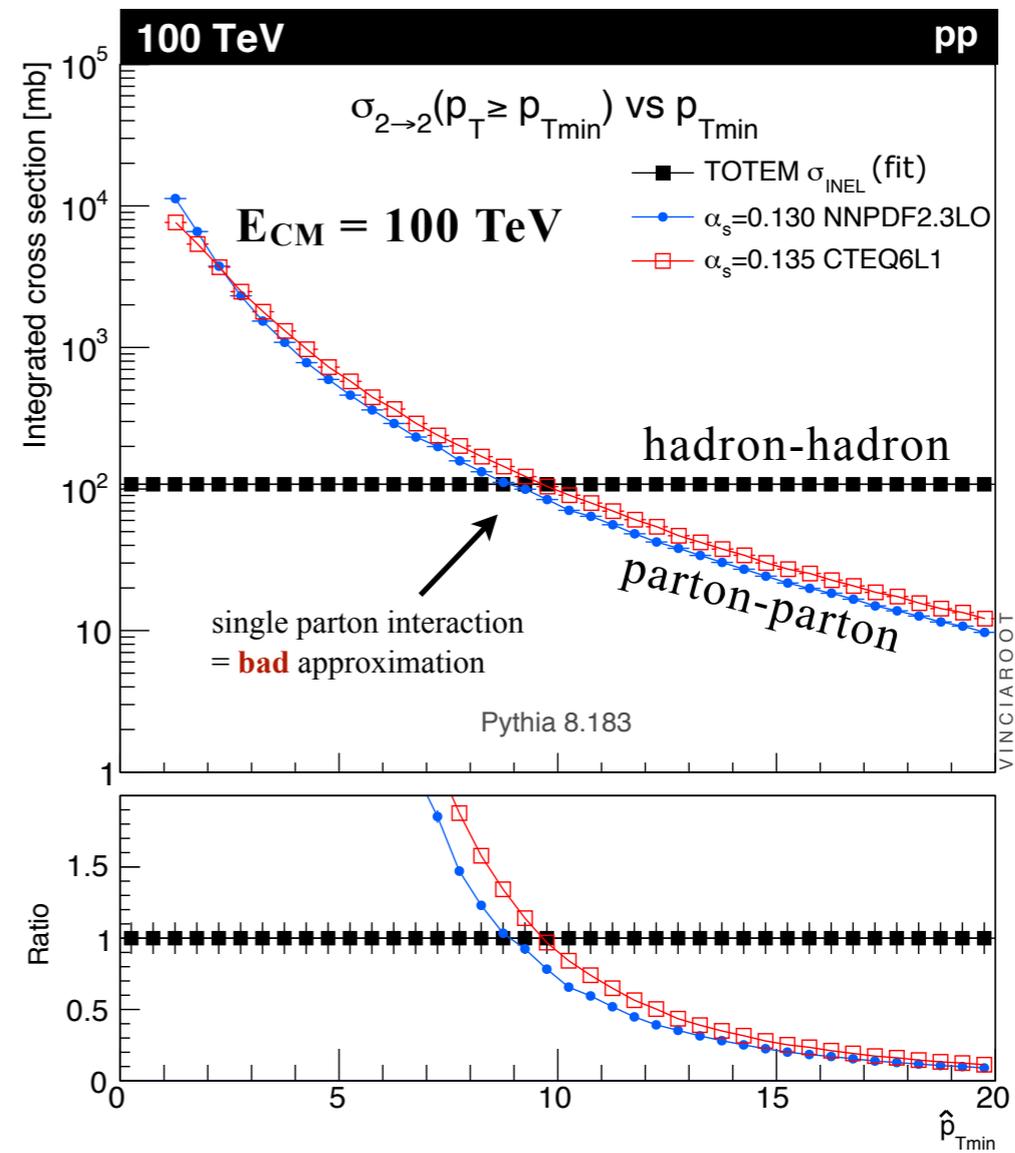
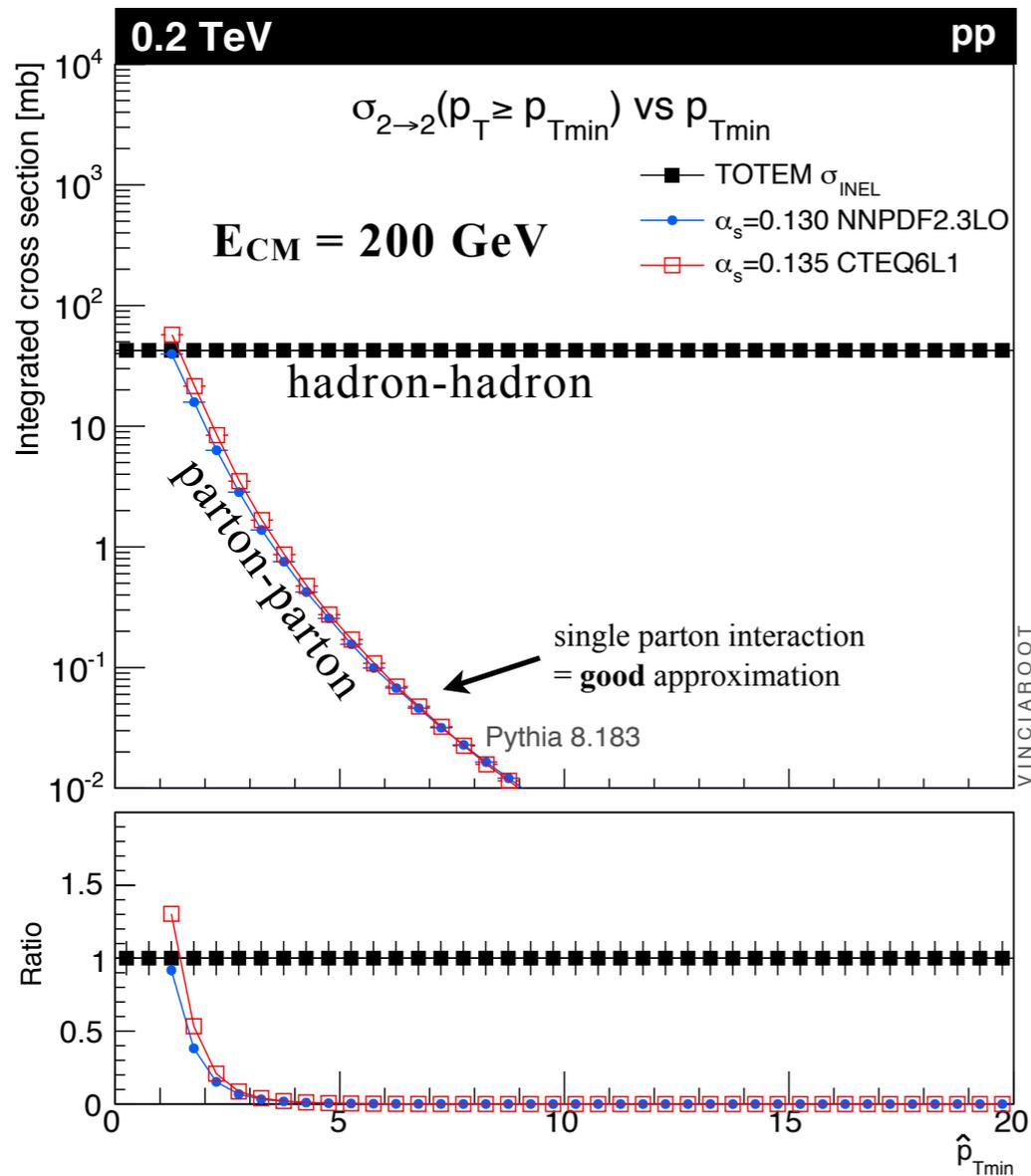
+ "Mixed"

E.g., PHOJET, EPOS,  
SHERPA-KMR

# B

# Parton-Based Models : MPI

Consider the inclusive di-jet cross section in QCD

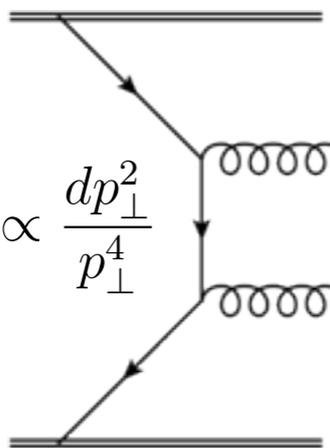


$\sigma_{2 \rightarrow 2} > \sigma_{pp}$  interpreted as consequence of each pp containing several  $2 \rightarrow 2$  interactions: MPI

# Soft MPI

## Main applications:

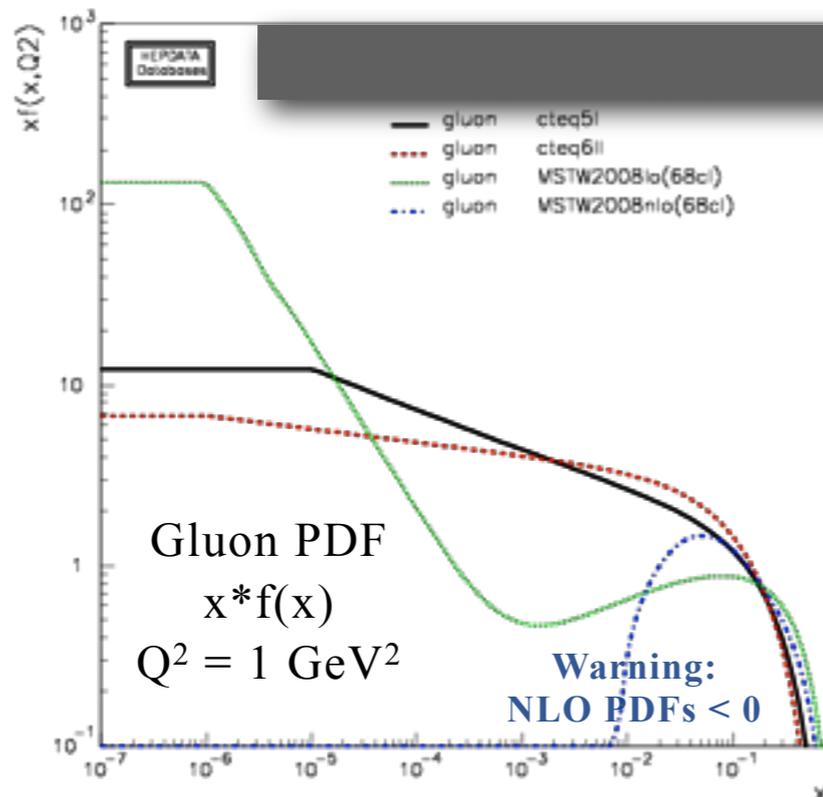
Central Jets/EWK/top/  
Higgs/New Physics

$$d\sigma_{2\rightarrow 2} \propto \frac{dp_{\perp}^2}{p_{\perp}^4} \otimes \text{PDFs}$$


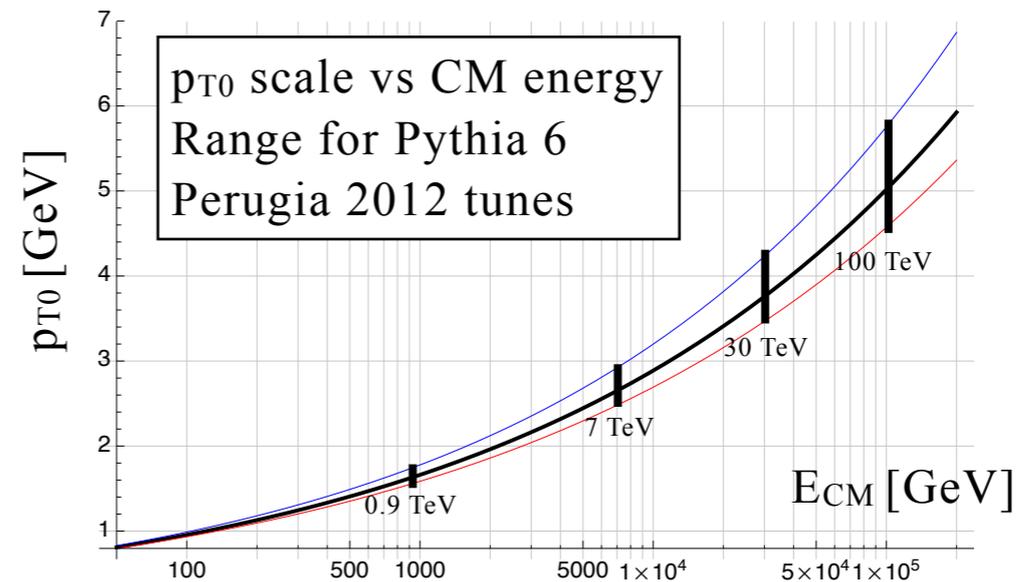
High  $Q^2$   
and  
finite  $x$

**Extrapolation to soft scales delicate.**  
Impressive successes with MPI-based models but still far from a solved problem

- Form of PDFs at small  $x$  and  $Q^2$  Saturation
- Form and  $E_{\text{cm}}$  (and/or  $x$ ) dependence of  $p_{T0}$  regulator
- Modeling of the diffractive component
- Proton transverse mass distribution
- Colour Reconnections, Collective Effects



## Poor Man's Saturation



See also Connecting hard to soft: KMR, EPJ C71 (2011) 1617 + PYTHIA "Perugia Tunes": PS, PRD82 (2010) 074018

# Low- $x$ Issues (in MC/PDF context)

**Low  $x$  :** parton carries tiny fraction of beam energy.

E.g.: 
$$x_{\Lambda} = \frac{2\Lambda_{\text{QCD}}}{E_{\text{CM}}} \quad x_{\perp 0} = \frac{2p_{\perp 0}}{E_{\text{CM}}}$$

7 TeV:  $x \sim 10^{-5} - 10^{-4}$

100 TeV:  $x \sim 10^{-6} - 10^{-4}$

**Higher  $x$  :** momenta  $> \Lambda_{\text{QCD}}$

→ pQCD ~ OK

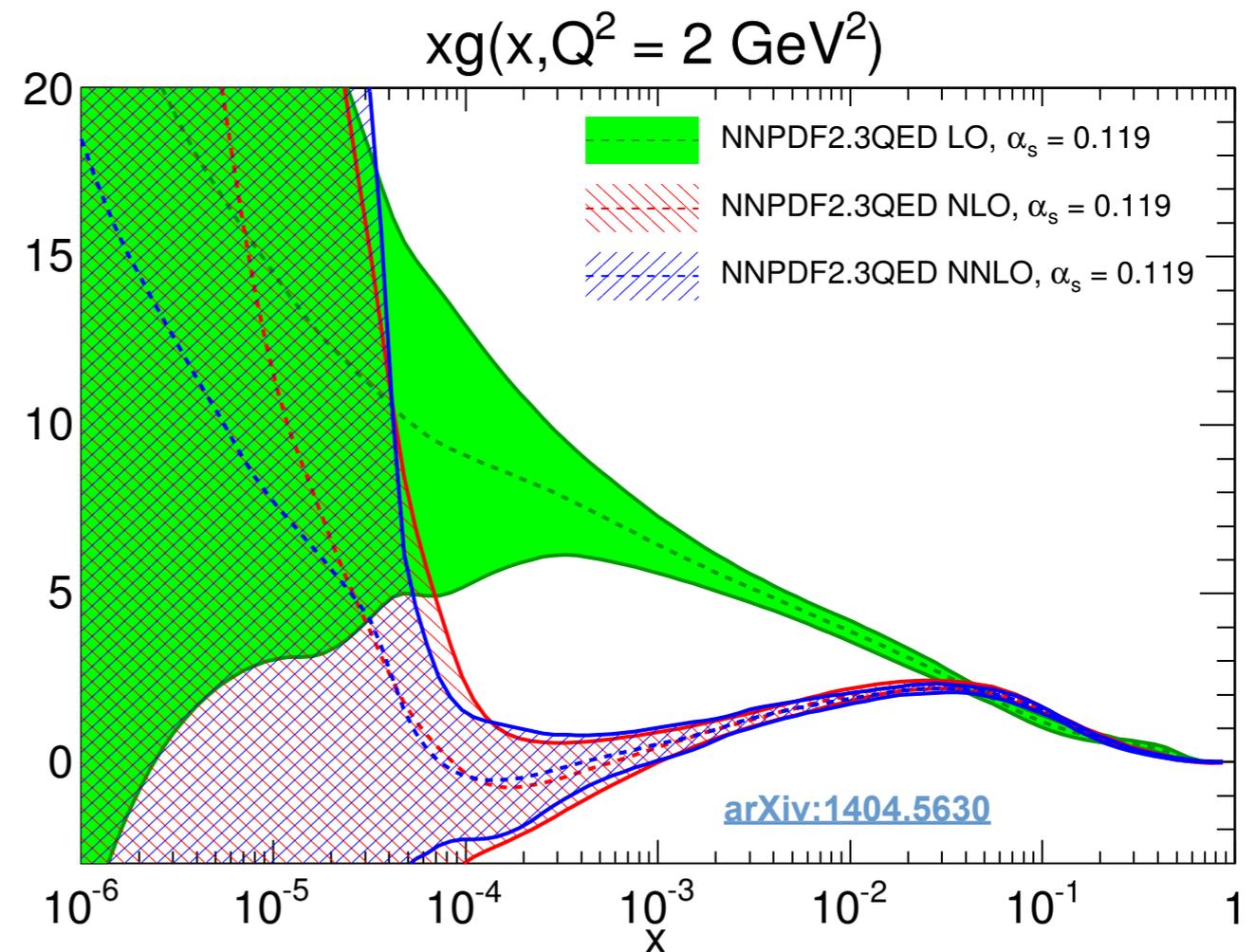
**Smaller  $x$  :** strong non-perturbative / colour-screening / saturation effects expected

What does a PDF even mean?

Highly relevant for MPI (& ISR)

PDF *must* be a probability density → can *only* use LO PDFs

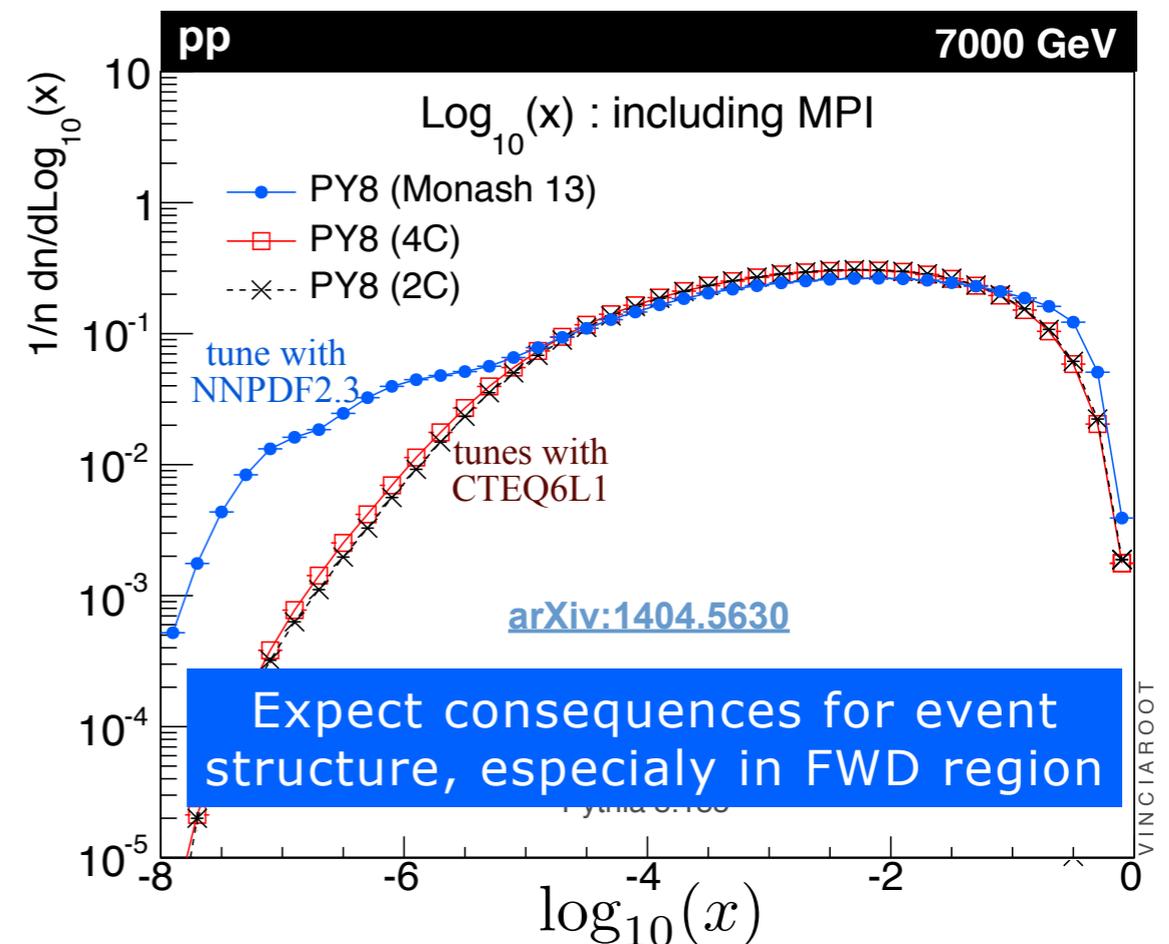
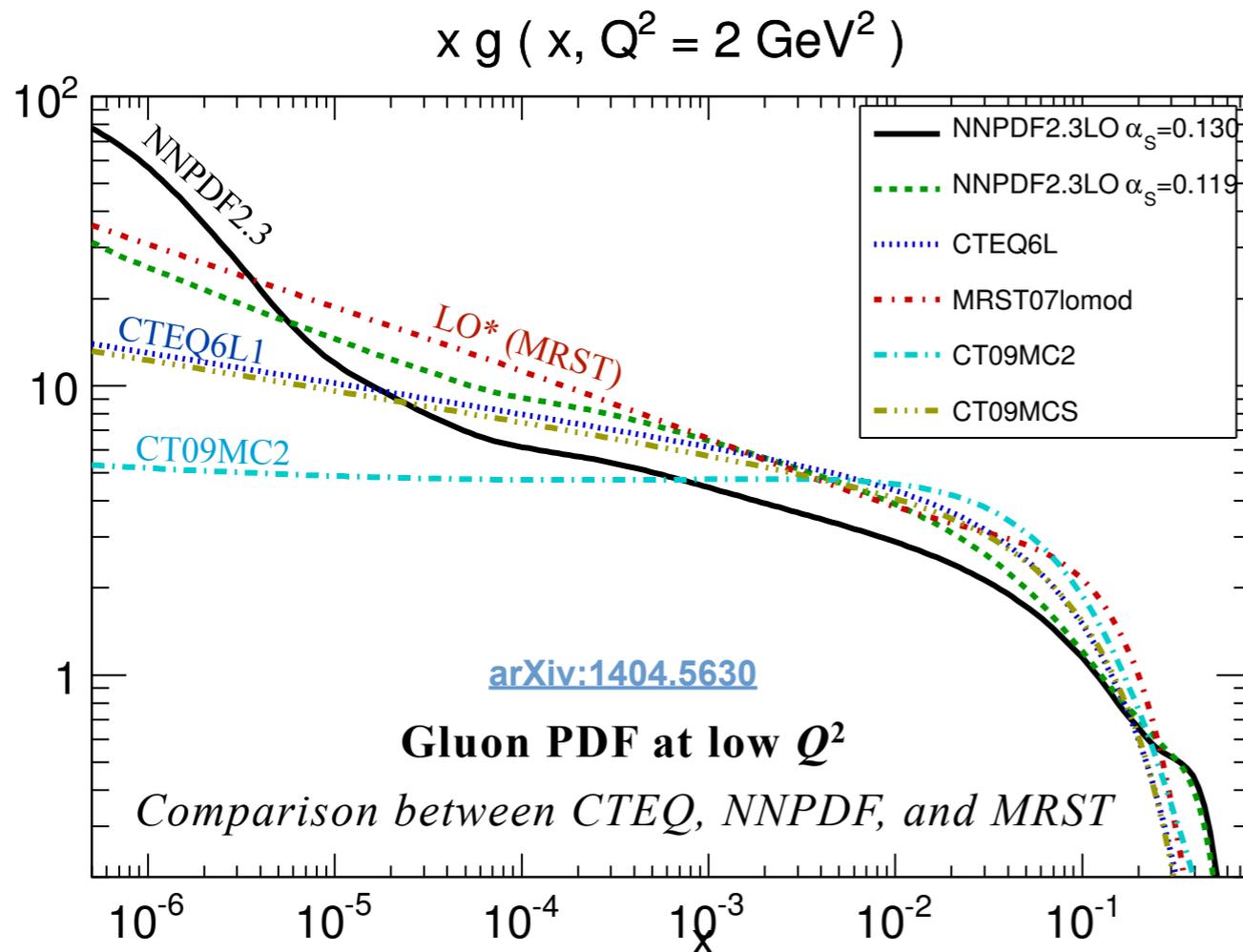
(+ Constraints below  $x \sim 10^{-4}$  essentially just momentum conservation + flavour sum rules)



# MPI models and Low $x$

## Gluon PDF at low $Q^2$ drives MPI

**EXAMPLE: PYTHIA 8**  
Range of  $x$  values probed by  
different MPI tunes



Controlling these issues will require an improved understanding of the interplay between low- $x$  PDFs, saturation / screening, and MPI in MC context. (+ Clean model-independent experimental constraints!)

**Not automatic: Communities don't speak same language (+ low visibility)**



# Recent PYTHIA Models/Tunes

## & Extrapolations to Event Structure at 100 TeV

### PYTHIA 8.1

Current Default = **4C** (from 2010)

Tunes 2C & 4C: e-Print: [arXiv:1011.1759](https://arxiv.org/abs/1011.1759)

LEP tuning undocumented (from 2009)  
LHC tuning only used very early data  
based on CTEQ6L1

### Aims for the Monash 2013 Tune

Monash 2013 Tune: e-Print: [arXiv:1404.5630](https://arxiv.org/abs/1404.5630)

Set M13 Tune:  
→  
in PYTHIA 8

Tune:ee = 7  
Tune:pp = 14

- Revise (and document) constraints from  $e^+e^-$  measurements
  - In particular in light of possible interplays with LHC measurements
- Test drive the new NNPDF 2.3 LO PDF set (with  $\alpha_s(m_Z) = 0.13$ ) for pp & ppbar
  - Update min-bias and UE tuning + energy scaling → 2013
  - Follow "Perugia" tunes for PYTHIA 6: use same  $\alpha_s$  for ISR and FSR
  - Use the PDF value of  $\alpha_s$  for both hard processes and MPI

### PYTHIA 6.4 (*warning: no longer actively developed*)

Default: still rather old  $Q^2$ -ordered tune  $\sim$  Tevatron Tune A

Most recent: Perugia 2012 set of  $p_T$ -ordered tunes (370 - 382) + Innsbruck (IBK) Tunes (G. Rudolph)

Perugia Tunes: e-Print: [arXiv:1005.3457](https://arxiv.org/abs/1005.3457)  
(+ 2011 & 2012 updates added as appendices)

Note: I will focus on default / author tunes here  
(Important complementary efforts undertaken by LHC experiments)



# Tuning

means different things to different people

10% agreement is great  
for (N)LO + LL

MB/UE/Soft: larger  
uncertainties since driven  
by non-factorizable and  
non-perturbative physics

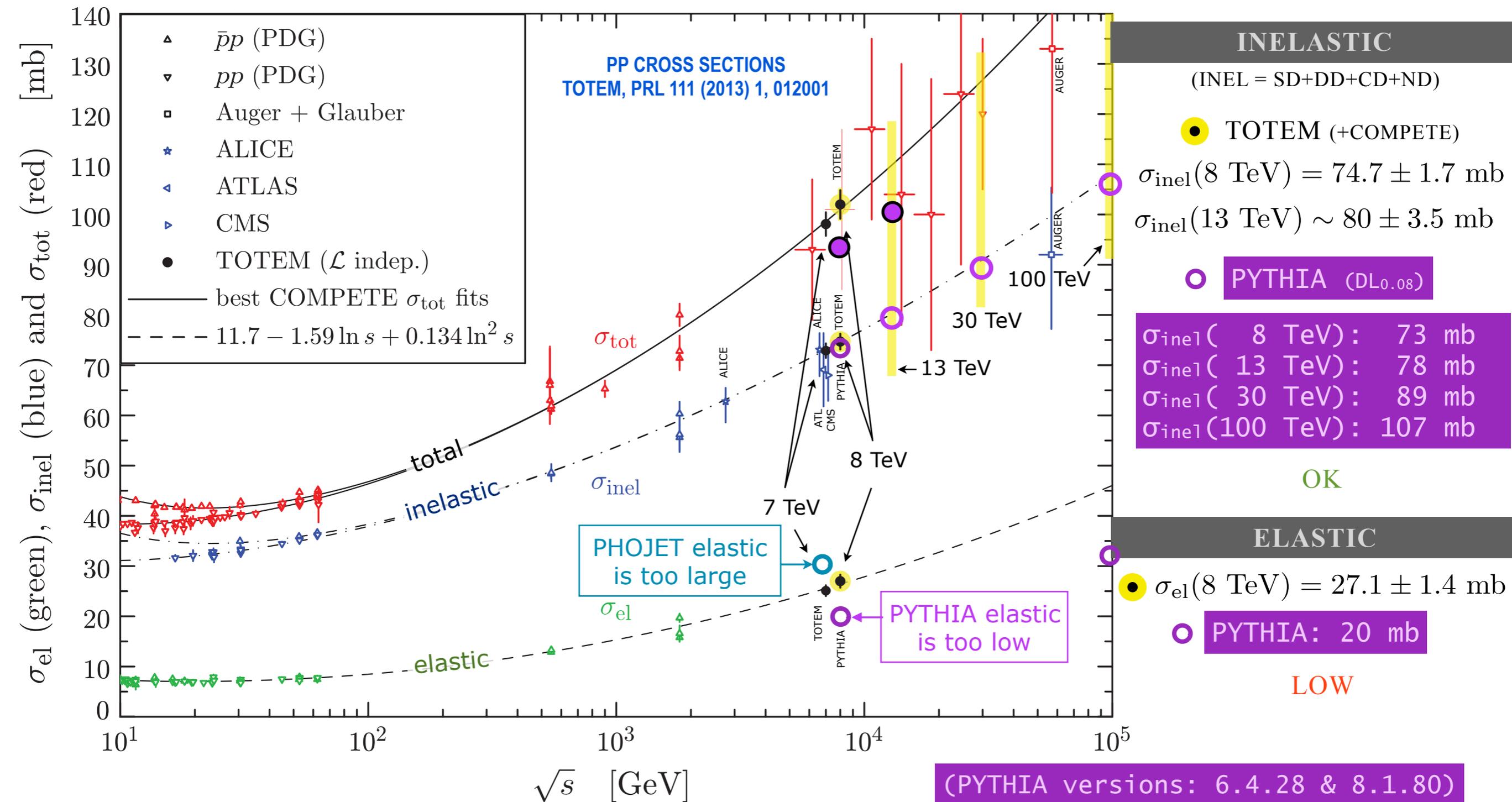
Complicated dynamics:  
If a model is simple, it is  
wrong (*T. Sjöstrand*)



# Cross Sections & Energy Scaling

Pileup rate  $\propto \sigma_{\text{tot}}(s) = \sigma_{\text{el}}(s) + \sigma_{\text{inel}}(s) \propto s^{0.08}$  or  $\ln^2(s)$  ?

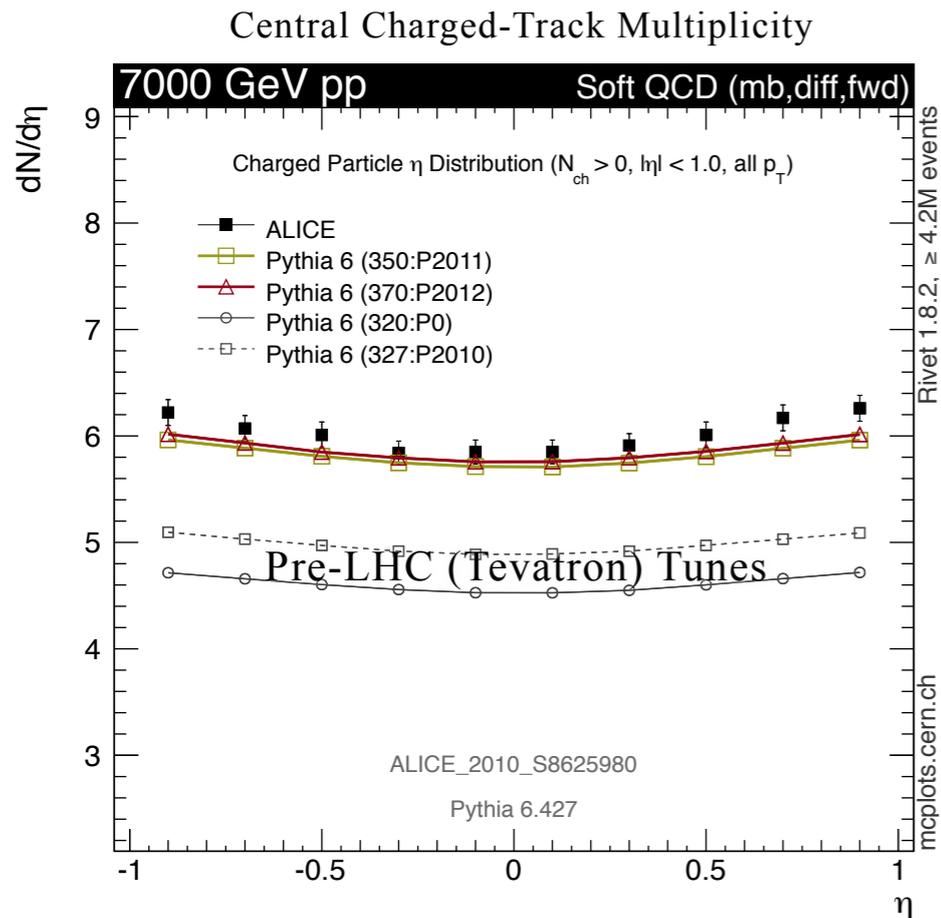
Donnachie-Landshoff (or 0.096?)      Froissart-Martin Bound



# Event Properties: Minimum-Bias

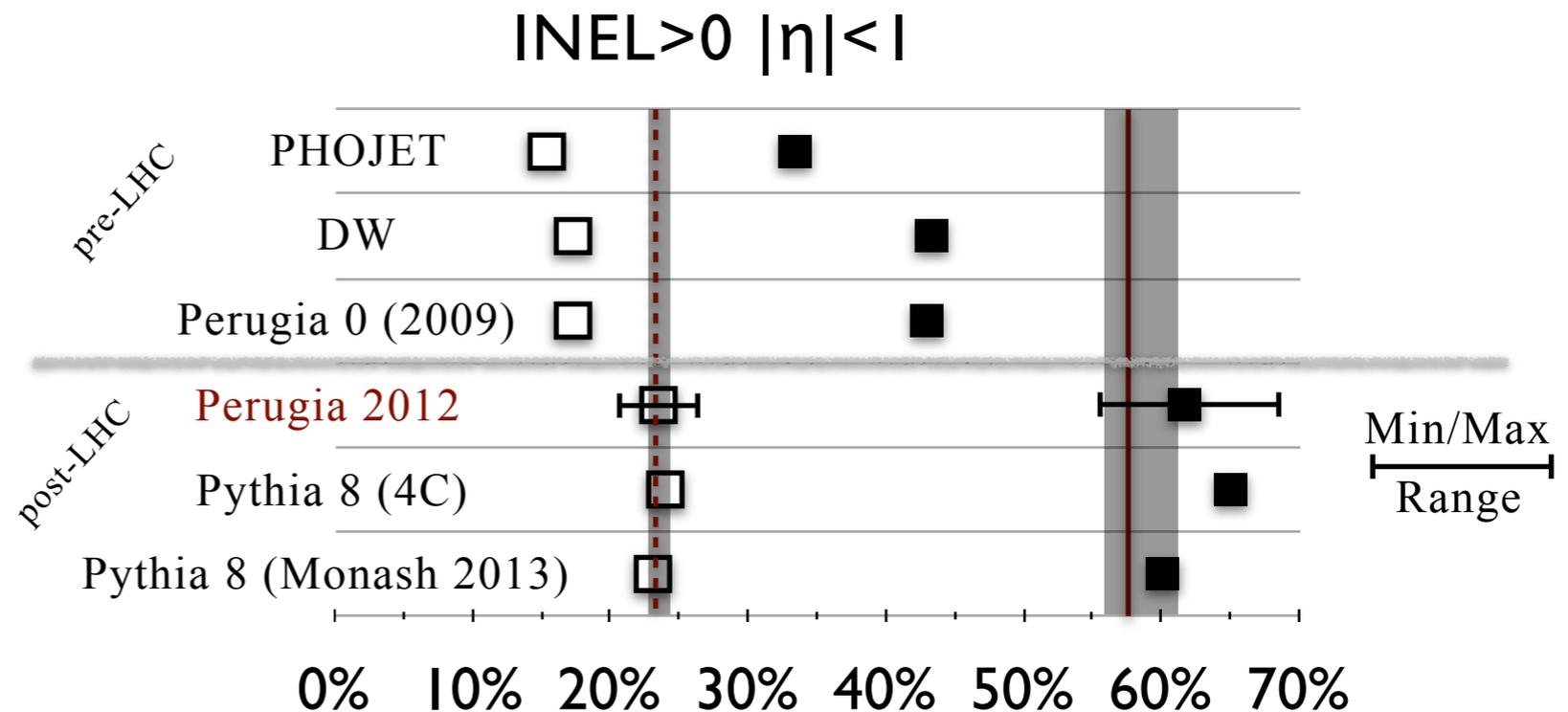
## How many charged tracks? (in central region)

**The updated models** (as represented here by the Perugia 2012 and Monash 2013 tunes):  
 Agree with the LHC min-bias and UE data at each energy  
 And, non-trivially, they exhibit a more consistent energy scaling between energies  
 So we may have some hope that we can use these models to do extrapolations



Tevatron tunes were ~ 10-20% low on MB and UE

A VERY SENSITIVE E-SCALING PROBE: relative increase in the central charged-track multiplicity from 0.9 to 2.36 and 7 TeV



Data from ALICE EPJ C68 (2010) 345

Discovery at LHC: things are larger and scale faster than we thought they did

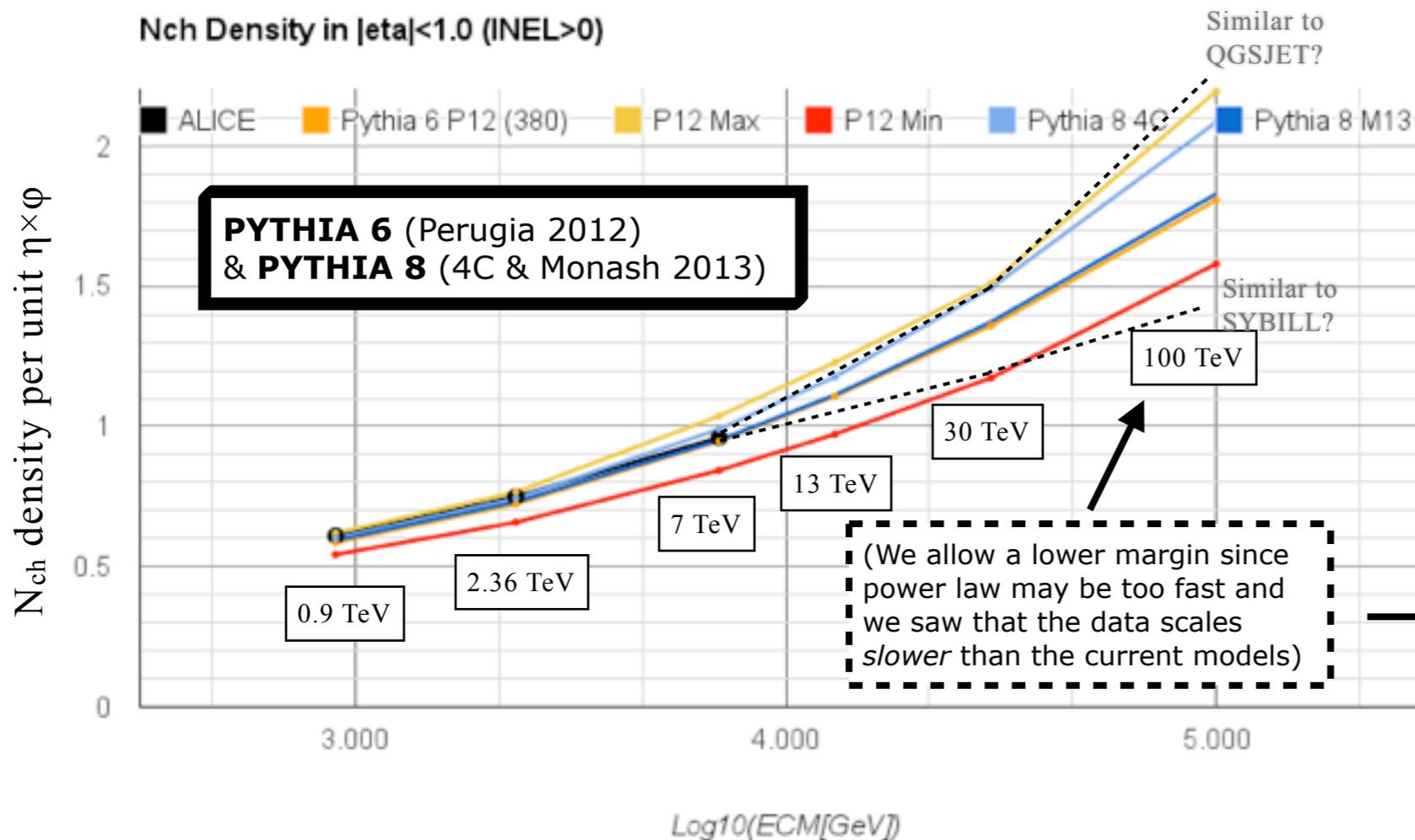
Caveat: still not fully understood why Tevatron tunes were low.

See also: Schulz & Skands,  
[arXiv:1103.3649](https://arxiv.org/abs/1103.3649)

# Central $\langle N_{ch} \rangle \rightarrow 100$ TeV

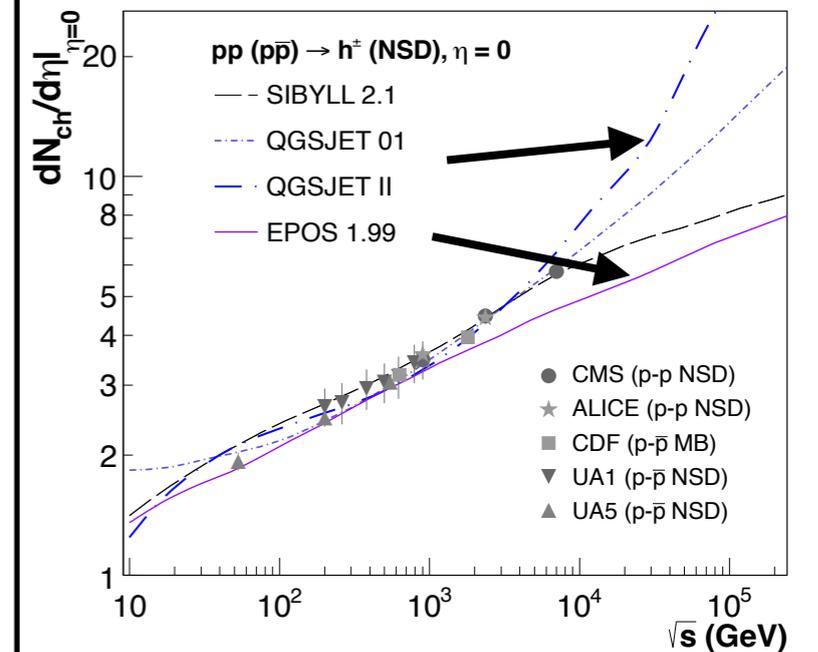
**B** From parton-based models, expect  $\sim$  power law

Note: I use INEL>0 (rather than NSD, INEL, ...)  
Recap: this means events with at least one charged particle in  $|\eta| < 1$   
charged particle defined with  $c \times \tau > 10$  mm



**A**

Comparison with Pomeron-based models. From D. d'Enterria et al, [arXiv:1101.5596](https://arxiv.org/abs/1101.5596)



QGSJET too aggressive? Would predict very high densities at 100 TeV  
EPOS too low (new version fits LHC better, worth trying out)

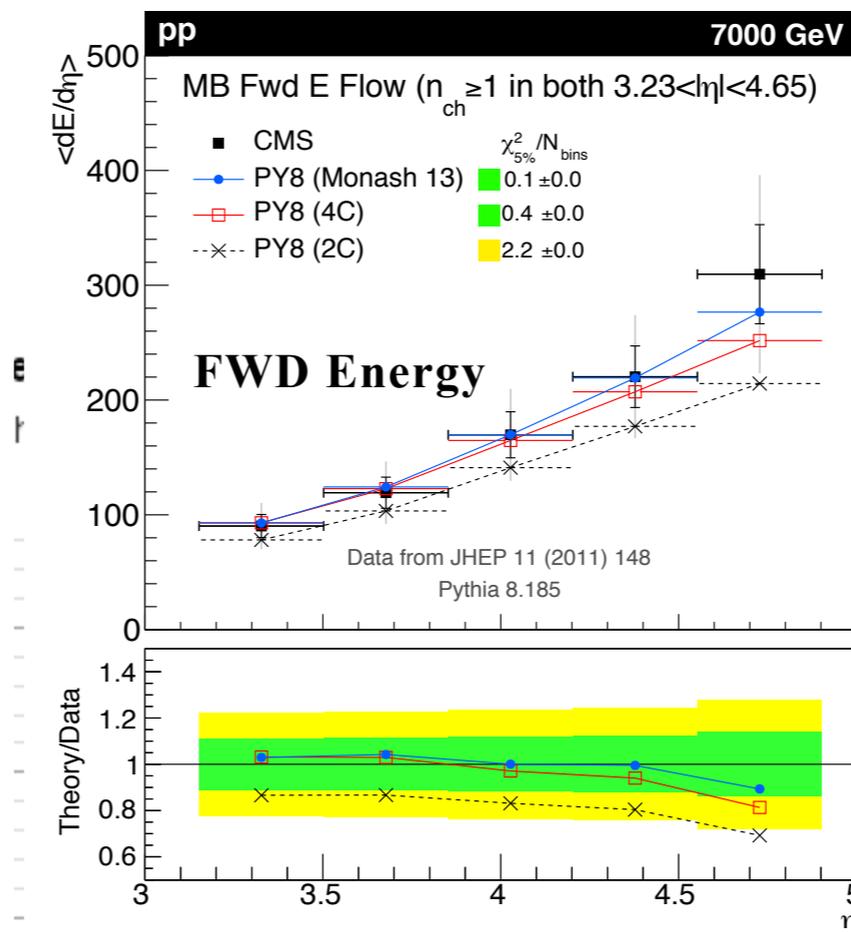
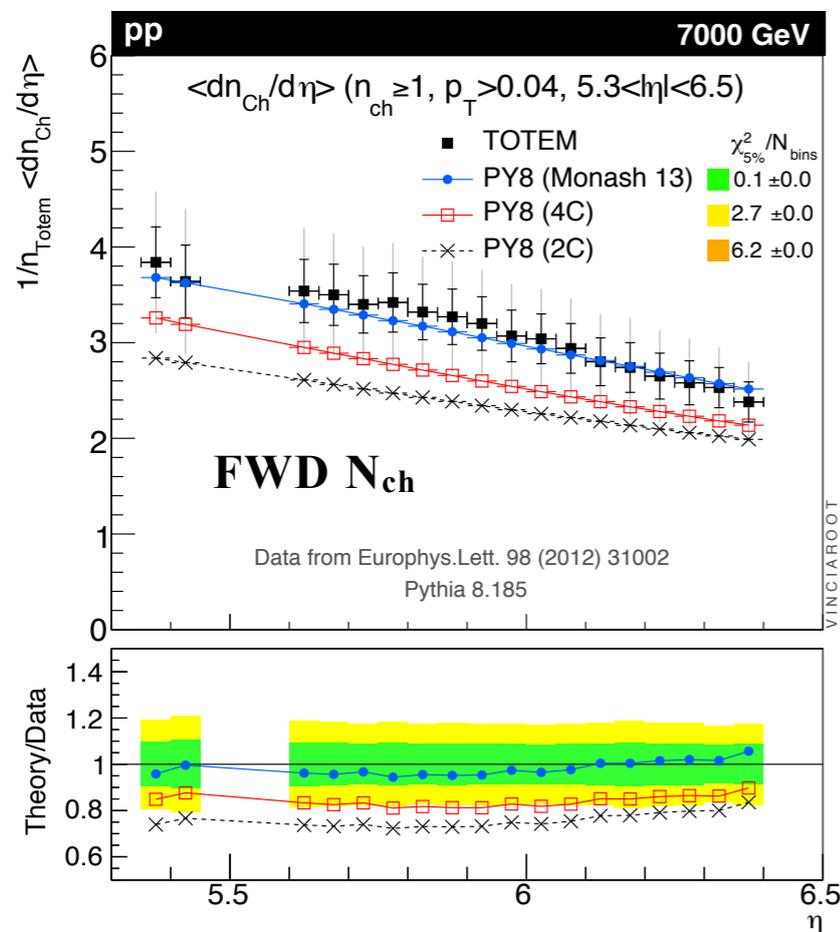
**Extrapolations for INEL > 0**  
**Central  $\langle N_{ch} \rangle$  density**  
(per unit  $\Delta\eta\Delta\phi$  in  $|\eta| < 1$ ;  $c\tau > 10$ mm)

- @13 TeV :  $1.1 \pm 0.1$
- @30 TeV :  $1.33 \pm 0.14$
- @100 TeV :  $1.8 \pm 0.4$

# Low $x$ : Looking Forward

Higher NNPDF gluon at low  $x \rightarrow$  more forward activity

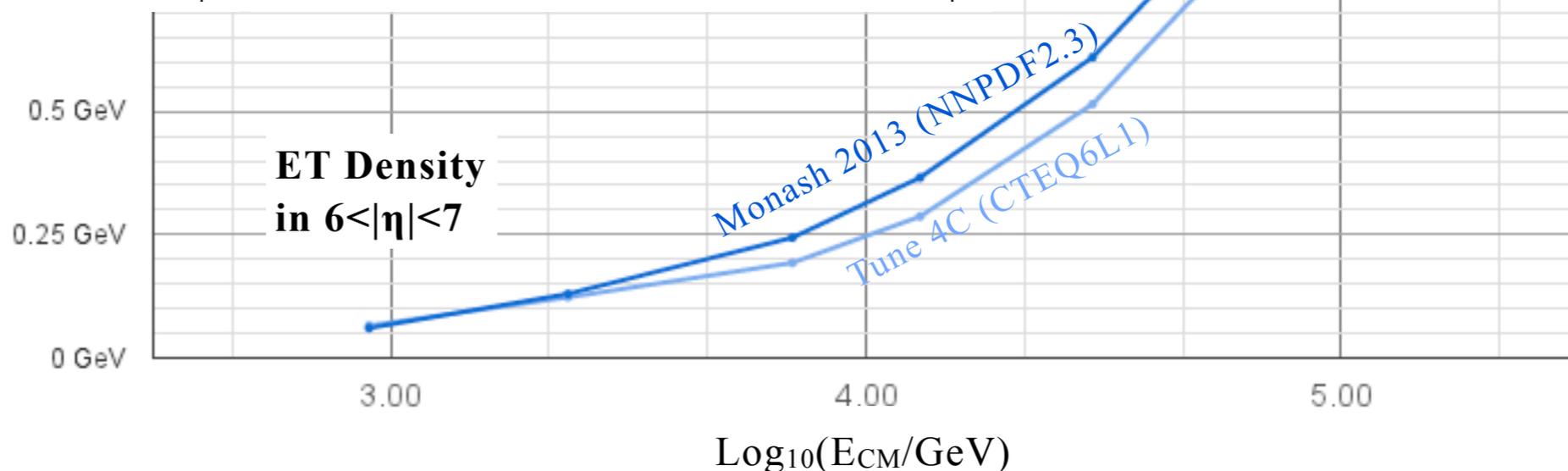
Monash 2013 Tune: e-Print: [arXiv:1404.5630](https://arxiv.org/abs/1404.5630)



E.g., 4C (CTEQ6L1) has higher *central* density than Monash 2013 (NNPDF2.3)

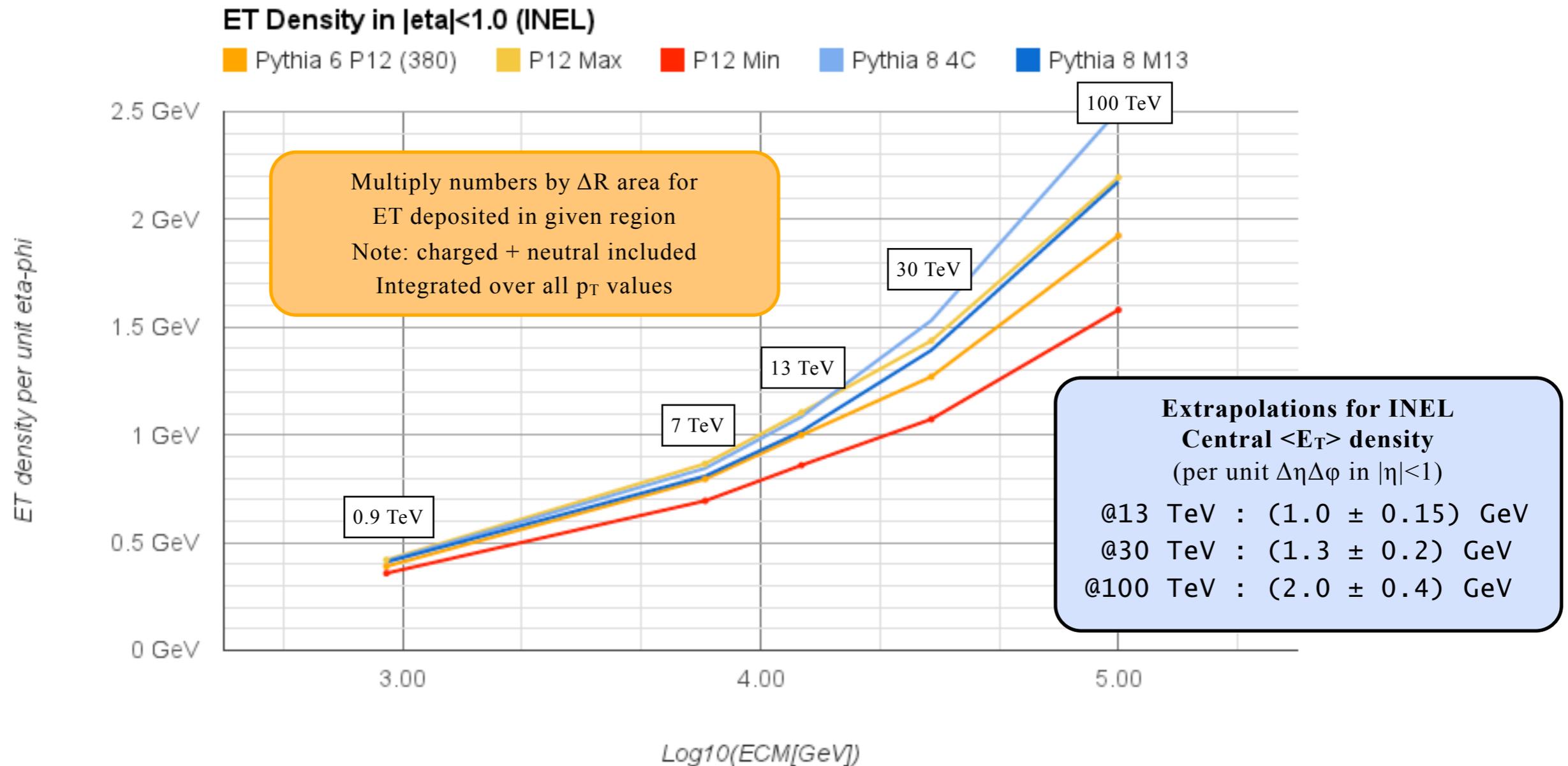
But the *opposite* is true in the forward region

ET density  $p$



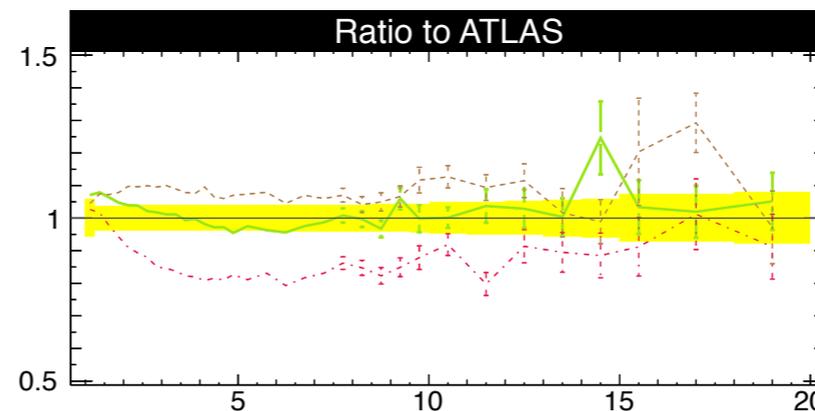
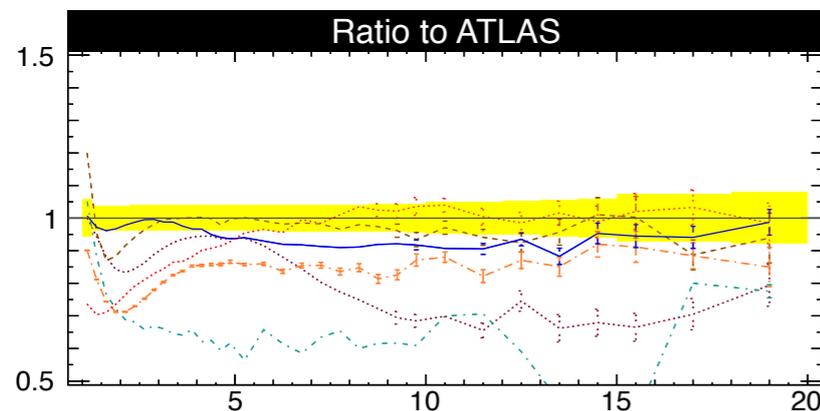
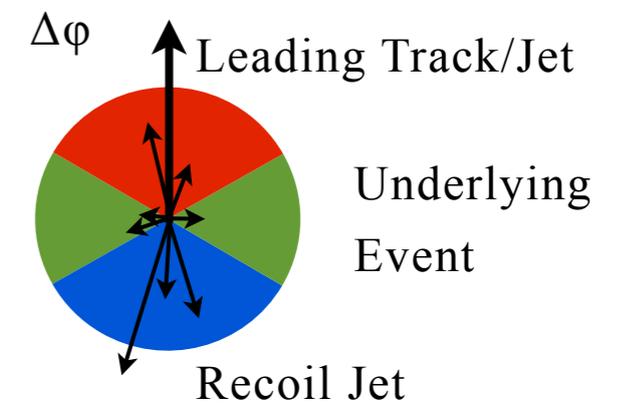
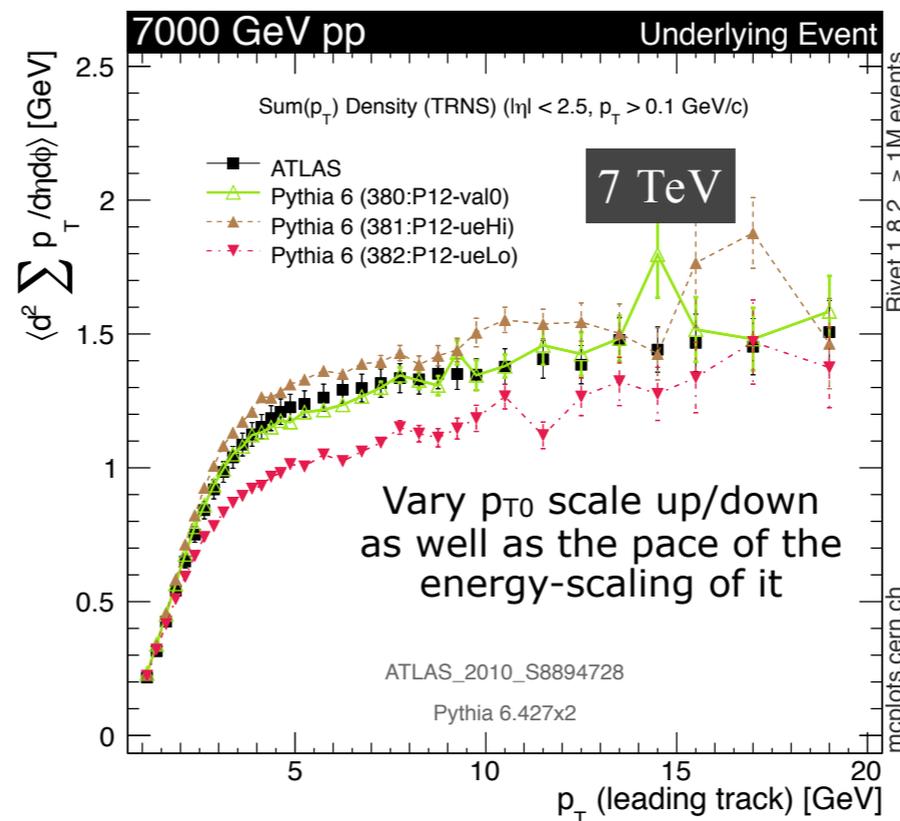
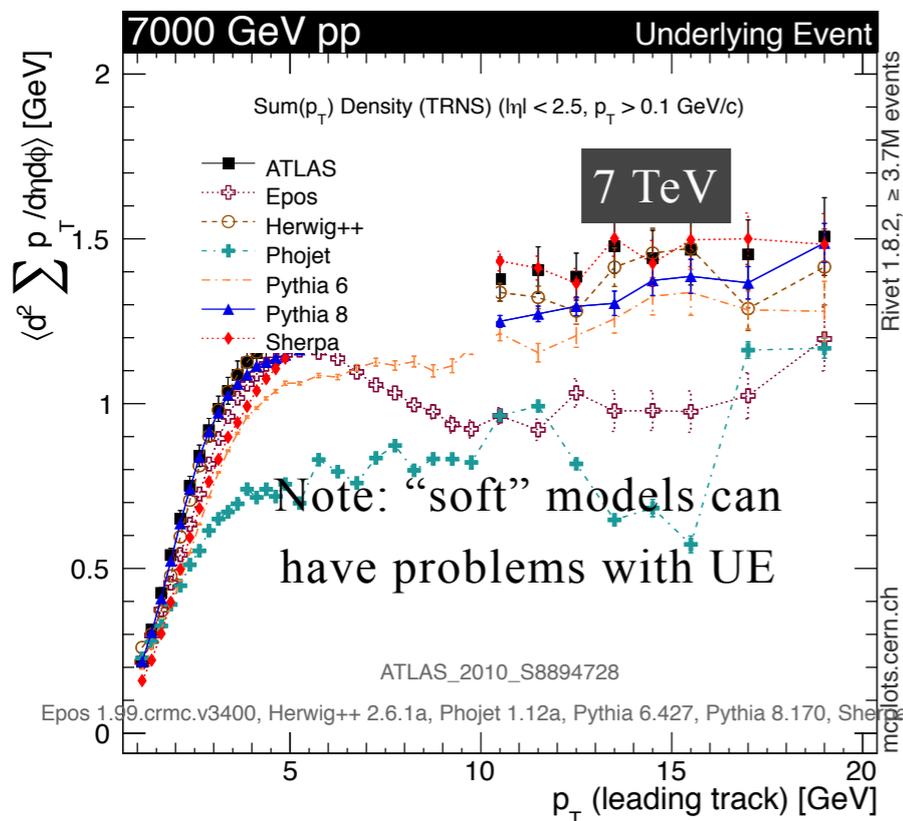
# How Much $E_T$ ? (in central detectors)

Note: I use INEL and include all charged+neutral  
 This can be combined with  $\sigma_{\text{INEL}}$  to find the central  $E_T$  deposited e.g. by pileup



# Underlying Event

There are many UE variables. The most important is  $\langle \sum p_T \rangle$  in the Transverse Region  
That tells you how much (transverse) energy the UE deposits under a jet. It is also more IR safe than  $\langle N_{ch} \rangle$ .

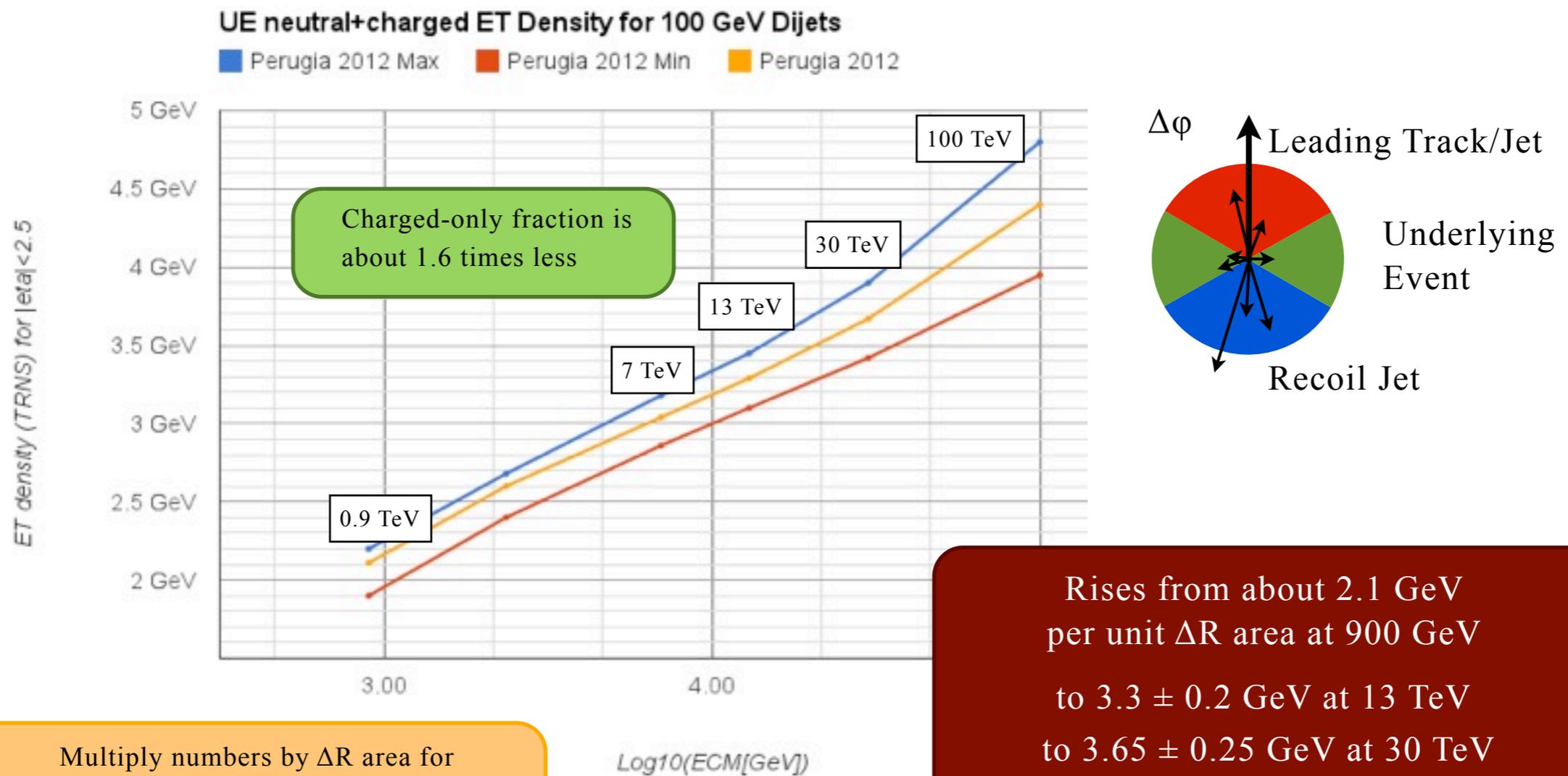


Transverse Region (TRNS)  
Sensitive to activity at right angles to the hardest jets  
Useful definition of Underlying Event

# UE $\rightarrow$ 100 TeV

## Test case: 100 GeV dijets

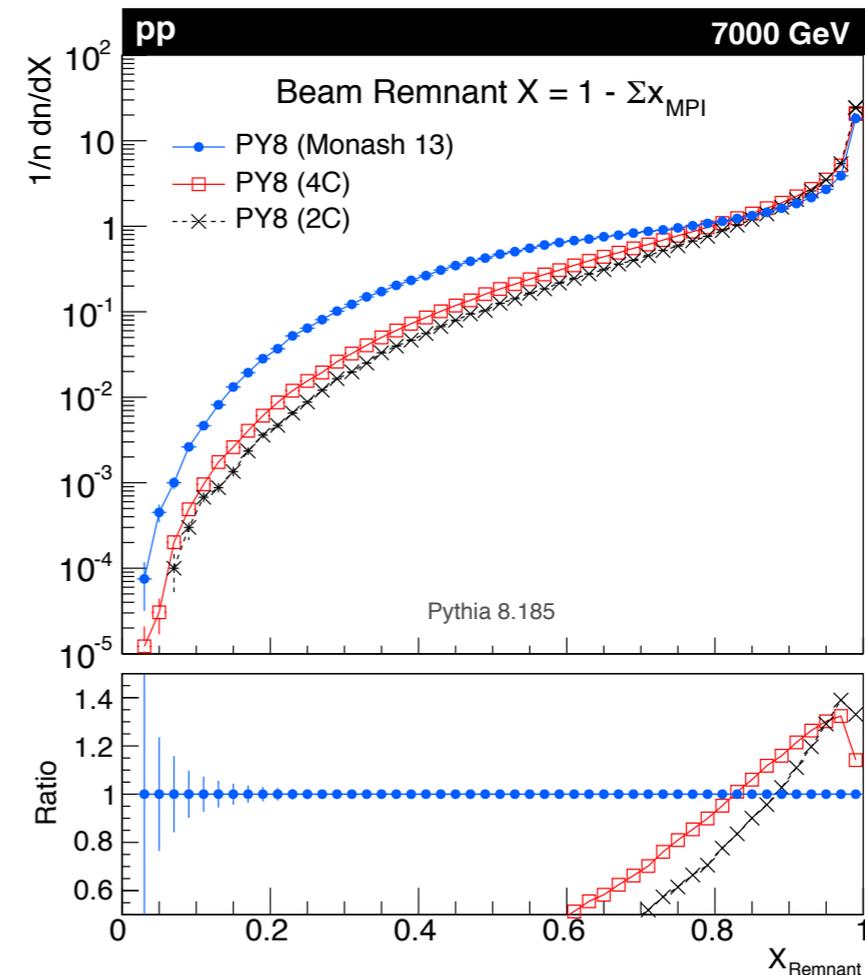
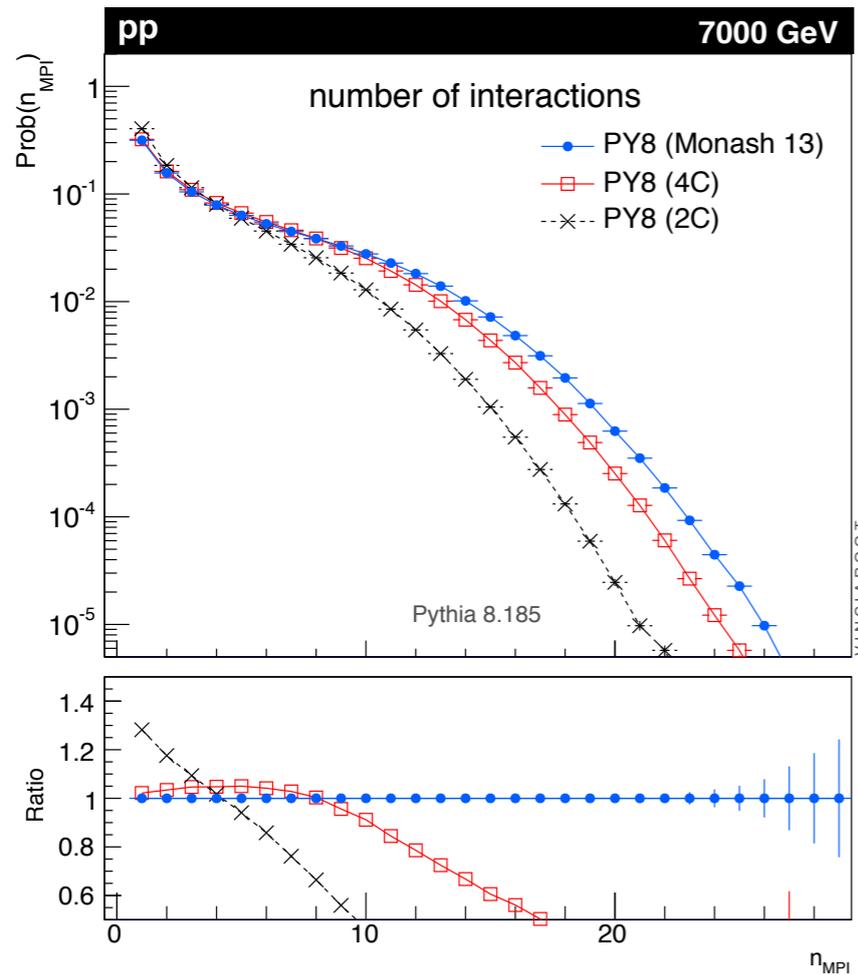
Measure ET in region transverse to the hardest track (in  $|\eta| < 2.5$ )



Multiply numbers by  $\Delta R$  area for ET deposited in given region  
Note: charged + neutral included  
Integrated over all  $p_T$  values

Rises from about 2.1 GeV per unit  $\Delta R$  area at 900 GeV to  $3.3 \pm 0.2$  GeV at 13 TeV to  $3.65 \pm 0.25$  GeV at 30 TeV and  $4.4 \pm 0.45$  GeV at 100 TeV

# 100 TeV: Total Inelastic Scattering?



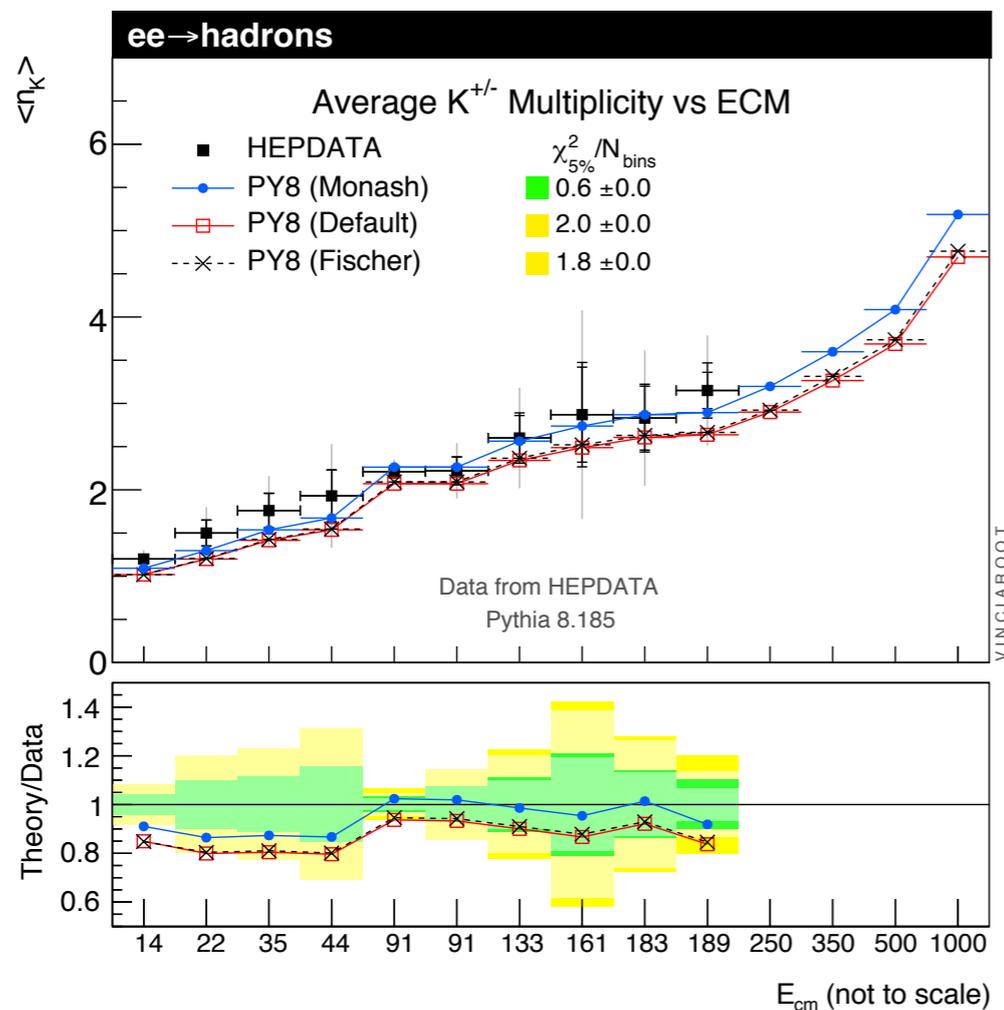
At  $O(10^{-4} - 10^{-5})$  of total cross section, the beam remnant (BR) retains  $< 10\%$  of beam energy.  
 → **“Catastrophic Energy Loss”** events. Intrinsic consequence of MPI. (Typically not caused by a single hard partonic scattering process; vanishing PDFs in the region  $x > 0.5$ ).

→ **“Total Inelastic Scattering”**?: more than 90% of the energy scattered out of both beams, may occur at a level of  $10^{-10} - 10^{-8}$  of the cross section → 10 - 1000 pb. Extremely interesting part of hadron-hadron collision physics, far from single-interaction limit. Triggers for this class of events are presumably non-trivial.

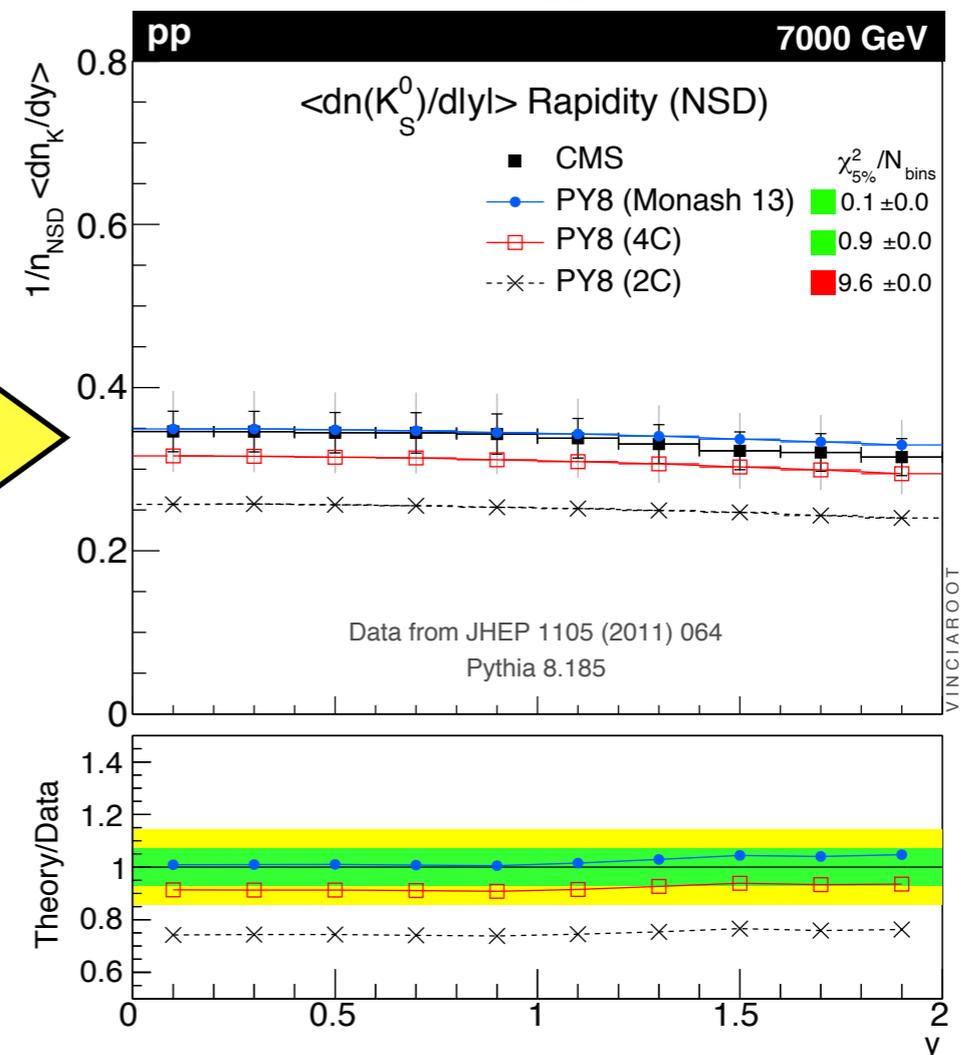
# (Event Structure: Strangeness)

**Strangeness (& baryons):** much recent debate sparked by LHC measurements. Collectivity in pp? Especially at high multiplicity?

Kaons : ee at different CM energies



Kaons:  $dn/dy$  in pp at 7000 GeV



“Trivial part”: 10% more strangeness in ee (nothing to do with collectiveness)

**Non-trivial part (still not understood!):  $p_T$  spectra & baryon sources**

# Summary

See more control plots at <http://mcplots.cern.ch>

## If you don't require precision better than 10%

And if you don't look at very exclusive event details (such as isolating specific regions of phase space or looking at specific identified particles)

## Then I believe these guesses are reasonable

$\sigma_{\text{INEL}}$	$\sigma_{\text{EL}}$	
$\sim 80 \text{ mb}$	$\sim 22 \text{ mb}$	@ 13 TeV
$\sim 90 \text{ mb}$	$\sim 25 \text{ mb}$	@ 30 TeV
$\sim 105 \text{ mb}$	$\sim 32 \text{ mb}$	@ 100 TeV

Central  $\langle N_{\text{ch}} \rangle$  density (INEL>0)  
 $\sim 1.1 \pm 0.1 / \Delta\eta\Delta\phi$  @ 13 TeV  
 $\sim 1.33 \pm 0.14 / \Delta\eta\Delta\phi$  @ 30 TeV  
 $\sim 1.8 \pm 0.4 / \Delta\eta\Delta\phi$  @ 100 TeV

Central  $\langle E_T \rangle$  density (INEL)  
 $\sim 1.0 \pm 0.15 \text{ GeV} / \Delta\eta\Delta\phi$  @ 13 TeV  
 $\sim 1.3 \pm 0.2 \text{ GeV} / \Delta\eta\Delta\phi$  @ 30 TeV  
 $\sim 2.0 \pm 0.4 \text{ GeV} / \Delta\eta\Delta\phi$  @ 100 TeV

UE TRNS  $\langle \Sigma p_T \rangle$  density (j100)  
 $\sim 3.3 \pm 0.2 / \Delta\eta\Delta\phi$  @ 13 TeV  
 $\sim 3.65 \pm 0.25 / \Delta\eta\Delta\phi$  @ 30 TeV  
 $\sim 4.4 \pm 0.45 / \Delta\eta\Delta\phi$  @ 100 TeV



## For tuning, Perugia 2012 (PY6) → Monash 2013 (PY8)

Diffraction could still use more dedicated pheno / tuning studies

Baryon and strangeness spectra in pp still not well understood → color reconnections?

Forward region highly sensitive to PDF choice → what do low-x PDFs mean?

# (Multiplicities with $p_T$ cuts)

Indication from LHC is that current PYTHIA models exhibit a slightly too hard  $p_T$  spectrum.

Rates of very soft particles may be underpredicted. Very hard particles may be overpredicted

