OFT with Hadrons Introduction to B Physics

1. Leptonic Decays of Hadrons: from $\pi \rightarrow \ell \nu$ to $B \rightarrow \ell \nu$

QFT in Hadron Decays. Decay Constants. Helicity Suppression in the SM.

2. On the Structure and Unitarity of the CKM Matrix

The CKM Matrix. The GIM Mechanism. The Unitarity Triangle.

3. Semi-Leptonic Decays and the "Flavour Anomalies"

 $B \rightarrow D^{(*)} \ell v$. The Spectator Model. Form Factors. Heavy Quark Symmetry.

 $B \rightarrow K^{(*)} \ell^+ \ell^-$. FCNC. Aspects beyond tree level. Penguins. The OPE.

Quantum Field Theory II

Applications & Phenomenology

Peter Skands Monash University

Recap: Charged-Current Processes at Low Energies

Consider *W* interactions with quarks ("charged current")



For now, assume free quarks, for simplicity

(will reintroduce effects of confinement later.)

Generic amplitude for W exchange between two fermion currents, J_1, J_2 :



Recap: Charged-Current Processes at Low Energies

Consider W interactions with quarks ("charged current")



*Note I use the word **lepton** to refer collectively to charged leptons + neutrinos

Recap: The CKM Matrix



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Note: there *are* other parametrisations, such as the "PDG" parametrisation: same numerical values of V_{ij} , cast in terms of a 3 rotation angles and a phase instead of (λ, A, ρ, η)

The CKM elements in Physical Processes

(Note that most of these processes are charged-current **semileptonic** decays)



Illustration by M. Bona

Consequences of CKM Unitarity 1: The GIM Mechanism

S.L. Glashow, J. Iliopoulos and L. Maiani, Phys. Rev. D2 (1970) 1285.

Off-diagonal CKM terms imply amplitudes for processes like: $K^0 \rightarrow \mu^+ \mu^-$



Expect $M \propto G_F V_{us} \sim G_F \sin \theta_C$

Observed to be much more strongly suppressed (BR~10⁻⁸)

Historical Note: the absence of the processes discussed on this slide led GIM to **predict** the existence of the charm quark!

> (Summed amplitude small but non-zero because $m_c \neq m_u$)

E.g.,: $V_{\mu d} V_{\mu s}^* + V_{cd} V_{cs}^* \sim \cos \theta_C \sin \theta_C - \sin \theta_C \cos \theta_C = 0$

Exercise problem E4: draw diagrams analogous to the one above for these two processes and show how the GIM mechanism is at work in them. Hint: One of the incoming quarks is a "spectator"



Consequences of CKM Unitarity 2: The Unitarity Triangle(s)

Write the unitarity constraints explicitly:

$$\sum_{j} V_{ij} V_{jk}^{\dagger} = \delta_{ik} \qquad \text{e.g.} \qquad V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = \delta_{ik}$$

Sum of three complex numbers = 0



Normalise by $|V_{cd}V_{cb}^*|$:



University

= 0rs = 0

Recap: The Unitarity Triangle*

This is called "the unitarity triangle"



Note: complex phases \Rightarrow **CP Violation** (Note: requires **interfering** amplitudes) ► Measurements of CPV processes constrain relative phases.

$$\alpha = \arg[-V_{td}V_{tb}^{*}/V_{ud}V_{ub}^{*}] = \phi_{2}$$

$$\beta = \arg[-V_{cd}V_{cb}^{*}/V_{td}V_{tb}^{*}] = \phi_{1}$$

$$\gamma = \arg[-V_{ud}V_{ub}^{*}/V_{cd}V_{cb}^{*}] = \phi_{3}$$

Different weak processes probe different combinations of the CKM elements -> constrain different sides or angles in the triangle. **Measure many processes**

(*In principle, each unitarity constraint has its own "triangle" - this is the standard one.)



Exercise problem E5: show mathematically why CPV is only observable in processes with at least two interfering amplitudes with different relative CKM phases.

→ Overconstrain the triangle = Test SM

Constraints on the CKM Triangle

Example: "Our" process, $B \rightarrow \tau v$, is proportional to $|V_{ub}|^2$:



The Current Picture





Now (2018)

Why keep going?

The triangle *has to* break, at some point...

- For 2023, explain the Sakharov conditions
- + maybe general considerations: new physics easily introduces new phase(s)

Summary of Problems and Exercises for Self Study

E4. Draw diagrams for processes on <u>p.6</u>; explain their GIM suppression E5. Show why CPV is only physically observable in processes with at least two interfering amplitudes with different CKM phases.

E6. Draw LO Feynman diagrams for (1) $D^0 \rightarrow K^+\pi^-$ and (2) $D^0 \rightarrow K^-\pi^+$, and explain the observation that $\Gamma_{(1)} / \Gamma_{(2)} \sim 4 \times 10^{-3}$.

> You will present your progress on these in the next lesson and we will discuss any questions / issues you encounter.

Assignment Problems 1&2 : the B physics research problems



An example of a recent conundrum

Discrepancies between inclusive and exclusive determinations of V_{cb} and V_{ub}



An example of a recent conundrum

