



Pythia

(ピューティアー)

# Pythia $\longleftrightarrow$ Belle II



Peter Skands (University of Oxford & Monash University)

## PART 1

1. Introduction to **Event Generators**
2. Constraining Pythia at LEP  $\longleftrightarrow$   $q\bar{q}$  continuum
3. Pythia for **B Decays**

## PART 2

4. Tuning Approaches
5. The MCPLOTS event-generator **validation resource**



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# Event Generators: Divide and Conquer

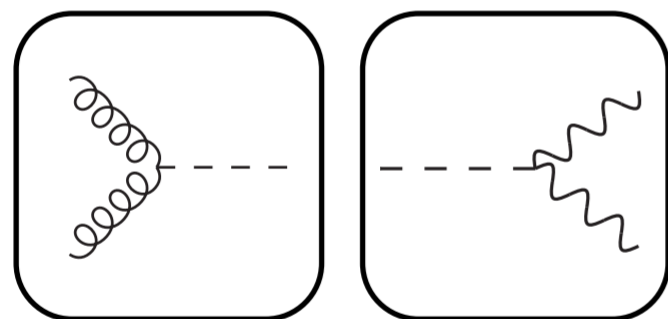
Model full event structure by repeated/nested **factorizations**

→ Split the problem into many ~ simple pieces

$$\mathcal{P}_{\text{event}} = \underbrace{\mathcal{P}_{\text{Hard}} \otimes \mathcal{P}_{\text{Res}} \otimes \mathcal{P}_{\text{FSR}} \otimes \mathcal{P}_{\text{Had}} \otimes \mathcal{P}_{\text{Dec}} \otimes \dots}$$

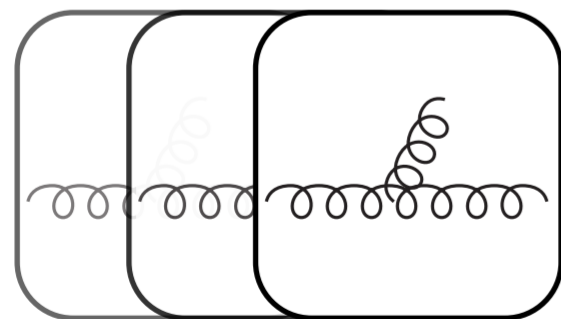
Quantum mechanics → **Probabilities** → Make **Random Choices** (as in nature)

→ **Markov-Chain Monte Carlo** → "Event Generators"



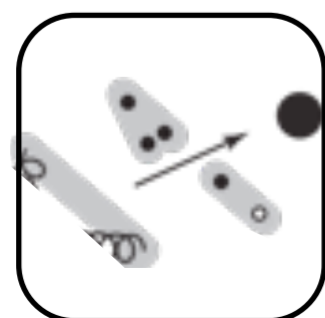
## Hard Process & Decays:

Process-specific (N)LO matrix elements → Sets "Hard" scale:  $Q_{\text{MAX}}$



## Accelerated Charges → Perturbative Bremsstrahlung:

Differential evolution,  $dP/dQ^2$ , from  $Q_{\text{MAX}}$  to  $Q_{\text{Hadronization}} \sim 1 \text{ GeV}$



## Hadronization (and hadron decays)

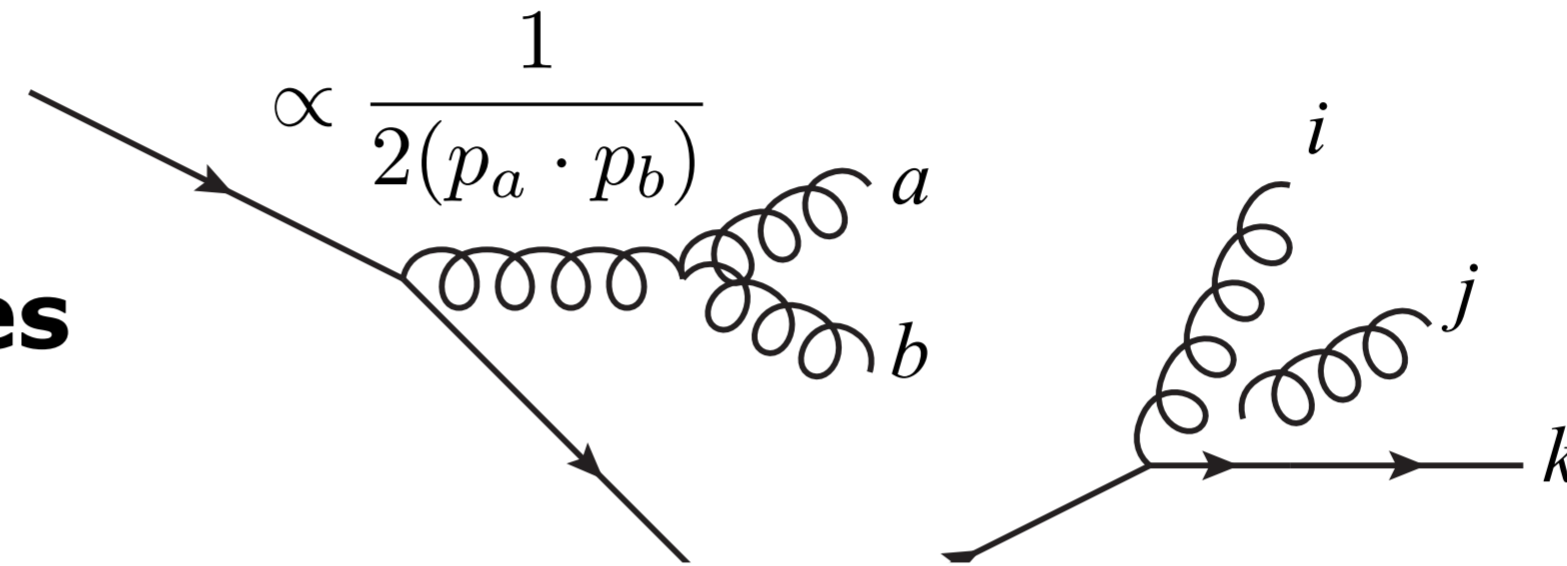
Non-perturbative model of color-singlet parton systems → hadrons

# 1) Bremsstrahlung via Parton Showers

see e.g PS, *Introduction to QCD*, TASI 2012, arXiv:1207.2389

**Most bremsstrahlung** is driven by **divergent propagators** → simple structure

Mathematically, **gauge amplitudes factorize** in singular limits



Partons  $ab$   
→ **collinear:**

$$|\mathcal{M}_{F+1}(\dots, a, b, \dots)|^2 \xrightarrow{a \parallel b} g_s^2 \mathcal{C} \frac{P(z)}{2(p_a \cdot p_b)} |\mathcal{M}_F(\dots, a + b, \dots)|^2$$

$P(z)$  = **DGLAP splitting kernels**, with  $z = E_a / (E_a + E_b)$

Gluon  $j$   
→ **soft:**

$$|\mathcal{M}_{F+1}(\dots, i, j, k, \dots)|^2 \xrightarrow{j_g \rightarrow 0} g_s^2 \mathcal{C} \frac{(p_i \cdot p_k)}{(p_i \cdot p_j)(p_j \cdot p_k)} |\mathcal{M}_F(\dots, i, k, \dots)|^2$$

**Coherence** → Parton  $j$  really emitted by  $(i, k)$  “dipole” or “**antenna**” (**eikonal factors**)

These are the **building blocks of parton showers** (DGLAP, dipole, antenna, ...) (+ running coupling, unitarity, and explicit  $(E, p)$  conservation.)

# Shower Uncertainties: Non-Singular Variations in Pythia 8

## Parton Showers rely on Factorisations in Soft/Collinear Limits

$$|M_{n+1}|^2 \rightarrow \sum_{\text{radiators}} a_{\text{sing}} |M_n|^2$$

Approximations based on universal singular structures of gauge theories.

Driven by  $1/Q^2$  poles from propagators, with spin-dependent numerators

Renormalization-scale variations **only** produce terms  $\propto$  to these “kernels”

## But genuine matrix elements also have “non-singular terms”

Our solution

[[Vincia 1102.2126](#); [Pythia 1605.08352](#)]

Non-singular variations

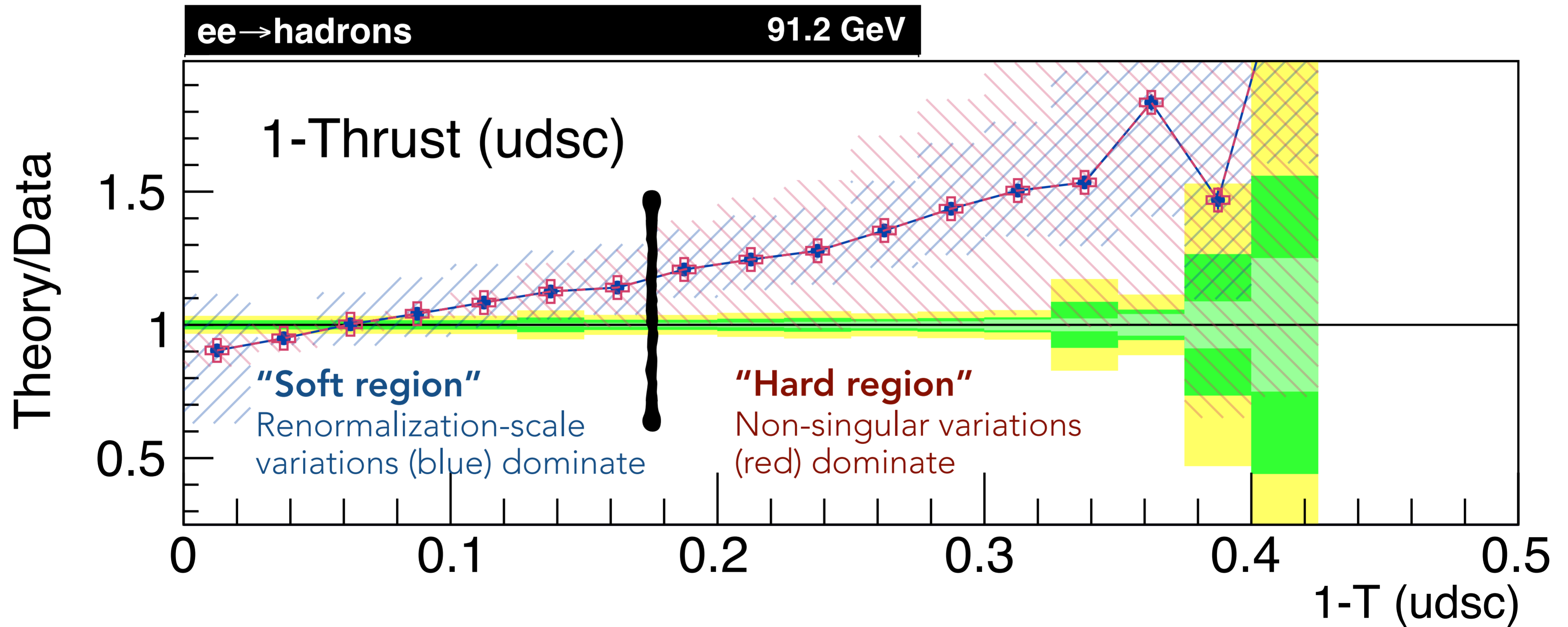
$$a_{\text{sing}} \rightarrow a_{\text{sing}} + \Delta a_{\text{non-sing}}$$

Can also be helpful to estimate need for higher matching/merging

# Non-Singular Variations: Example

Example from Mrenna & **PS**, Automated Parton-Shower Variations in Pythia 8, [1605.08352](#)

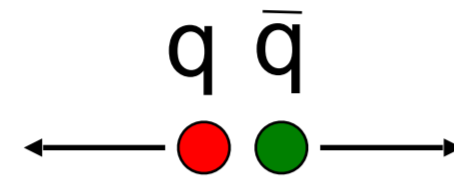
Can vary **renormalisation scale** and **non-singular terms** independently



Note: ME corrections were switched off for illustration. Would reduce red band, but not blue.

## 2) Hadronization and Jets

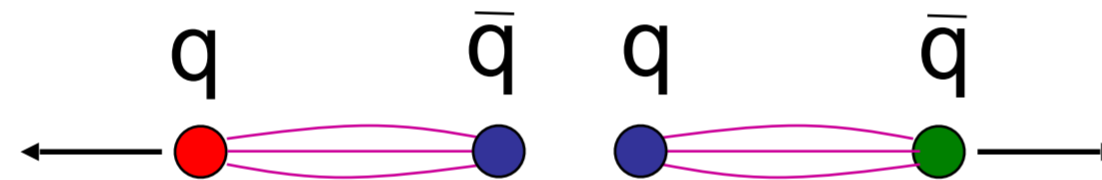
Consider a quark and anti-quark produced in  $e^+e^-$  annihilation



i) Initially Quarks separate at high velocity



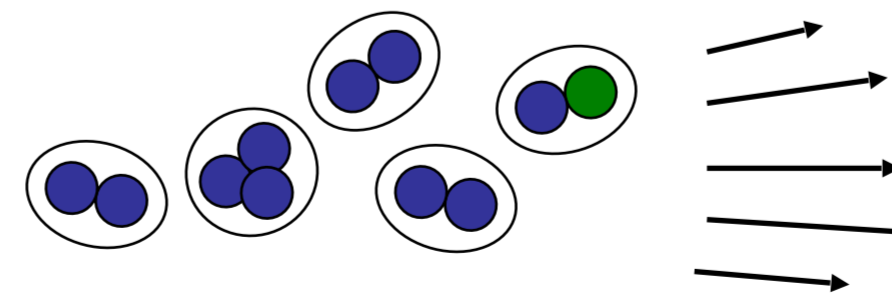
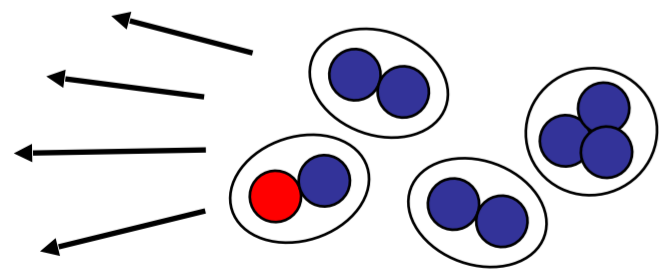
ii) Colour flux tube forms between quarks



iii) Energy stored in the flux tube sufficient to produce new  $\bar{q}q$  pairs

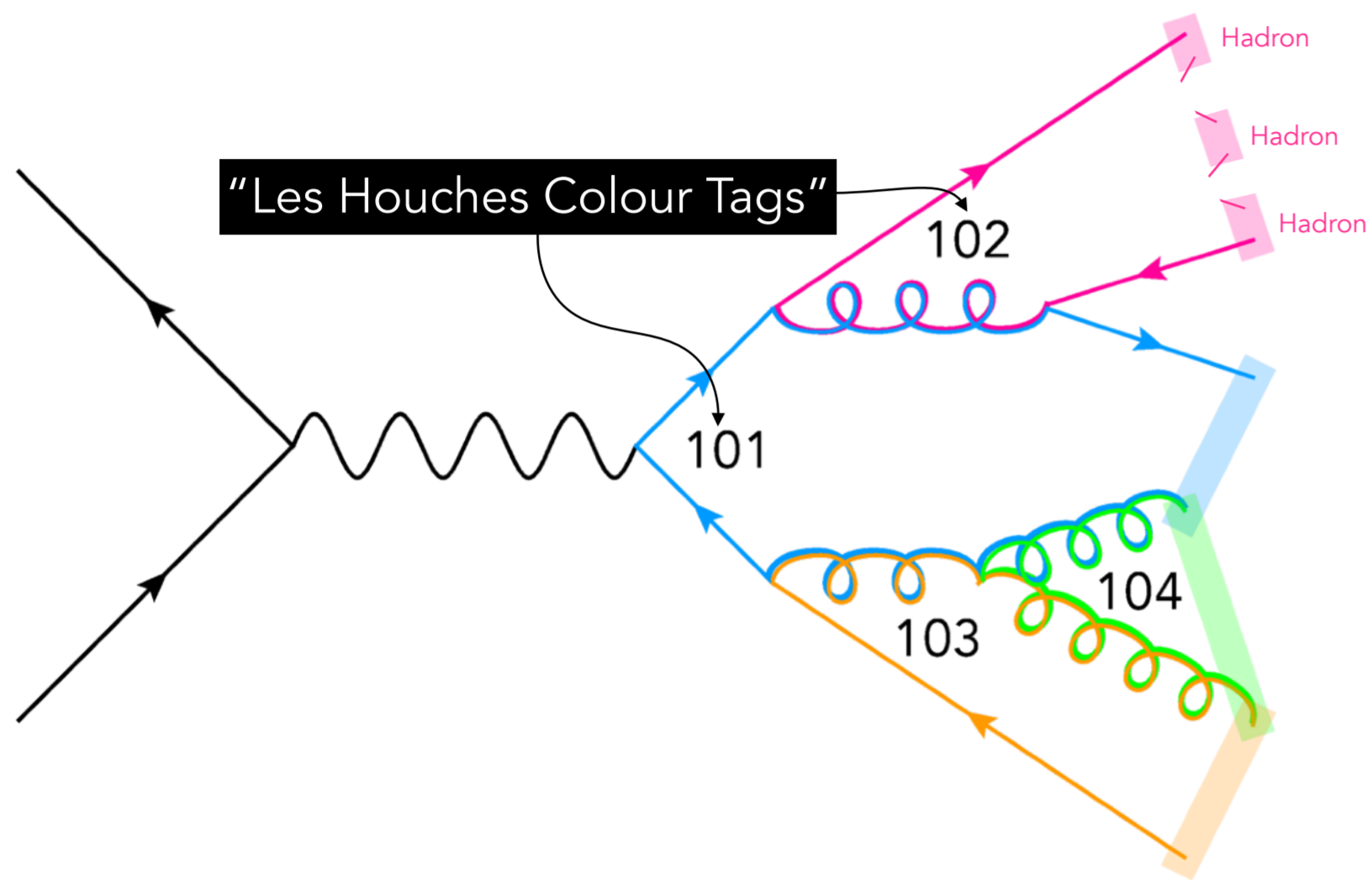


iv) Process continues  $\implies$   
Jets of colourless hadrons

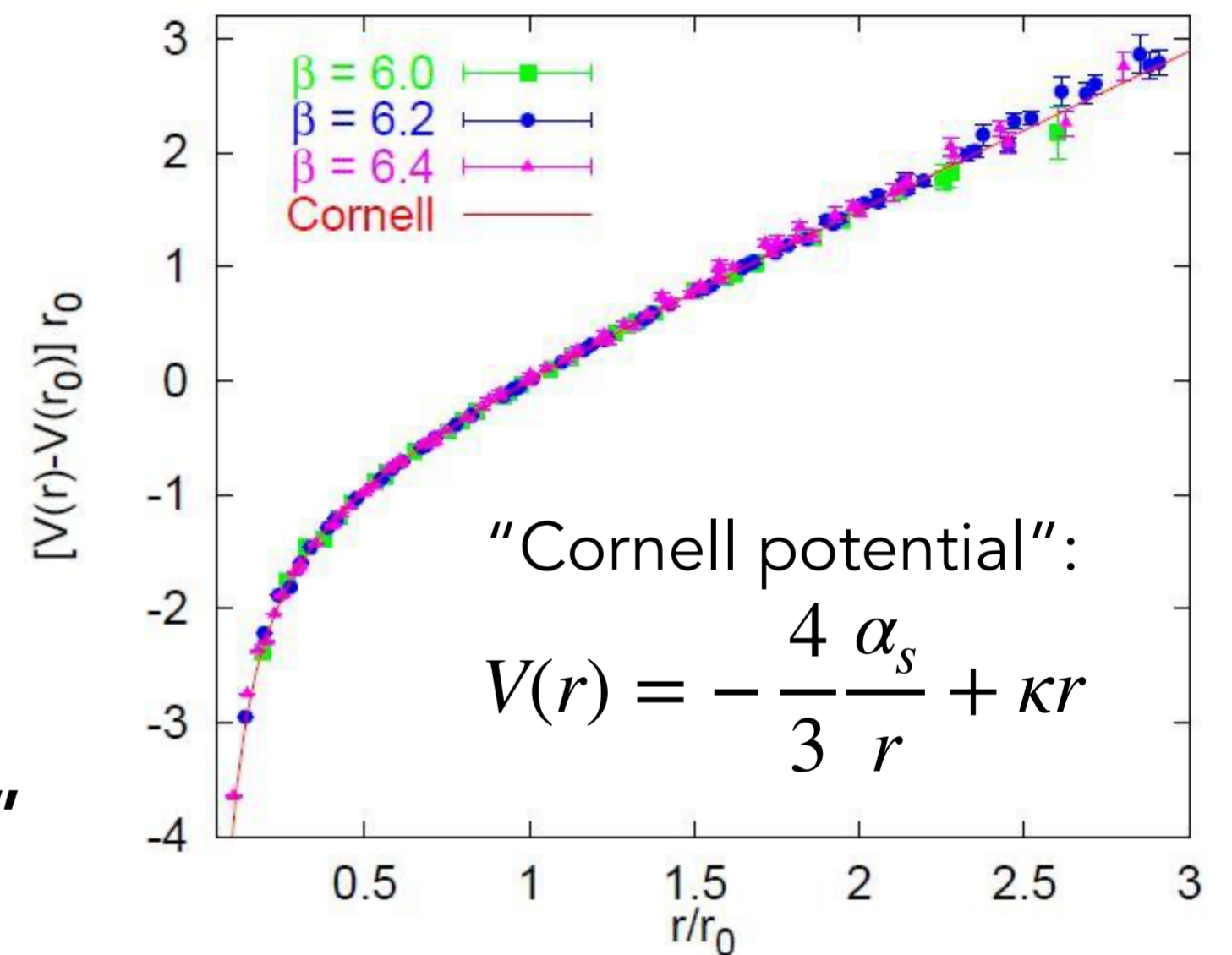


# Confinement in PYTHIA: *The Lund String Model*

**Simplified** (leading- $N_c$ ) “colour flow” → determine between which partons to set up confining potentials



“Linear confinement”  
(From Lattice & Hadron Spectroscopy)



**Map to Strings:** Quarks → string endpoints; gluons → “kinks”

System then evolves as a string world sheet

+ **String breaks** via spontaneous  $q\bar{q}$  pair creation (“Schwinger mechanism”) → **hadrons**

**Baseline string model formulated in continuum limit of asymptotically “long” strings:**  $E_{\text{CM}} \gtrsim 10 \text{ GeV}$

 **Belle II** could provide **extremely accurate constraints** at the lower endpoint of the dynamical range?

 + test for **small-system modifications** ↔ eg non-universal best-fit tune parameters

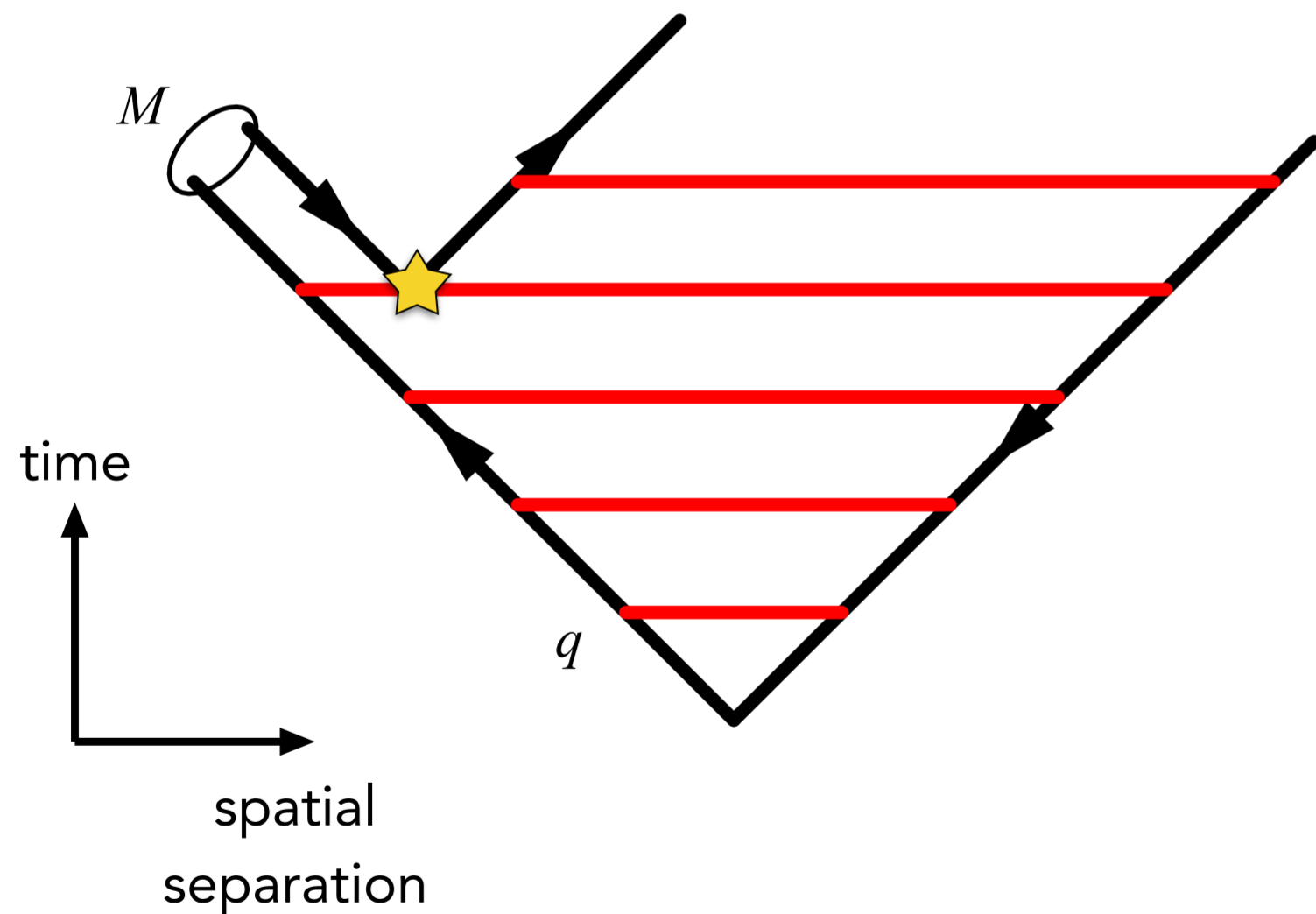
# String Breaking

## In "unquenched" QCD

$g \rightarrow q\bar{q} \implies$  The strings will "break"

Non-perturbative so can't use  $P_{g \rightarrow q\bar{q}}(z)$

Model: Schwinger mechanism



J. Schwinger, Phys. Rev. **82** (1951) 664

## Schwinger Effect

Non-perturbative creation of  $e^+e^-$  pairs in a strong external Electric field

Probability from Tunneling Factor

$$\mathcal{P} \propto \exp\left(\frac{-m^2 - p_{\perp}^2}{\kappa/\pi}\right)$$

( $\kappa$  is the string tension equivalent)

→ Gaussian suppression of high  $m_{\perp} = \sqrt{m_q^2 + p_{\perp}^2}$

Assume probability of string break constant per unit world-sheet area



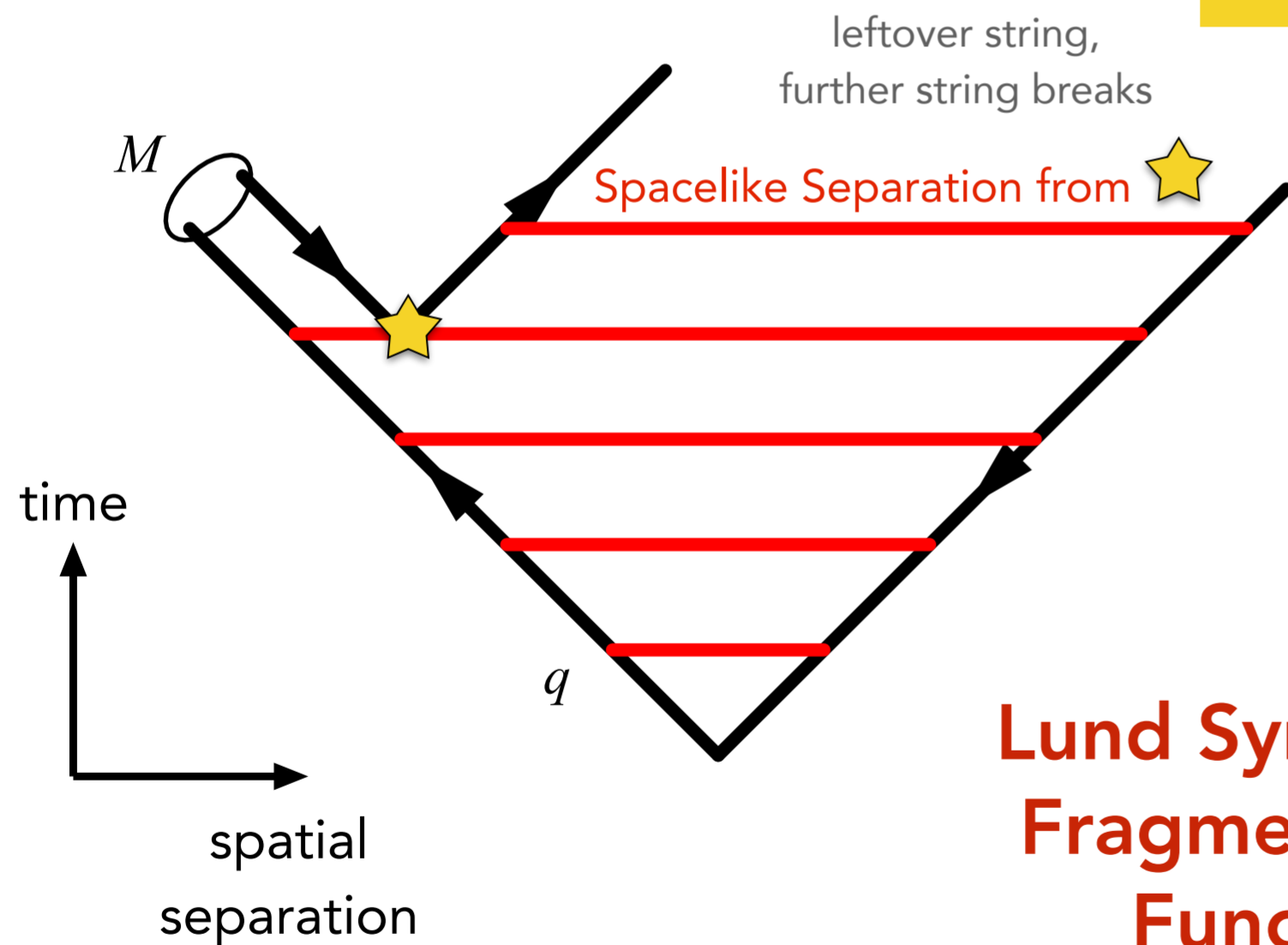
# Schwinger Case: the String Fragmentation Function

**Schwinger**  $\implies$  **Gaussian  $p_{\perp}$  spectrum** (transverse to **string axis**) & **Prob(d:u:s)  $\approx 1 : 1 : 0.2$**

The meson  $M$  takes a fraction  $z$  of the quark momentum,

Probability distribution in  $z \in [0,1]$  parametrised by **Fragmentation Function**,  $f(z, Q_{\text{HAD}}^2)$

**Observation:** All string breaks are **causally disconnected**



Lorentz invariance  $\implies$  string breaks can be considered in *any order*. Imposes "left-right symmetry" on the **FF**

$\implies$  **FF** constrained to a form with **two free parameters**,  $a$  &  $b$ : constrained by fits to measured hadron spectra

**Lund Symmetric  
Fragmentation  
Function**

$$f(z) \propto \frac{1}{z} (1-z)^a \exp\left(-\frac{b(m_h^2 + p_{\perp h}^2)}{z}\right)$$

↑  
Supresses  
high-z hadrons

↑  
Supresses  
low-z hadrons

# Constraining PYTHIA (in the $q\bar{q}$ continuum)

We use a combination of **Infrared Safe\*** and **Infrared Sensitive** observables

⇒ Stereo Vision on perturbative and nonperturbative QCD respectively

Some overlap / interplay: IR Safe becomes Sensitive at low scales & IR Sensitive seeded by IR Safe.

**IR Safe Observables** satisfy two simultaneous conditions

**1) Soft Safe:** observable does not change when adding soft partons/particles

E.g., adding infinitely soft gluons (perturbative), or soft pions (non-perturbative)

**2) Collinear Safe:** observable does not change when splitting a particle collinearly

E.g., doing a  $g \rightarrow gg$  or  $g \rightarrow q\bar{q}$  splitting, or a  $\rho \rightarrow \pi\pi$  decay, in limit of zero opening angle.

→ Hadronization and hadron decays suppressed by powers of  $\Lambda_{\text{QCD}}/Q$

**Full Set of IR Safe Observables:**

**Event Shapes:** typically Thrust Family, Linearised Sphericity Family, EECs, Angularities

**Jet Rates:** typically Durham kT resolutions (but other clustering algorithms also interesting)

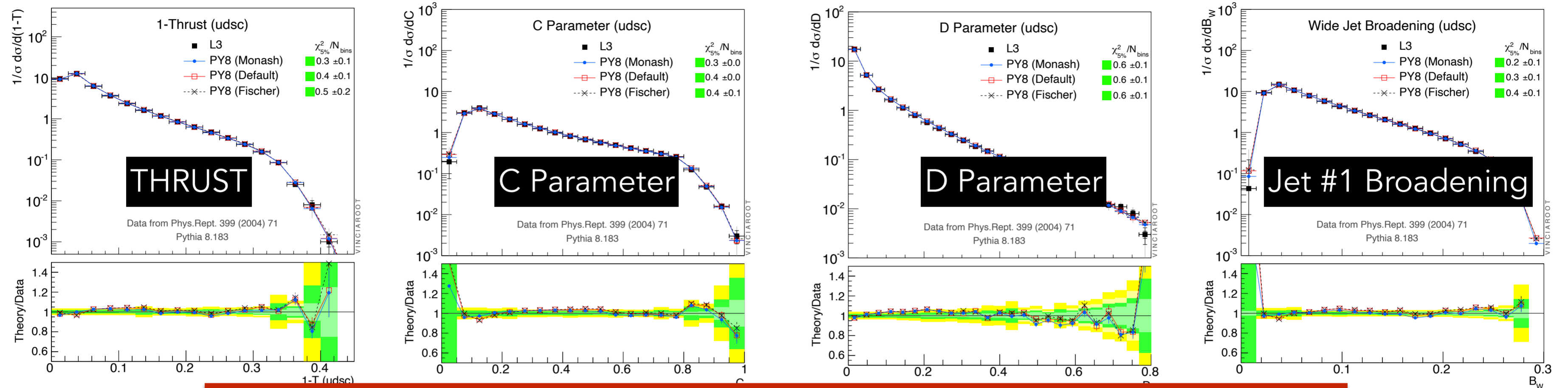
**Jet Structure:** Jet Masses, Jet Broadenings, Jet Shapes

Sometimes done using Charged Tracks only, for best experimental resolution.

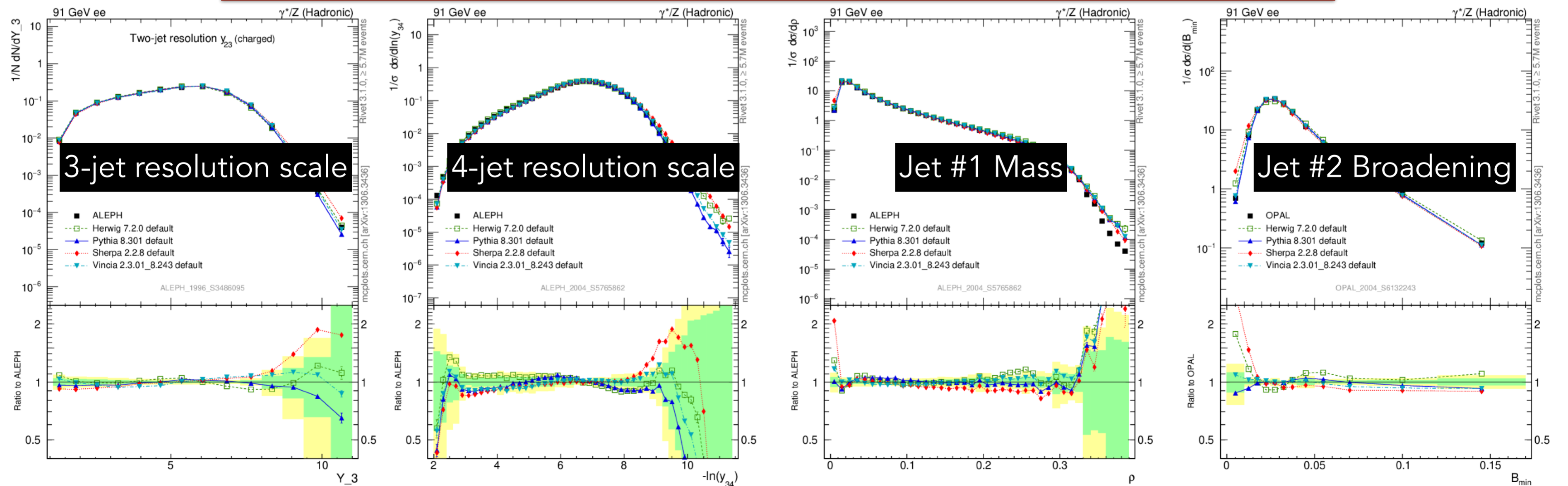
\*Sometimes referred to as IRC safe

# Constraining PYTHIA: IR Safe Observables (main examples) (at $\sqrt{s} \sim m_Z$ )

Top Row: from PS et al., "Tuning PYTHIA 8.1: the Monash 2013 Tune", Eur.Phys.J.C 74 (2014) 8



Question: could Belle II separate  $e^+e^- \rightarrow \gamma^* \rightarrow c\bar{c}$  out from  $d\bar{d}, u\bar{u}, s\bar{s}$ ?



Bottom Row: from [mcplots.cern.ch](http://mcplots.cern.ch)

## Multiplicities, Spectra, and Correlations

Inclusive charged particles

Identified particles (rates and ratios).

**+ correlations**, with event multiplicity, with rapidity along jet axis, with ... ?

 Strangeness correlations, baryon correlations, ...

## Spectra

Conventional absolute momentum fraction:  $x_p = \frac{2|p|}{E_{\text{CM}}}$

 But, even at  $E_{\text{CM}} \sim 10$  GeV, these hadrons are produced in **jets**;

**Jets have longitudinal and transverse axes:**

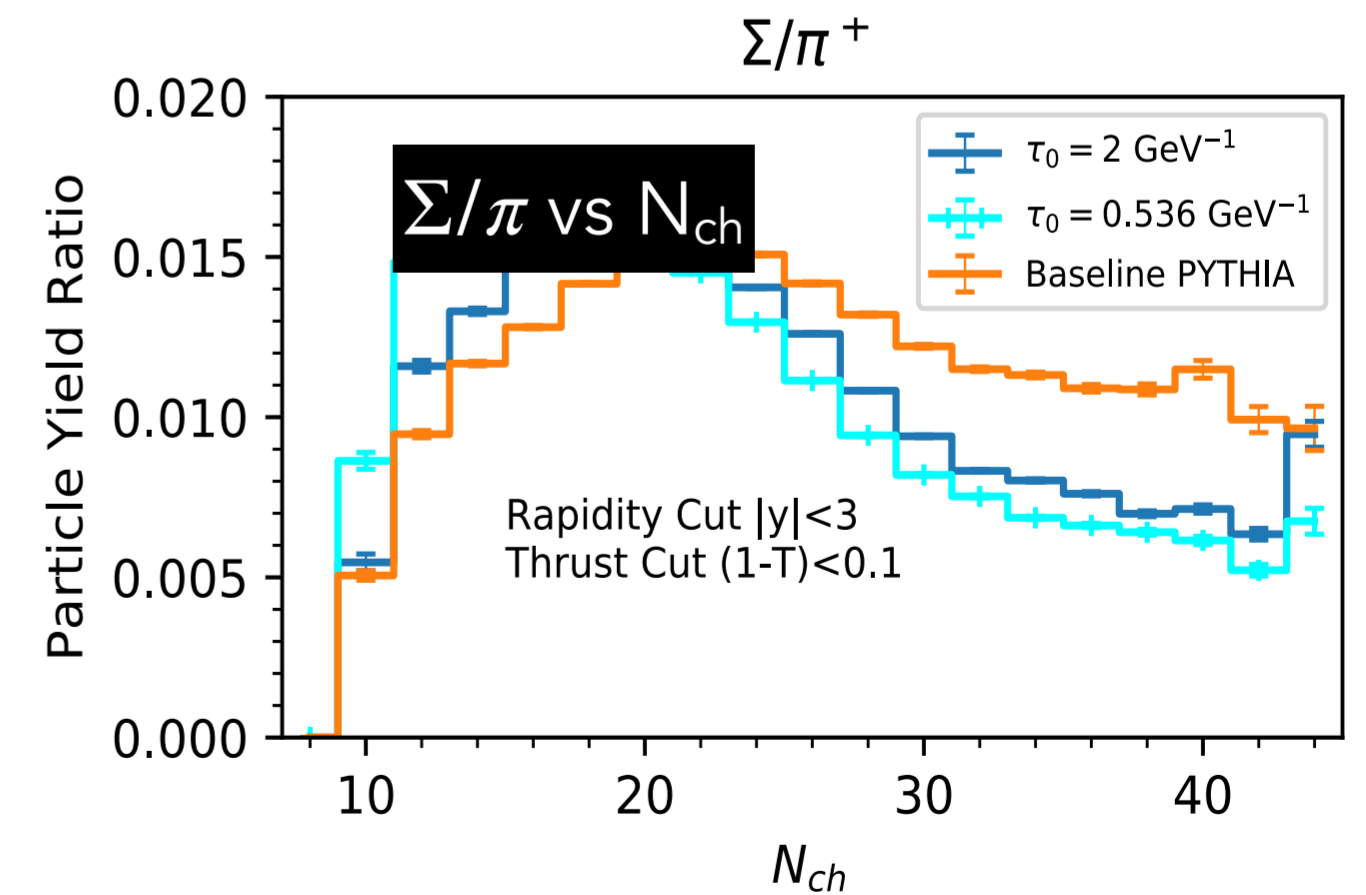
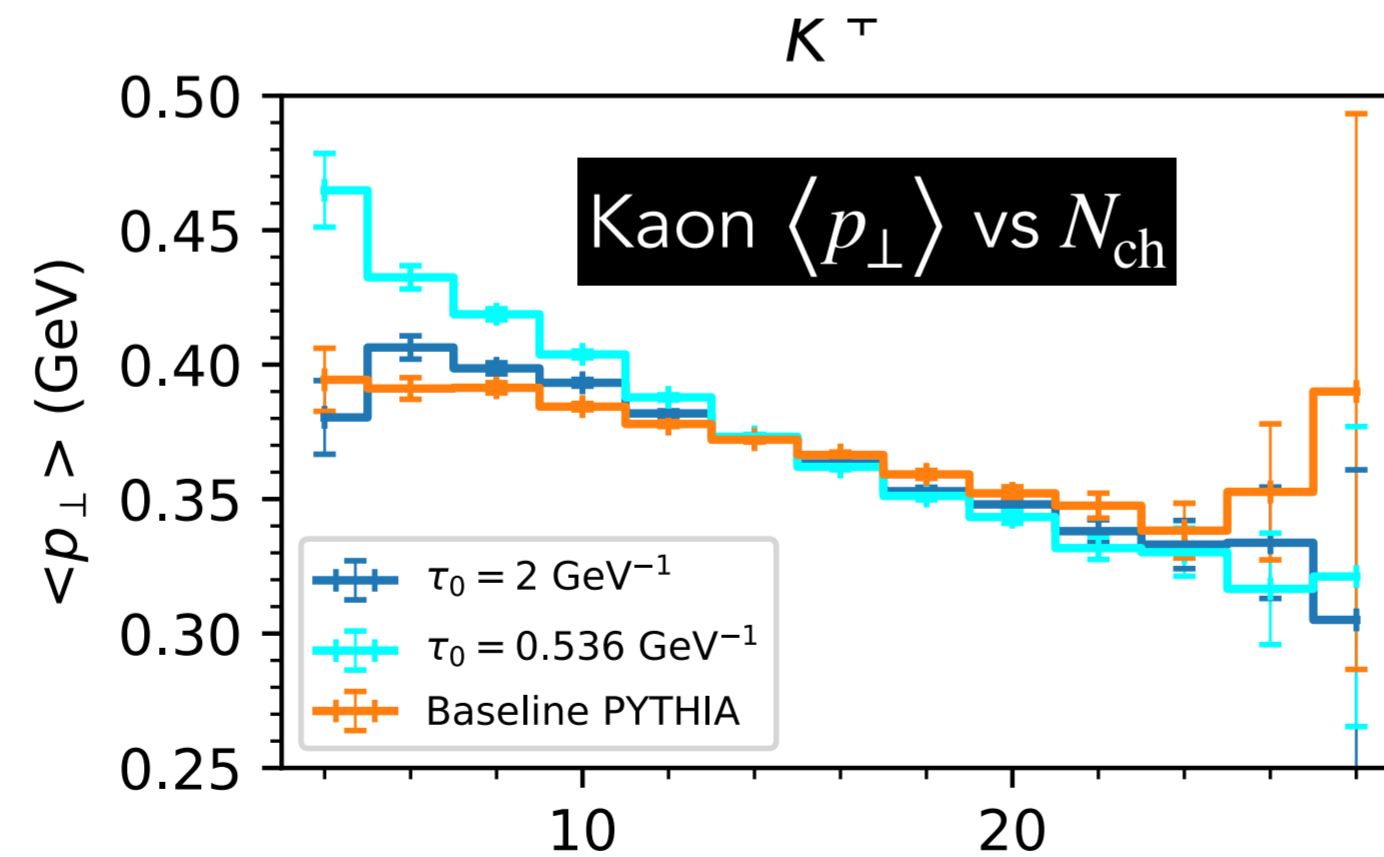
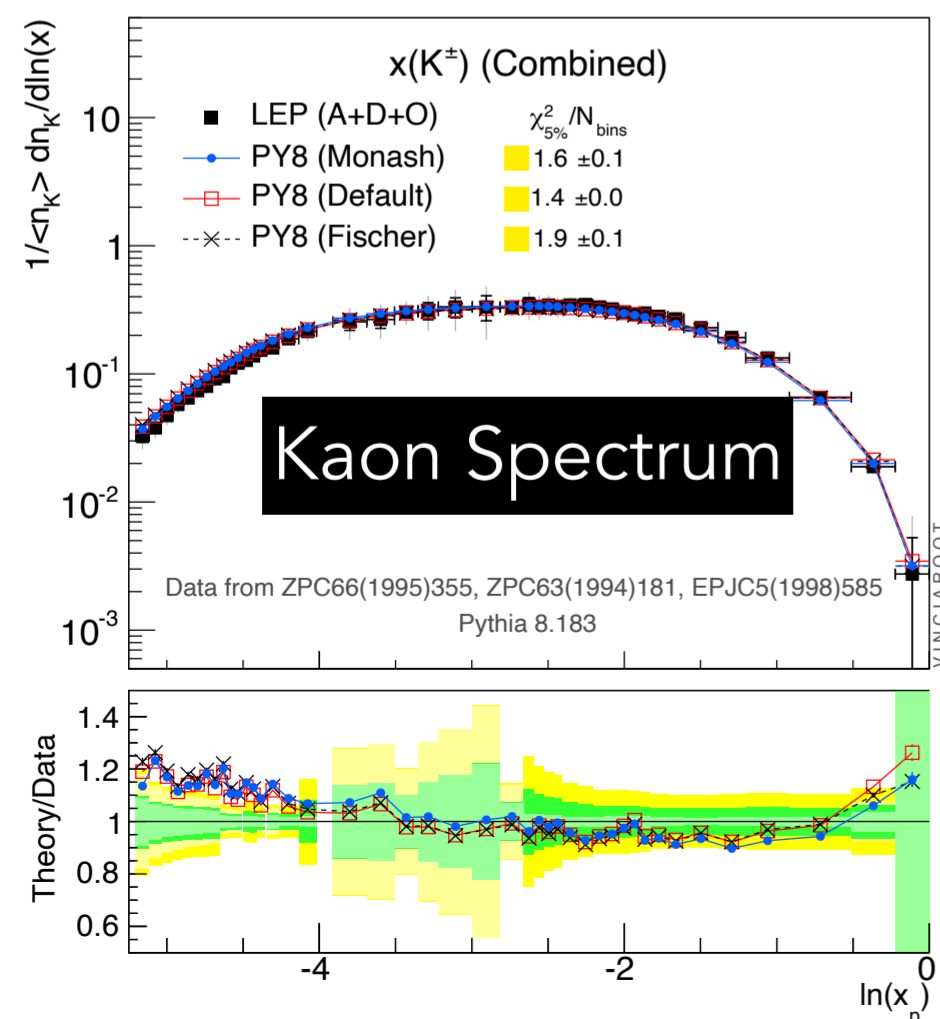
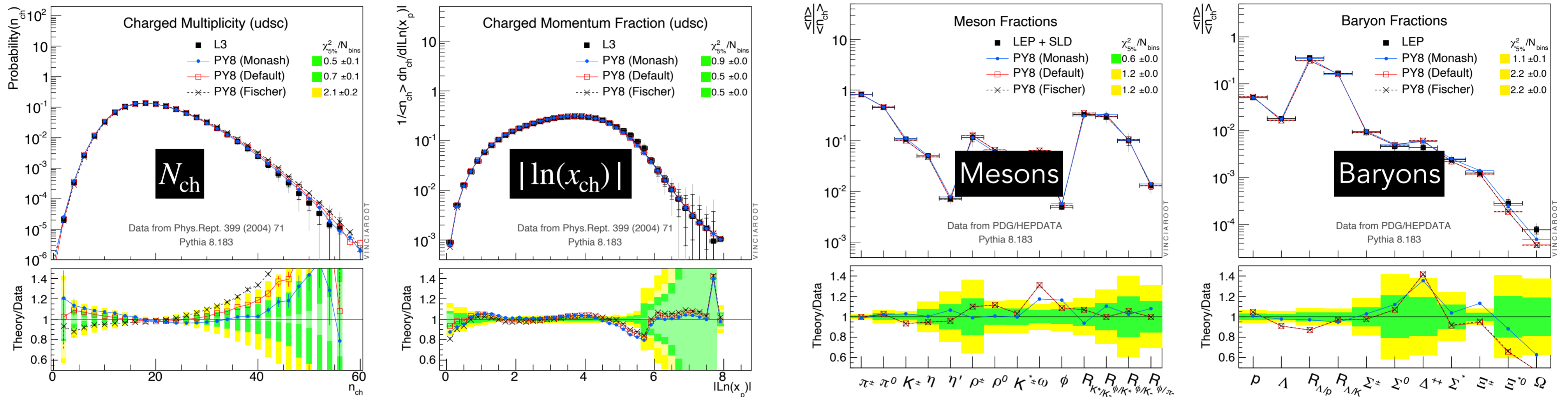
**More information: rapidity spectra** (along primary event/jet axis) :  $dn_{\text{ch}}/dy$ ,  $dn_{\text{PID}}/dy$

And momentum **transverse to it**,  $dn/dp_{\perp}$  ; + Let 2<sup>nd</sup> axis define a plane  $\implies p_{\perp\text{in}}, p_{\perp\text{out}}$

# Main Examples of IR Sensitive Observables

(at  $\sqrt{s} \sim m_Z$ )

Top Row: from PS et al., "Tuning PYTHIA 8.1: the Monash 2013 Tune", *Eur.Phys.J.C* 74 (2014) 8



Bottom Right Plots: from "String Fragmentation with a Time-Dependent Tension", N. Hunt-Smith & PS, *Eur.Phys.J.C* 80 (2020) 11

## 30% of B meson decays modelled as partonic transitions, with spectator

Passed back to PYTHIA for re-hadronisation (with same string parameters as at LEP).

How reliable is this modelling really? Not aware anyone has looked at that since org papers.

These tend to be high-multiplicity (multi-prong) modes

Rarely used as signals. But enter as backgrounds, and tagging modes?

Experimental constraints on these? Belle II, LHCb, ALICE ... ?

 **Would like to discuss, if there is interest, what Belle II could do here?**

## QED Radiative Corrections in B Decays

HERWIG and SHERPA have dedicated modules, based on “YFS” formalism

For PYTHIA, QED in hadron decays is normally done with **PHOTOS**

**Now:** looking at adapting the **QED Multipole Shower Module from VINCIA**

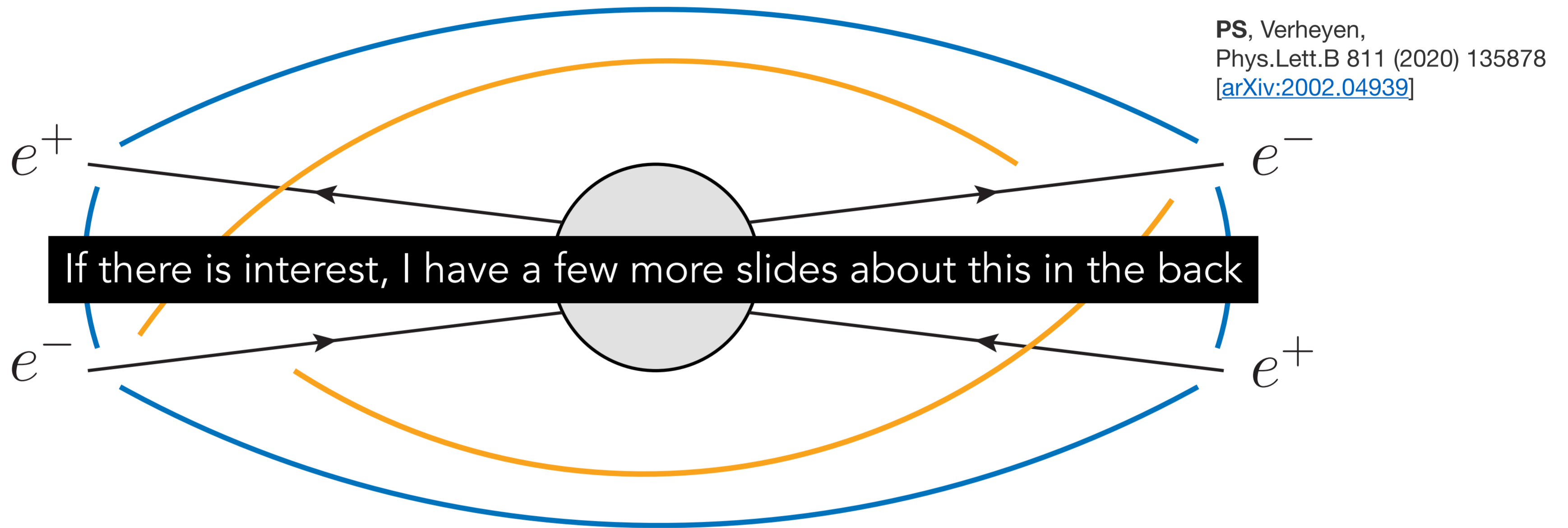
Native C++ and built-in in PYTHIA → thread-safe and trivial to parallelise

May be superior to YFS in some ways + modern shower formalism ⇒ matching, merging, ...

 **Would this be interesting to Belle II ?**

# QED Multipole Radiation Patterns

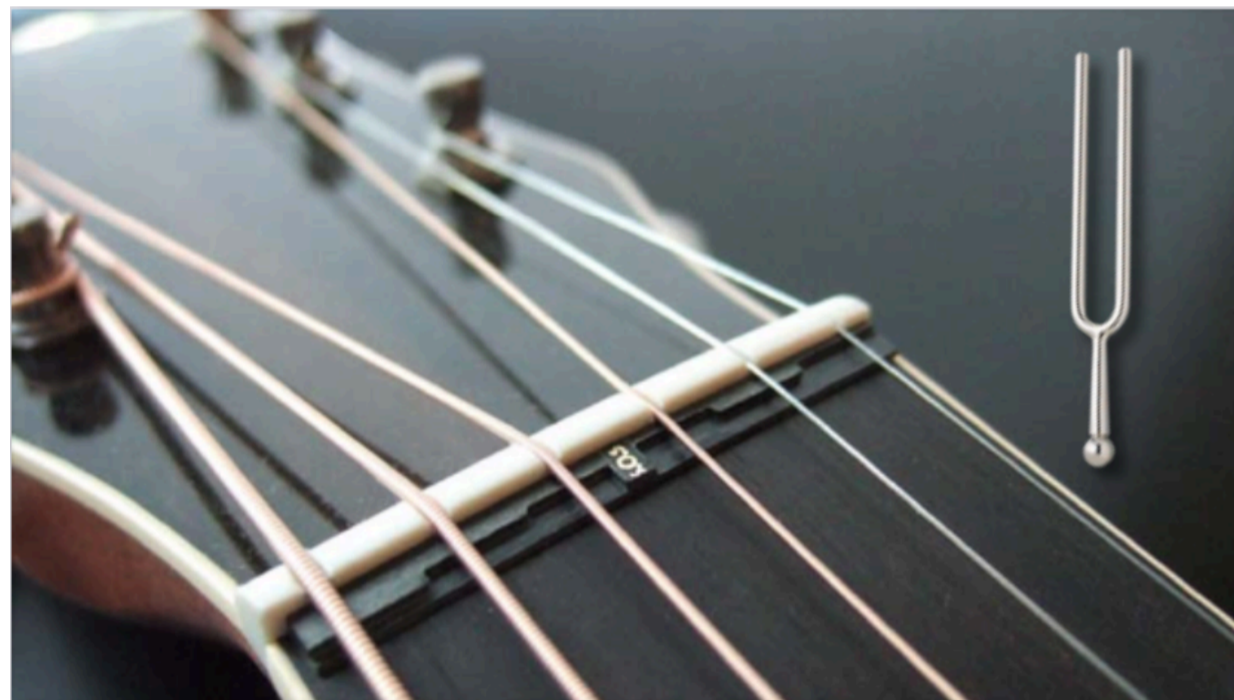
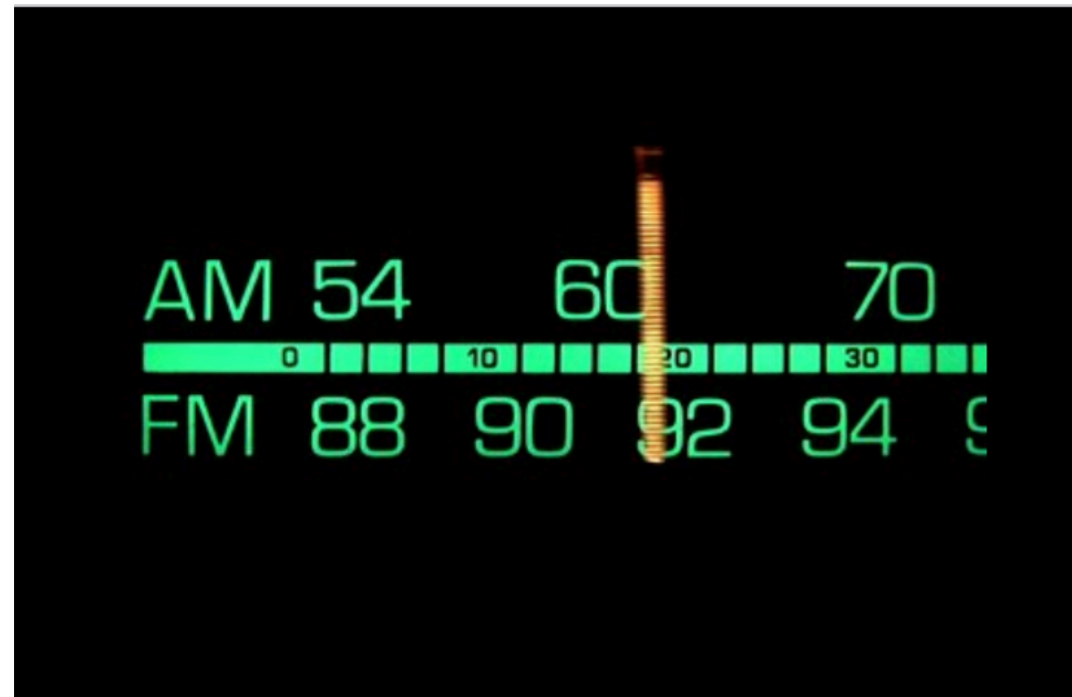
Example: Quadrupole final state (4-fermion:  $e^+e^+e^-e^-$ )



PS, Verheyen,  
Phys.Lett.B 811 (2020) 135878  
[\[arXiv:2002.04939\]](https://arxiv.org/abs/2002.04939)

Soft Photon Emission:  $|M_{n+1}(\{p\}, p_j)|^2 = -8\pi\alpha \sum_{x,y}^n \sigma_x Q_x \sigma_y Q_y \frac{s_{xy}}{s_{xj} s_{yj}} |M_n(\{p\})|^2$   
[Dittmaier, 2000]

- Opposite-charge pairs  $\blacktriangleright$  positive terms
- Same-charge pairs  $\blacktriangleright$  negative terms



**PART 2**

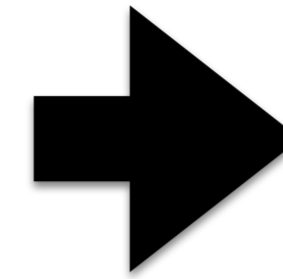
# Tuning



# Tuning: PROFESSOR — a powerful tool for (semi)automated tuning

Inspired by idea pioneered by DELPHI (Hamacher et al., 1995):

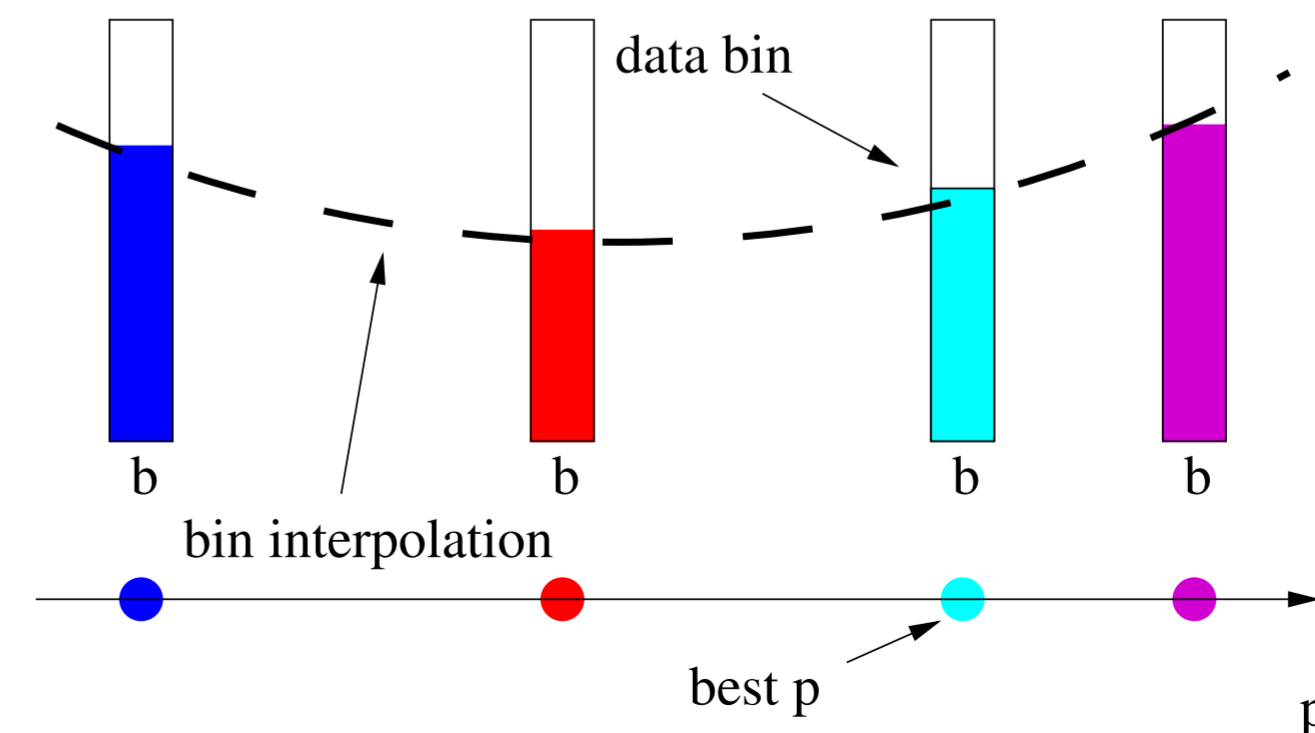
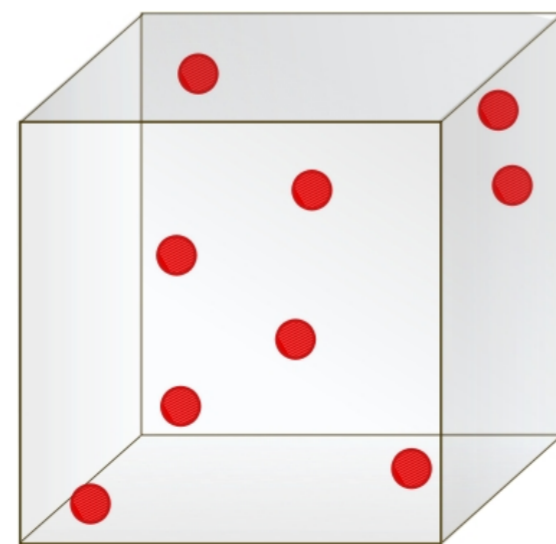
Bin-wise interpolation of MC generator response and  $\chi^2$  minimization  
2<sup>nd</sup>-order polynomials account for parameter correlations.



Modern Python Package  
with much more functionality,  
tutorials, etc.  
<https://professor.hepforge.org/>

## Professor Tuning procedure

- 1 Random sampling:  $N$  parameter points in  $n$ -dimensional space
- 2 Run generator and fill histograms
- 3 For each bin: use  $N$  points to fit interpolation (2<sup>nd</sup> or 3<sup>rd</sup> order polynomial)
- 4 Construct overall (now trivial)  $\chi^2 \approx \sum_{bins} \frac{(interpolation - data)^2}{error^2}$
- 5 and Numerically *minimize* pyMinuit, SciPy



I would (by now) recommend using PROFESSOR. Wisely.

## Some Dangers:

**Overfitting:** very precisely measured data points can generate large  $\chi^2$  values even if MC gets within what one would naively consider “reasonable” agreement

Fit reacts by sacrificing agreement elsewhere (typically in tails) to improve  $\chi^2$  in peaks.

PROFESSOR now has facility to include a “sanity limit” (e.g., 5%) “theory uncertainty”

► Fit not rewarded (much) for improving agreement beyond that point. More freedom in tails.

Also tends to produce  $\chi_{5\%}^2$  values  $\sim$  unity  $\rightarrow$  better uncertainty bands?

**Incompatibilities:** model may be **unable** to agree with (some part of) a given measurement

Fit reacts by desperately trying to reduce order-of-magnitude differences in bins it shouldn't have been asked to fit in the first place, at cost of everything else ► total garbage.

Choose measurements carefully — within domain of applicability of physics model

+ PROFESSOR now has facility to not penalise  $\chi^2$  beyond some max deviation.

# Some Helper Tools

## Wouldn't it be nice if there was a tool:

That could automatically detect correlations between parameters and observables.

And tell you which "groups" they fall into naturally : which parameter sets you should ideally tune together, and which are more nicely factorised.

## This is (at least partly) what the tool **AutoTunes** does [Bellm, Gellersen, Eur.Phys.J.C 80 \(2020\)](#)

I won't have time to discuss that today, but I think it looks promising

I encourage you to study it and use it

## You may also be interested in **Apprentice** [Krishnamoorthy et al., EPJ Web Conf. 251 \(2021\) 03060](#)

Variance reduction to semi-automate how to weight observables & bins

# Practical Example: Uncertainties on Dark-Matter Annihilation Spectra

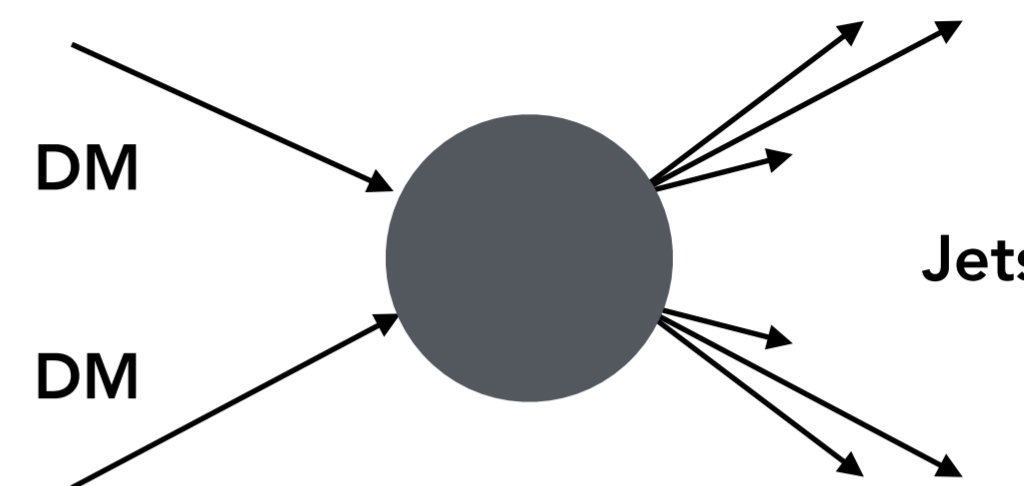
Based on A. Jueid et al., [1812.07424](#) (gamma rays, eg for GCE) and [2202.11546](#) (antiprotons, eg for AMS) + [2303.11363](#) (all)

## Compare different generators?

E.g., HERWIG – PYTHIA

Problem: tuned to ~ same data

Difference not guaranteed to span genuine uncertainties



## Instead, did parametric refittings of LEP data within PYTHIA's modelling

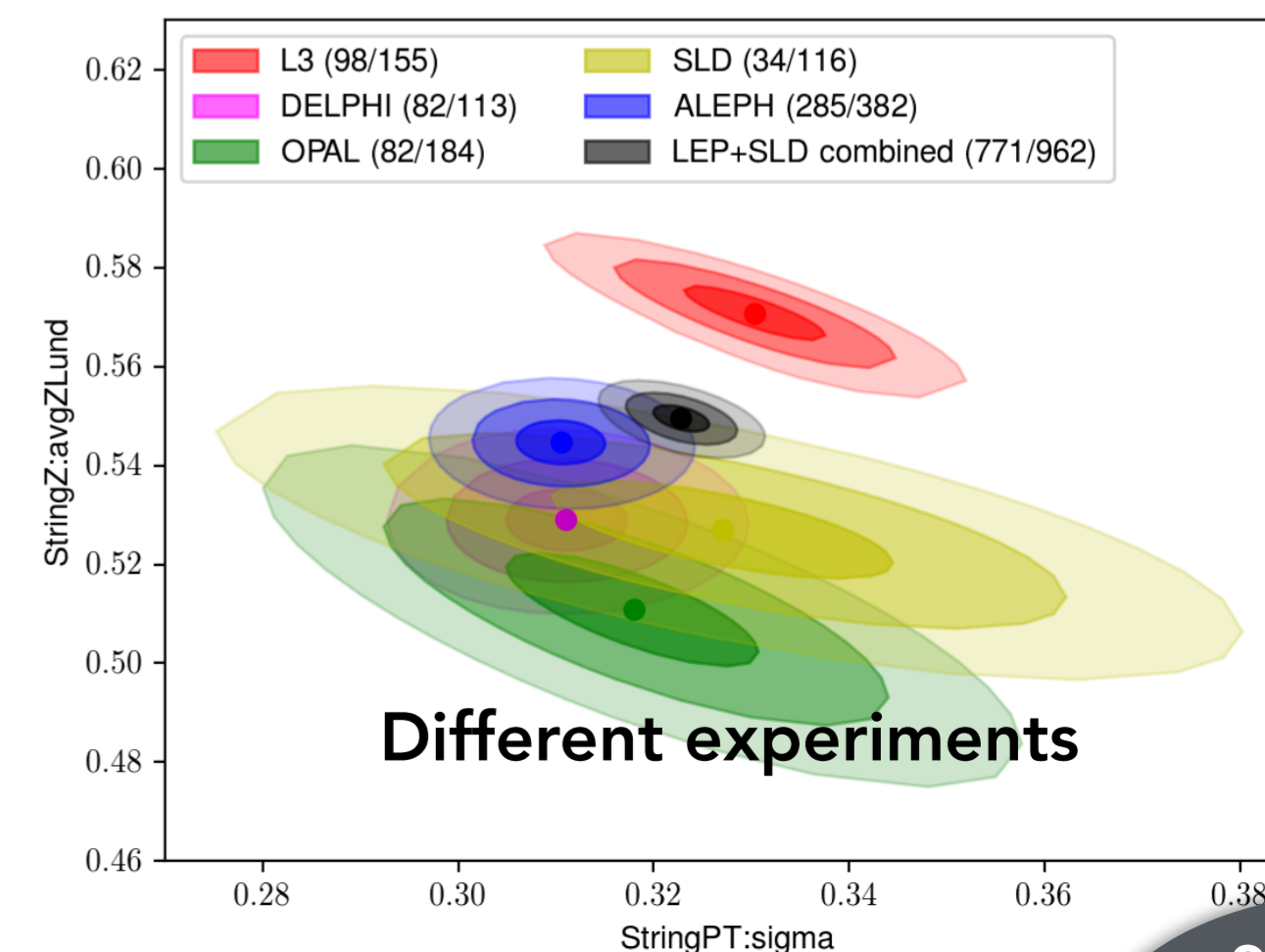
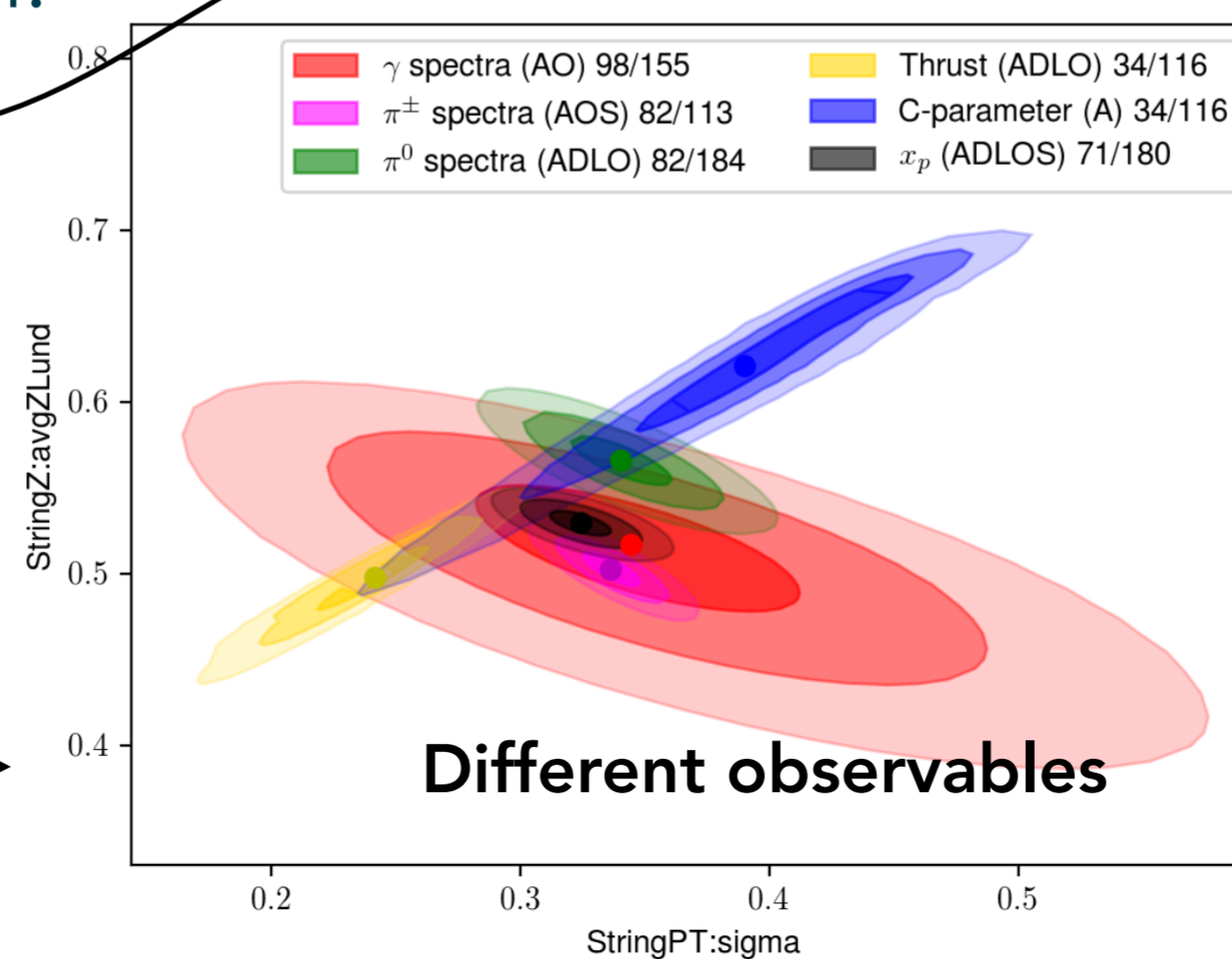
Simple sanity limit / overfit protection / tension resolution:

Add blanket 5% baseline uncertainty

(+ exclude superseded measurements)

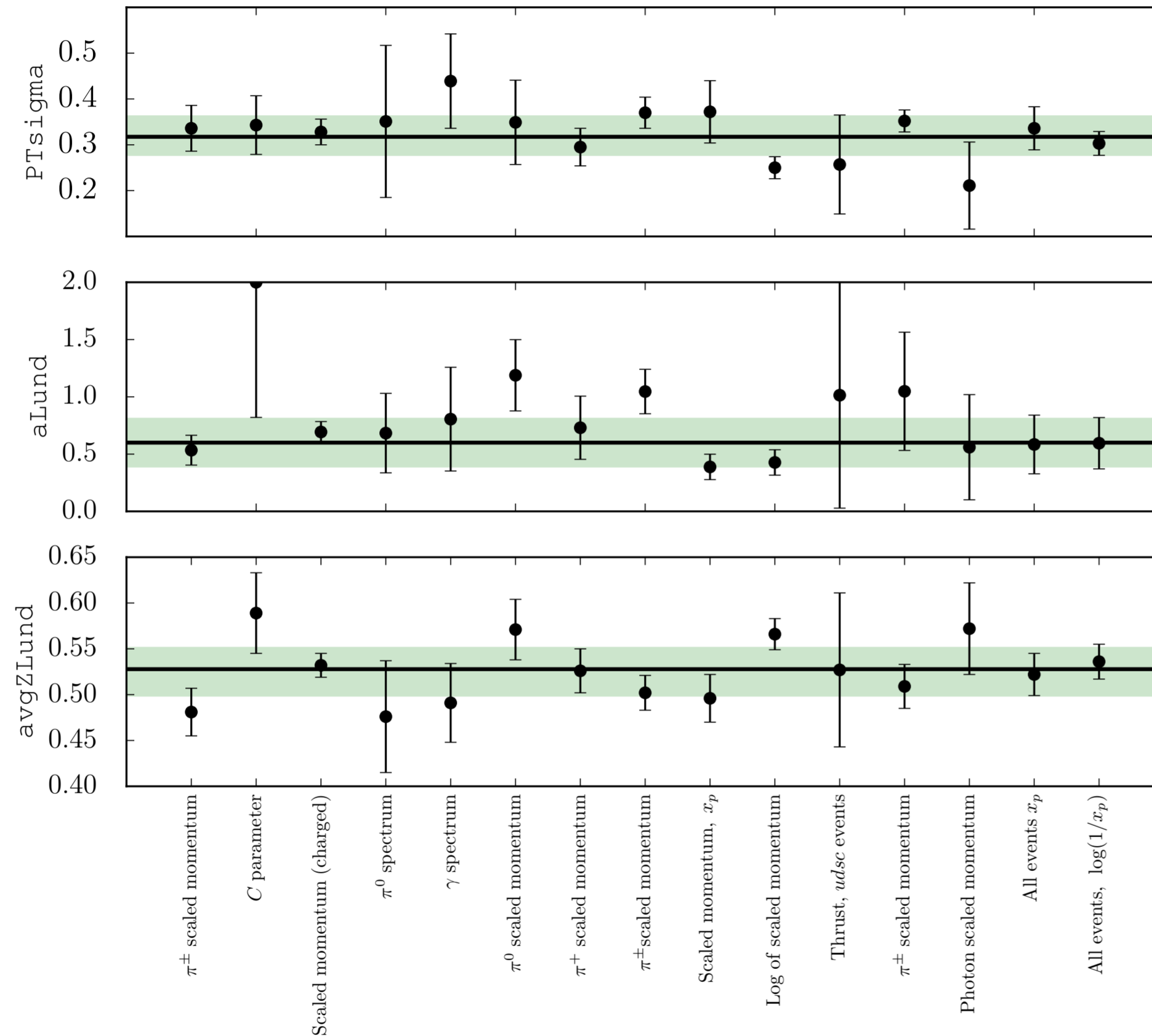
## + Universality Tests: →

Parameter	without 5%	with 5%
StringPT:Sigma	$0.3151^{+0.0010}_{-0.00010}$	$0.3227^{+0.0028}_{-0.0028}$
StringZ:aLund	$1.028^{+0.031}_{-0.031}$	$0.976^{+0.054}_{-0.052}$
StringZ:avgZLund	$0.5534^{+0.0010}_{-0.0010}$	$0.5496^{+0.0026}_{-0.0026}$
$\chi^2/\text{ndf}$	5169/963	778/963



# Practical Example: Uncertainties on Dark-Matter Annihilation Spectra

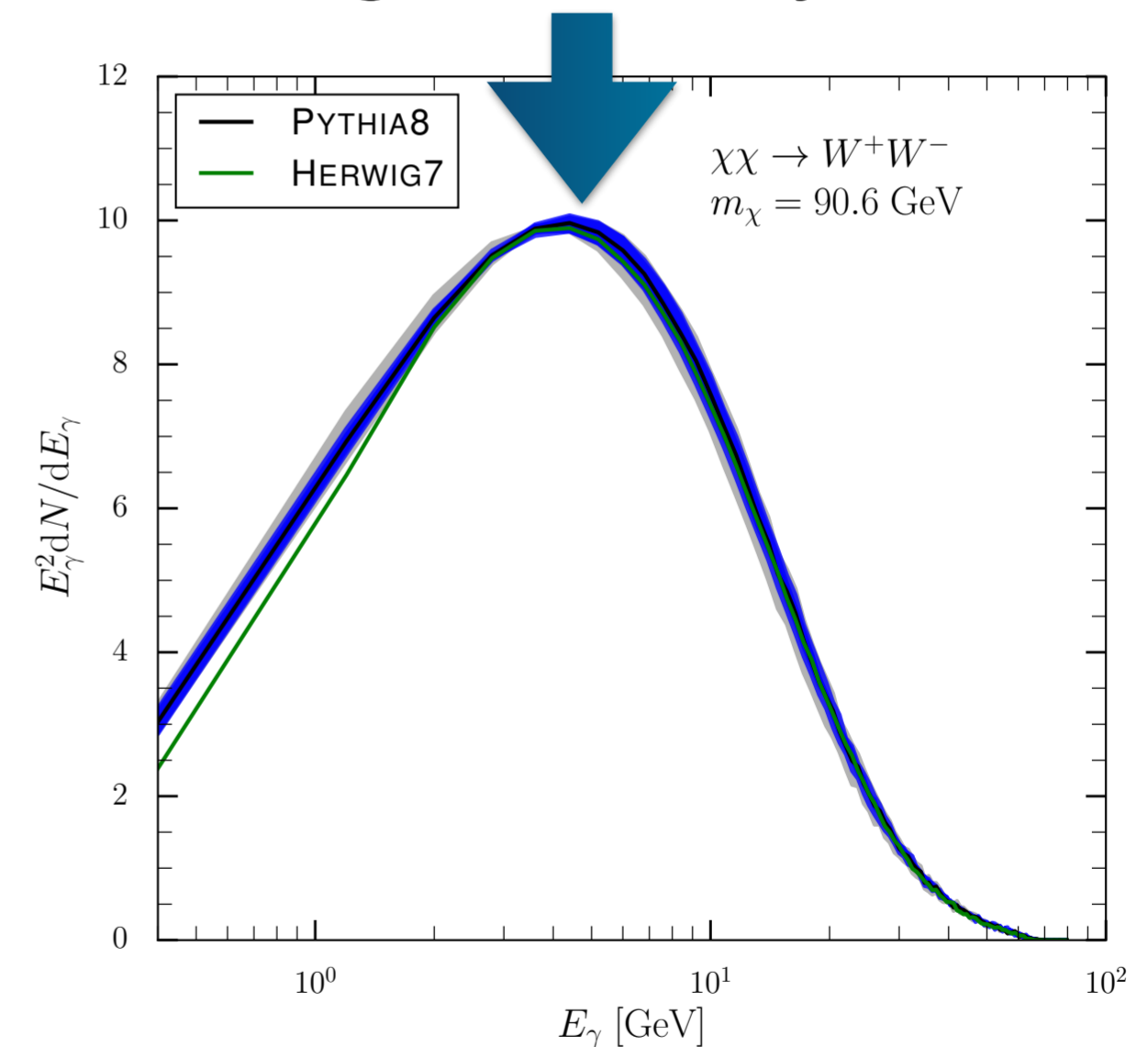
Based on A. Jueid et al., [1812.07424](#) (gamma rays, eg for GCE) and [2202.11546](#) (antiprotons, eg for AMS) + [2303.11363](#) (all)



**Weighted Average:** good consistency across observables

Expensive?

**10-point variations**  $\blacktriangleright$  **Fairly convincing** uncertainty bands?



**Same done for antiprotons, positrons, antineutrinos**

Main Contact: [adil.jueid@gmail.com](mailto:adil.jueid@gmail.com)

Tables with uncertainties available on request. Also the spanning tune parameters of course.

# New: Automated Hadronization Uncertainties

## Problem:

Given a colour-singlet system that (randomly) broke up into a specific set of hadrons:



What is the **relative probability** that same system would have resulted, if the fragmentation parameters had been **different**?

Would this particular final state become **more likely** ( $w' > 1$ )? Or **less likely** ( $w' < 1$ )

Crucially: **maintaining unitarity**  $\implies$  inclusive cross section remains unchanged!

**August 2023:** Bierlich, Ilten, Menzo, Mrenna, Szewc, Wilkinson, Youssef, Zupan

[*Reweighting MC Predictions & Automated Fragmentation Variations in Pythia 8*, [2308.13459](https://arxiv.org/abs/2308.13459)]

**Method is general;** demonstrated on variations of the 7 main parameters governing longitudinal and transverse fragmentation functions in PYTHIA 8

<https://gitlab.com/uchep/mlhad-weights-validation>

# Examples with Pythia 8

[Reweighting MC Predictions & Automated Fragmentation Variations in Pythia 8, [2308.13459](#)]

## Longitudinal Fragmentation Function (Lund Symmetric FF)



$f(z) \sim$  scaled light-cone hadron momentum fraction

$$\propto \frac{1}{z^{1+r_Q} b m_Q^2} (1-z)^a \exp\left(-\frac{b m_{\perp}^2}{z}\right)$$

variations  $\rightarrow$

### Reweighting Methodology:

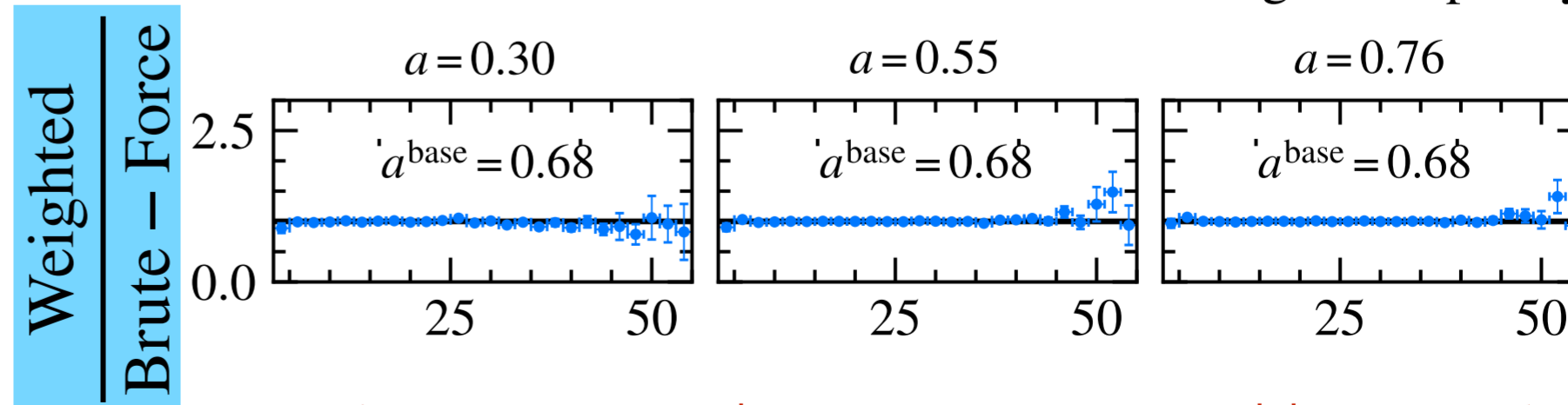
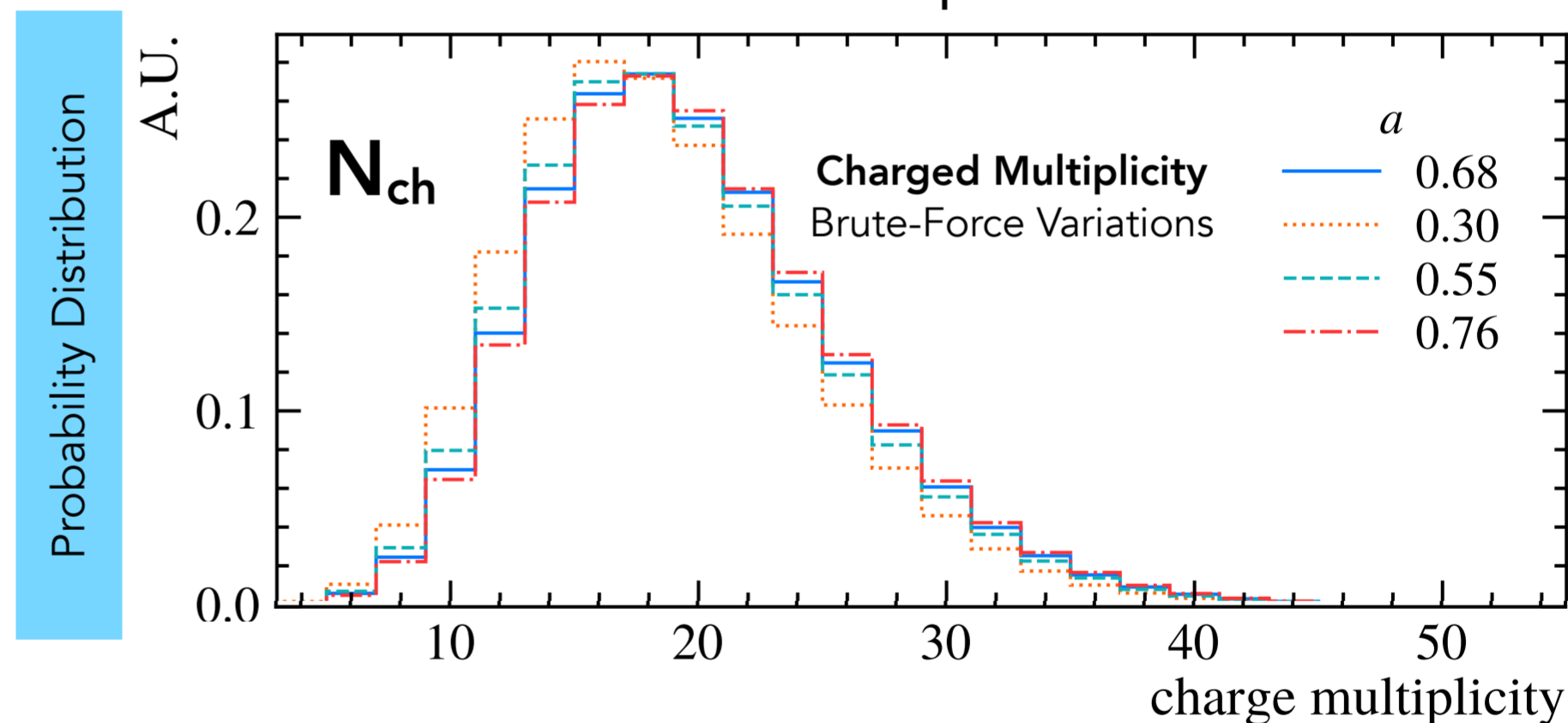
Accept-Reject Algorithm (analogous to shower variations):

$$w' = w \prod_{i \in \text{accepted}} R'_{i,\text{accept}}(z) \prod_{j \in \text{rejected}} R'_{j,\text{reject}}(z),$$

with

$$R'_{\text{accept}}(z) = \frac{P'_{\text{accept}}(z)}{P_{\text{accept}}(z)} \quad R'_{\text{reject}}(z) = \frac{P'_{\text{reject}}(z)}{P_{\text{reject}}(z)} = \frac{1 - P'_{\text{accept}}(z)}{1 - P_{\text{accept}}(z)}$$

### Example



(+ can vary 5 other parameters, in addition to  $a$ )

# From Data Analysis $\Rightarrow$ Validation of (current & future) MC Event Generators

## Experimental Measurement

## Data Preservation (for HEP): **HEPData**

(HEPData is funded by the UK STFC and is based at the IPPP at Durham U.)

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH (CERN)

**LHCb**

CERN-PH-EP-2010-027  
18 August 2010, rev. 15 September 2010

Prompt  $K_S^0$  production in  $pp$  collisions at  $\sqrt{s} = 0.9$  TeV

The LHCb Collaboration

Abstract

The production of  $K_S^0$  mesons in  $pp$  collisions at a centre-of-mass energy of 0.9 TeV is

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HEPData

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Prompt  $K_{\text{short}}$  production in  $pp$  collisions at  $\sqrt{s}=0.9$  TeV

The LHCb collaboration

Aaij, R , Abellan Beteta, C , Adeva, B , Adinolfi, M , Adrover, C , Affolder, A , Agari, M , Ajaltouni, Z , Albrecht, J , Alessio, F

Phys.Lett.B 693 (2010) 69-80, 2010.

<https://doi.org/10.17182/hepdata.55676>

Journal INSPIRE Resources

Rivet Analysis

Abstract (data abstract)

CERN-LHC. Measurement of the differential cross section  $D2\text{SIG}/DPT$

RE	P P --> K0S X		
SQRT(S)	900.0 GeV		
YRAP(P=3)	2.5-3.0	3.0-3.5	3.5-4.0
PT(P=3) [GEV]	SIG [MUB]		
	0.0 - 0.2	0.2 - 0.4	0.4 - 0.6
	294.0 $\pm 80.0$ stat $\pm 38.0$ sys_1 $\pm 90.0$ sys_2	316.0 $\pm 43.0$ stat $\pm 44.0$ sys_1 $\pm 72.0$ sys_2	196.0 $\pm 39.0$ stat $\pm 39.0$ sys_1 $\pm 38.0$ sys_2
	649.0 $\pm 133.0$ stat $\pm 136.0$ sys_1	562.0 $\pm 42.0$ stat $\pm 22.0$ sys_1	571.0 $\pm 42.0$ stat $\pm 25.0$ sys_1

Visualize

How to compare (unambiguously and exactly) to event generators? (e.g., to validate future ones)

Need **Analysis Preservation** too

Authors prepare & submit **code** to:

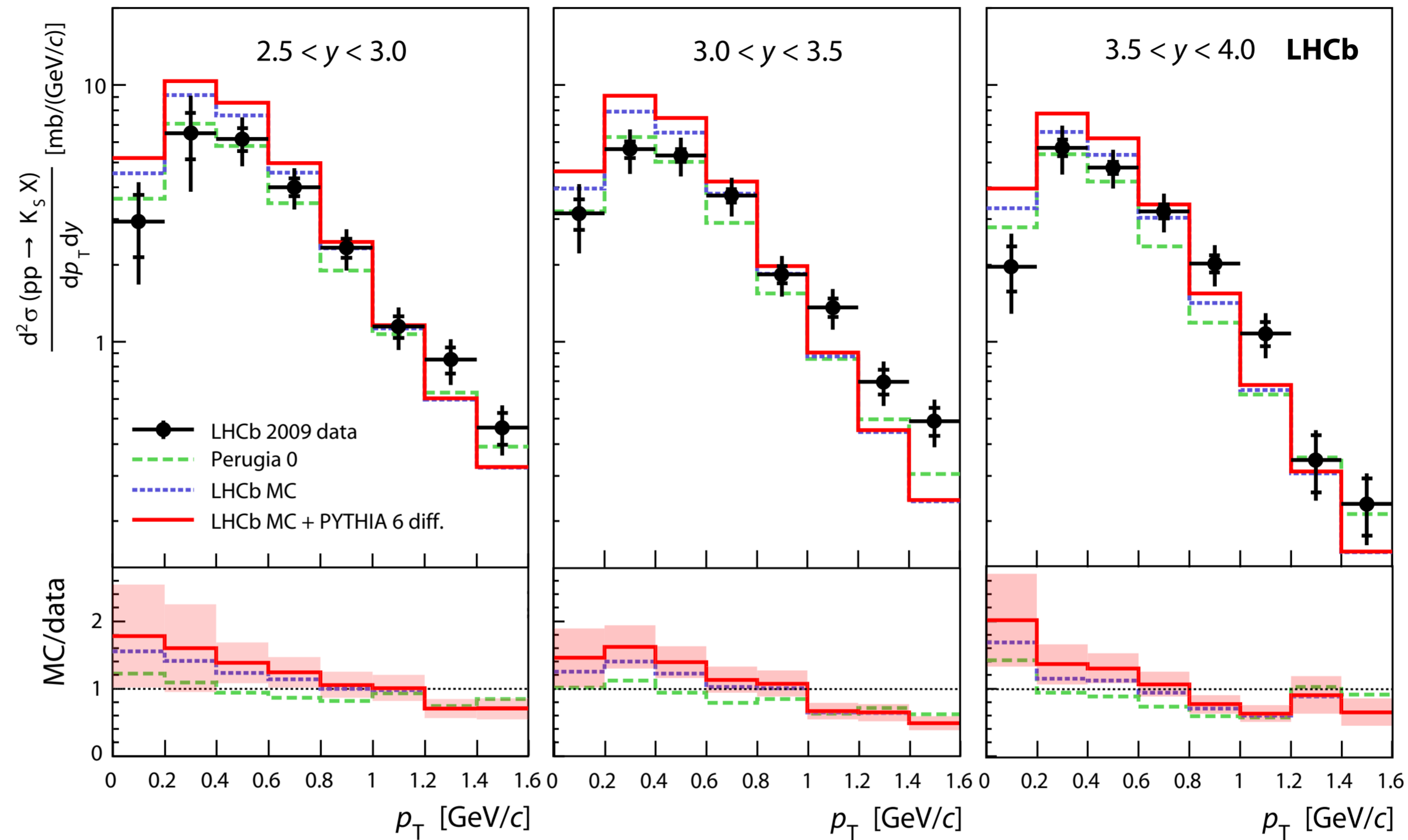
## Analysis Preservation (for HEP): **Rivet**

(Rivet is developed by the CEDAR project, also based in the UK)



# When showing plots from the original paper:

Example:  
Some kaon spectra  
compared to MCs



“Yes but this has been corrected in version X of that generator”

“But this other tune or MC that you didn’t compare to does better”

“Does the model shown there also describe correctly this **other** important observable?”

...

Instant answers would be convenient for faster & better informed discussions!

## **2010: LHC@home developers approached the CERN Theory Group**

Could we propose a simple test application for embedding physics applications in a Virtual Machine (CernVM) for running on the LHC@home volunteer cloud?

## **PYTHIA: simple to build (no external libs), small footprint, ...**

Would not previously have been able to run on a volunteer-cloud environment:

No native Windows support, nor much interest (or manpower) to develop that  
Small group of physicists; main (only) goal (& grant funding) = physics research

## **Virtualisation factorised the problem:**

Physics application just saw a (configurable) standard Linux environment (now CentOS)

## **Became the Test4Theory project, the world's first virtual volunteer cloud**

Run event generators → RIVET and display results at [mcplots.cern.ch](http://mcplots.cern.ch)



Preview at [mcplots-dev.cern.ch](https://mcplots-dev.cern.ch)

# MC PLOTS

Online repository of Monte Carlo plots compared to experimental data

**113**

data analyses

**126**

generators

**783667**

plots





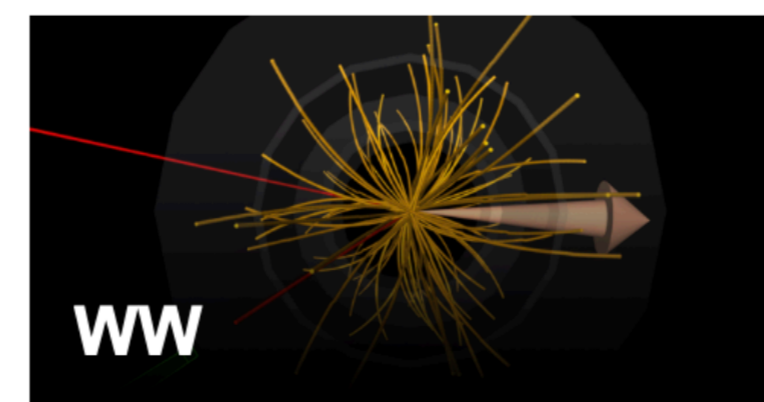
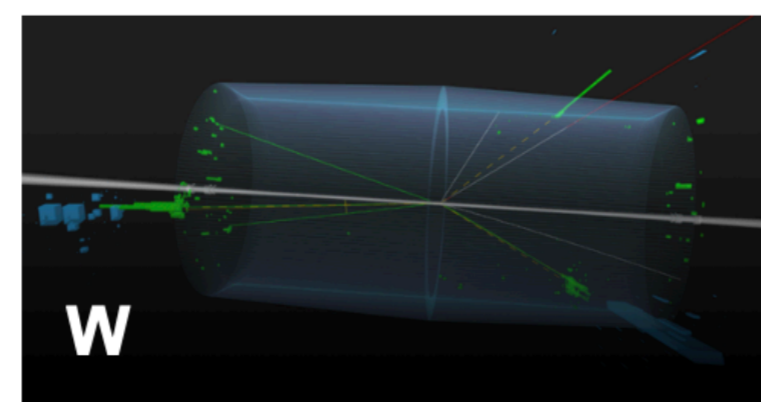
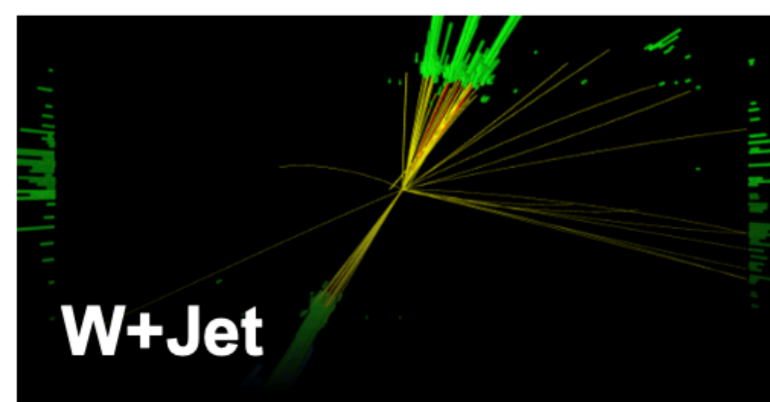
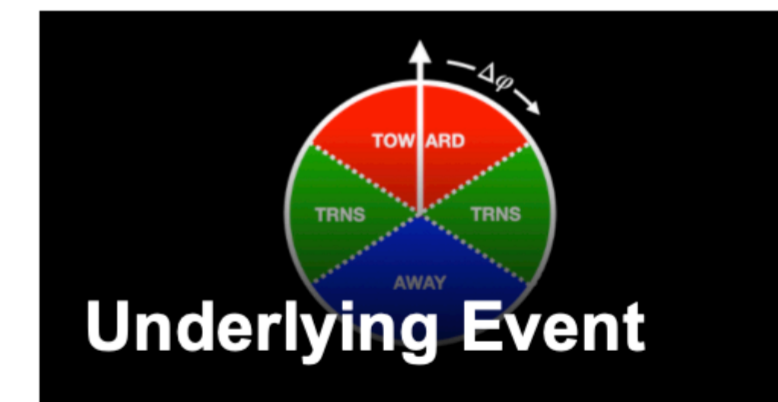
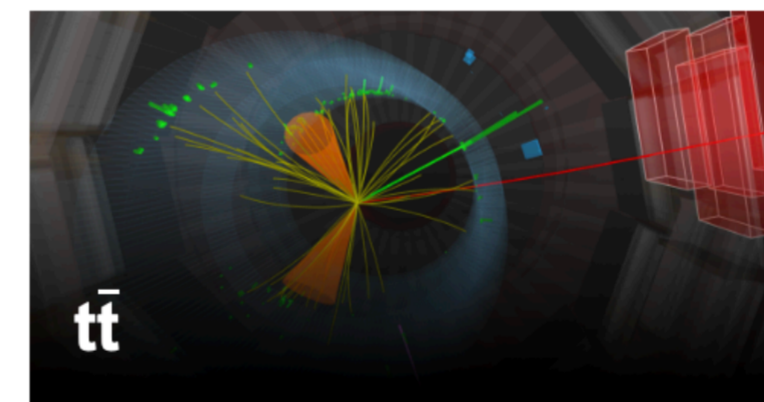
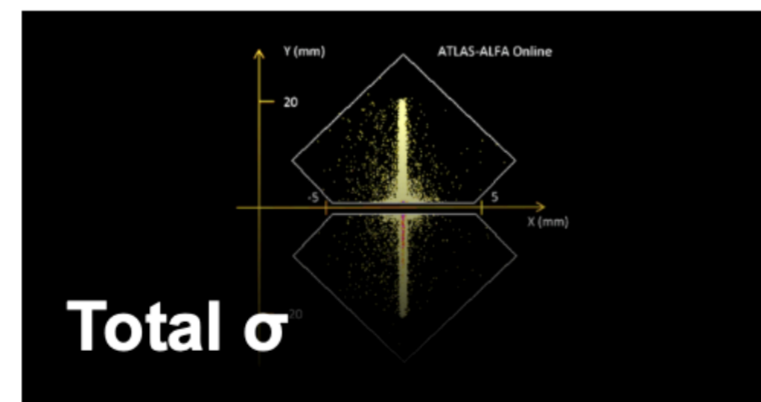
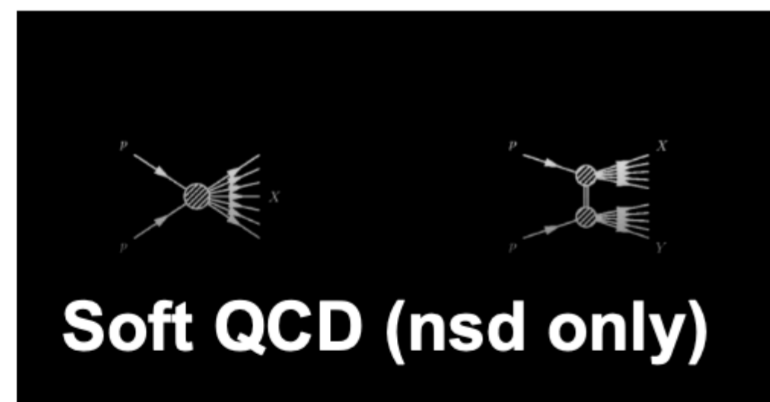
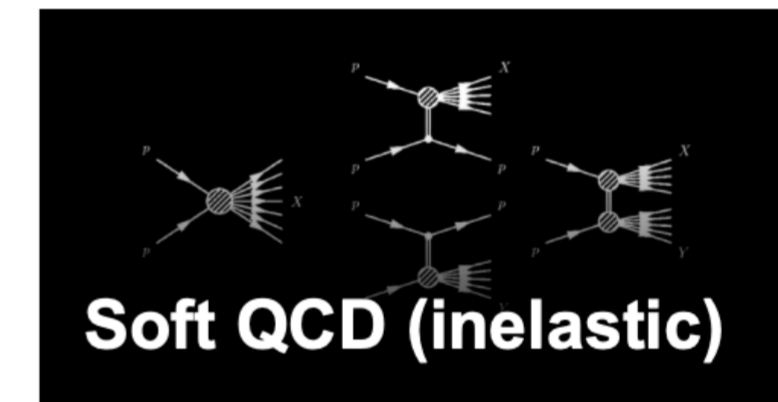
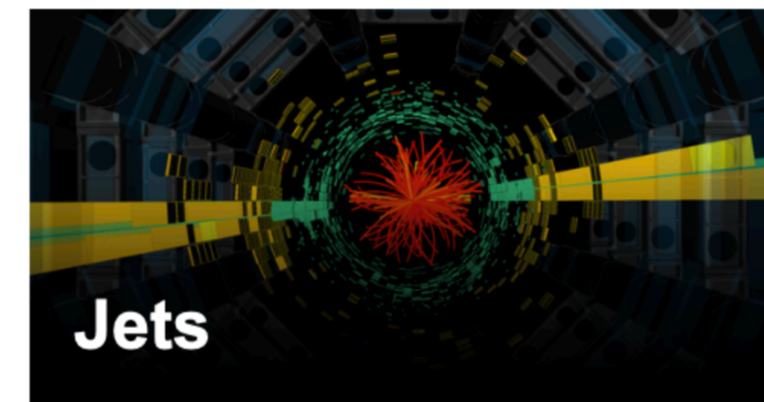
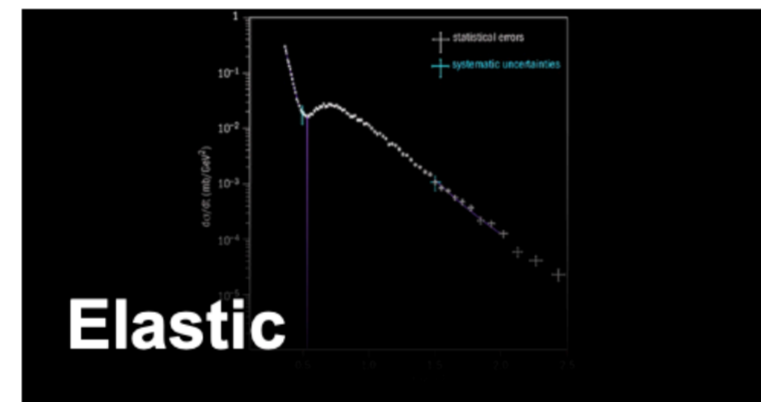
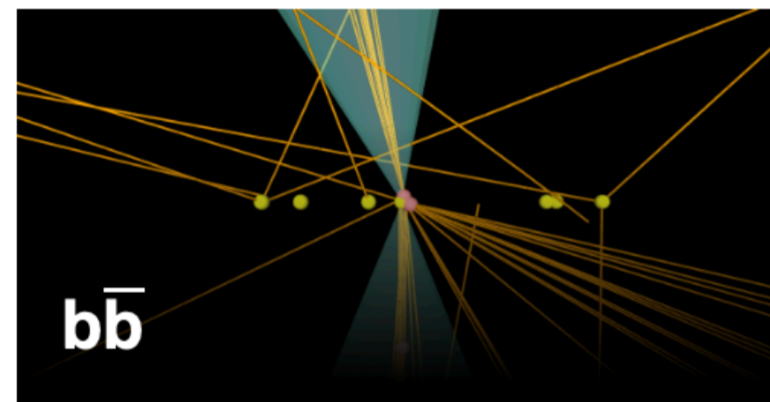
## Plots by analyses

Preview at [mcplots-dev.cern.ch](http://mcplots-dev.cern.ch)

Choose an analysis ▾



## Plots by beams : pp





## Plots by analyses

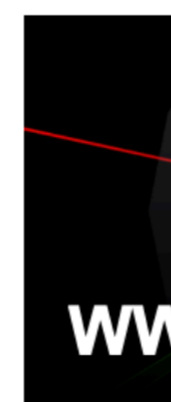
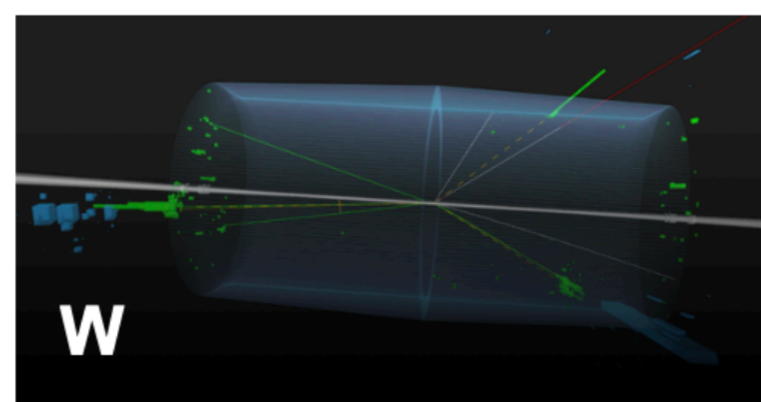
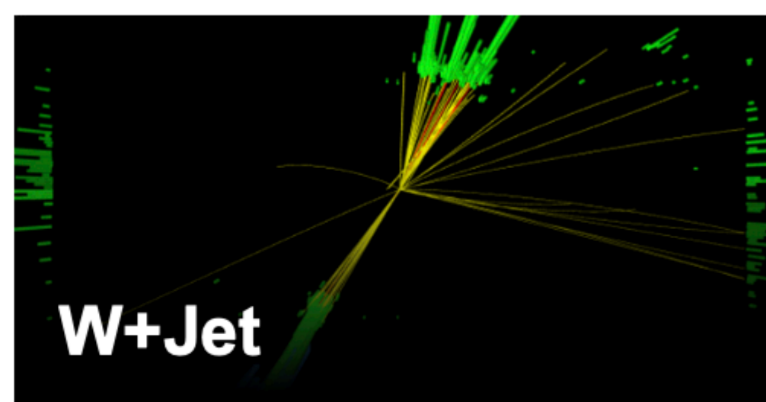
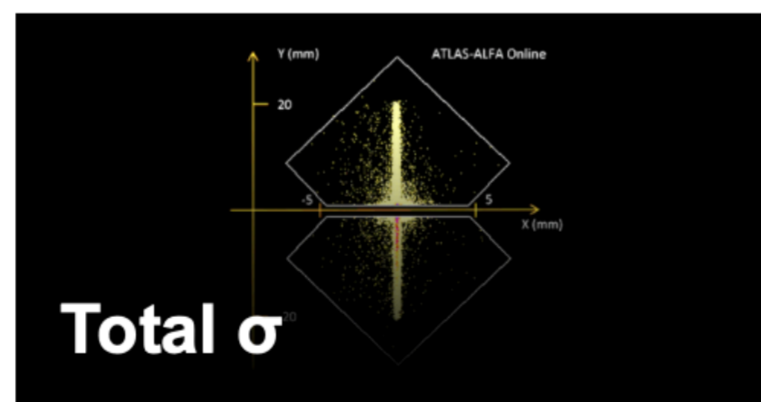
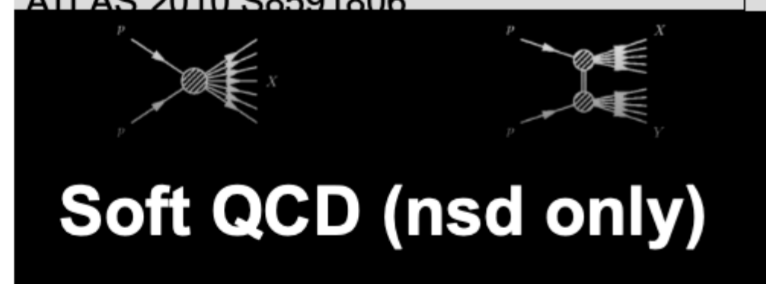
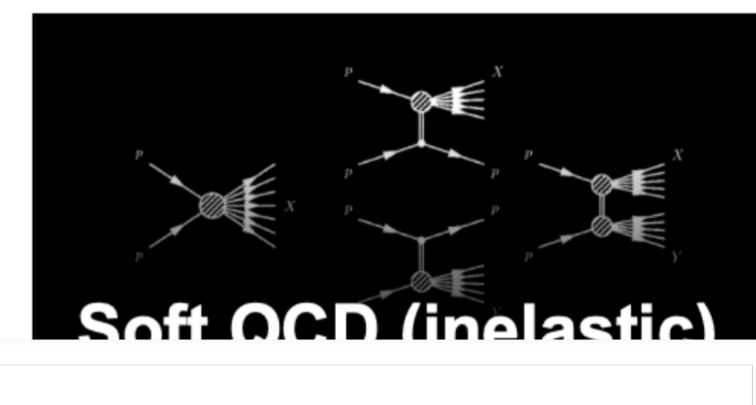
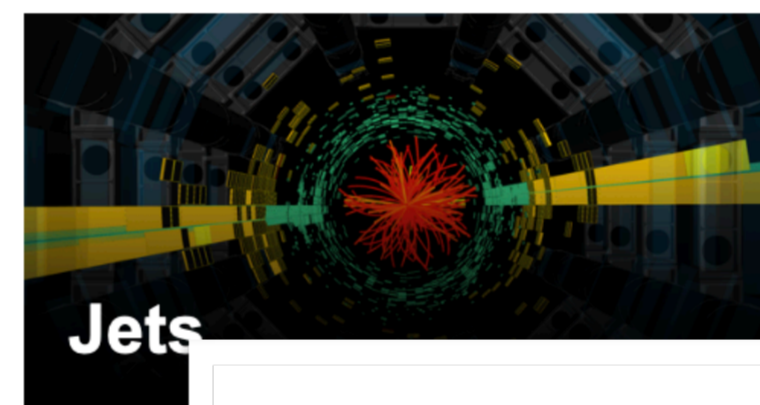
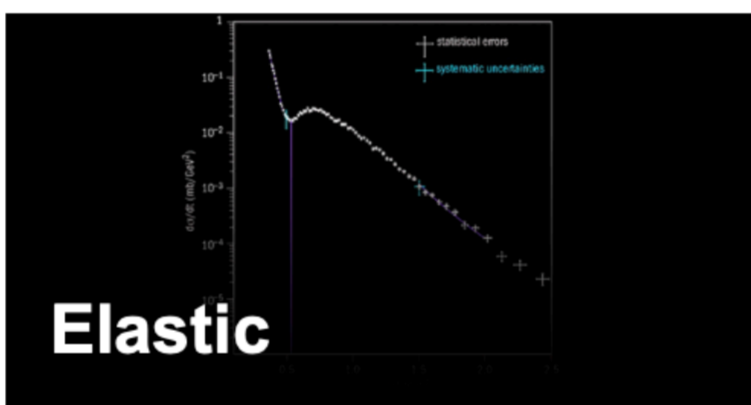
Preview at [mcplots-dev.cern.ch](http://mcplots-dev.cern.ch)

Choose an analysis ▾

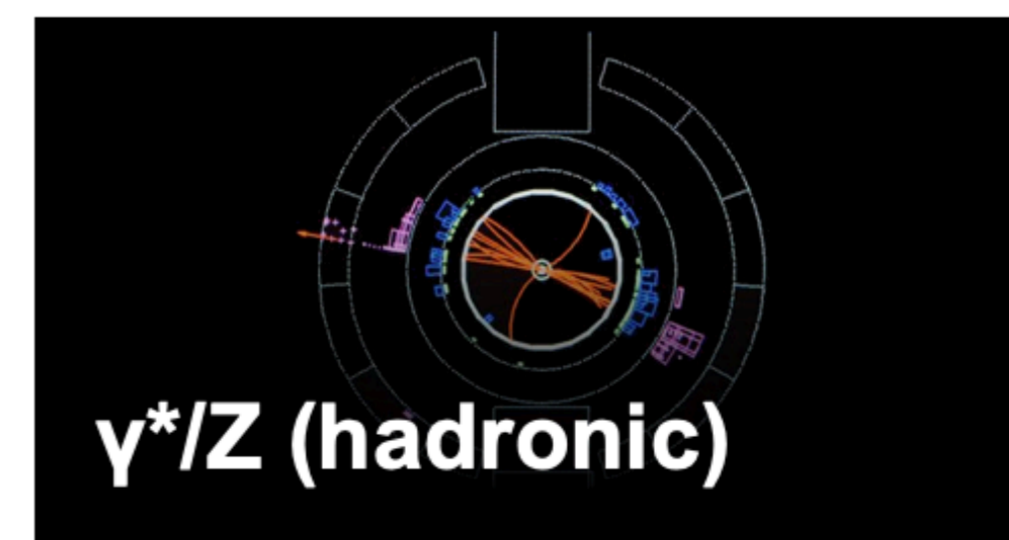
- ALEPH 1996 S3486095
- ALEPH 1999 S4193598
- ALEPH 2004 S5765862
- ALICE 2010 S8624100
- ALICE 2010 S8625980
- ALICE 2010 S8706239
- ALICE 2011 S8909580
- ALICE 2011 S8945144
- ALICE 2012 I1116147
- ALICE 2012 I1181770
- ALICE 2014 I1300380
- ALICE 2015 I1357424
- ATLAS 2010 CONF 2010 049
- ATLAS 2010 S8591806

Select individual RIVET analysis

Or process category



## Plots by beams : ee



# MC PLOTS — New Look Coming Soon

Work in Progress: A. Korneeva, A. Karneyeu, PS



ABOUT

HOME

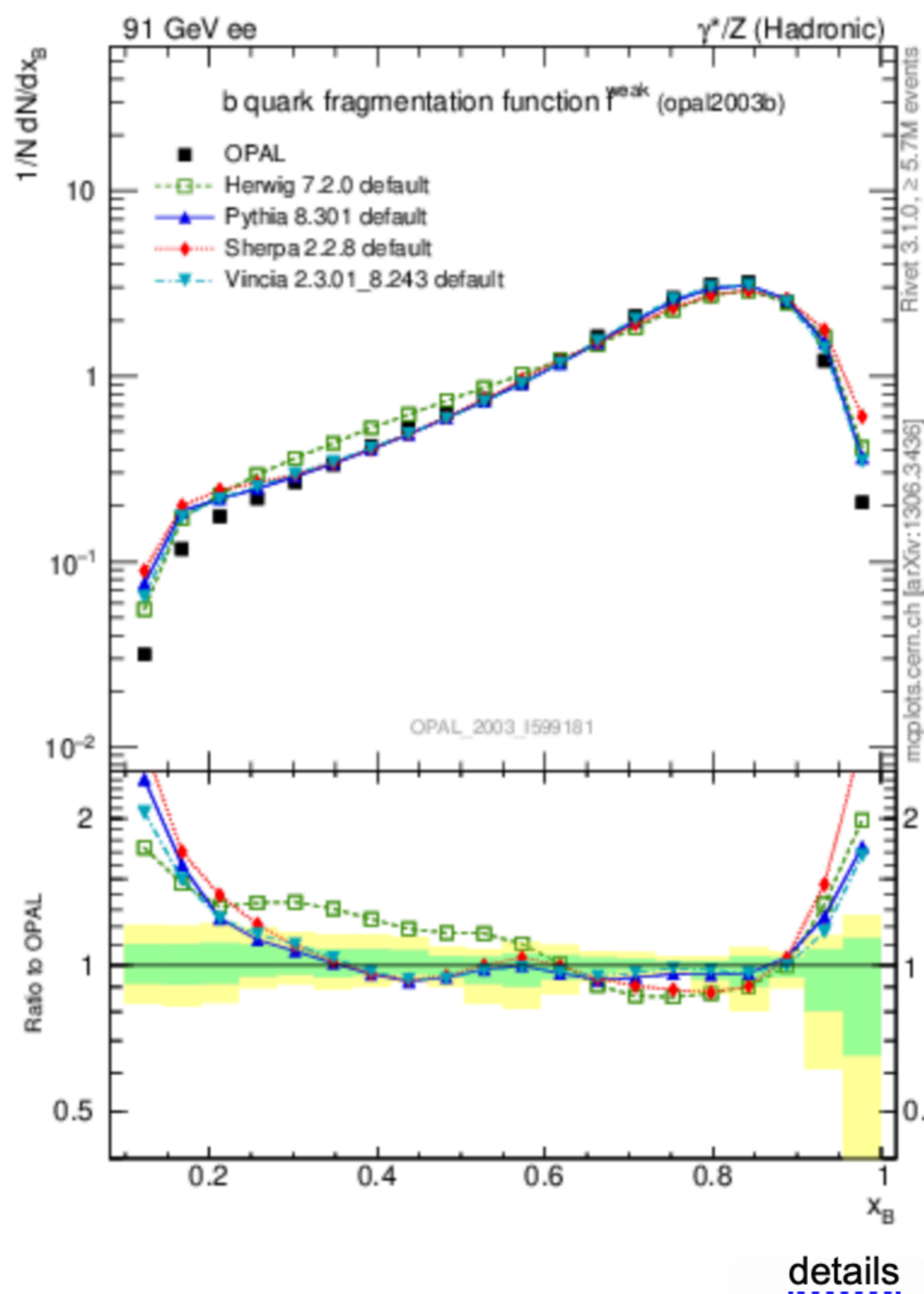
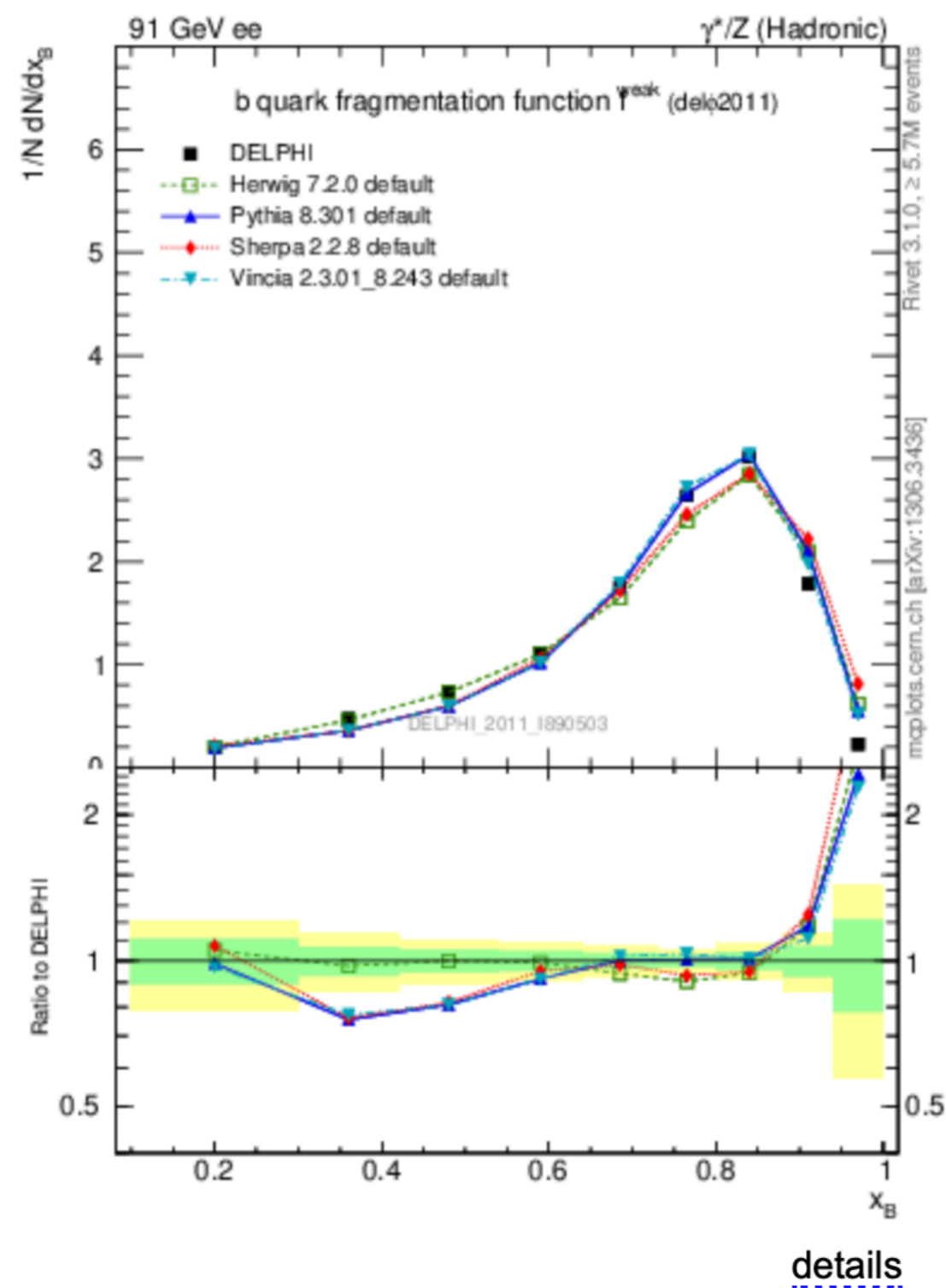
ee @ 91 GeV

General-Purpose MCs : Main ▾

Customize

Select between all available MC generators & versions

- ΔB(Max-Min)
- C parameter
- D parameter
- EEC
- EEC Asymmetry
- M(Heavy Hemisph)
- M(Light Hemisph)
- ΔM(Heavy-Light)
- Planarity
- Sphericity
- Thrust
- 1-Thrust
- Thrust Major
- Thrust Minor
- Thrust Oblateness
- Charm and Bottom ▾
- $f_{\text{weak}}$**
- Mean of  $f_{\text{weak}}$
- B multiplicity
- D multiplicity
- D\* multiplicity
- $\Lambda_b$  multiplicity
- D\* spectrum





ee @ 91 GeV

General-Purpose MCs : Main ▾

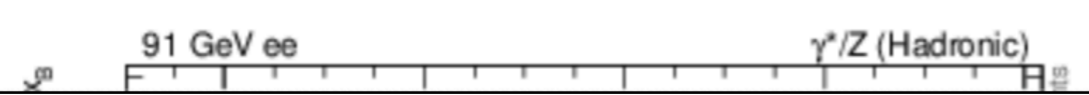
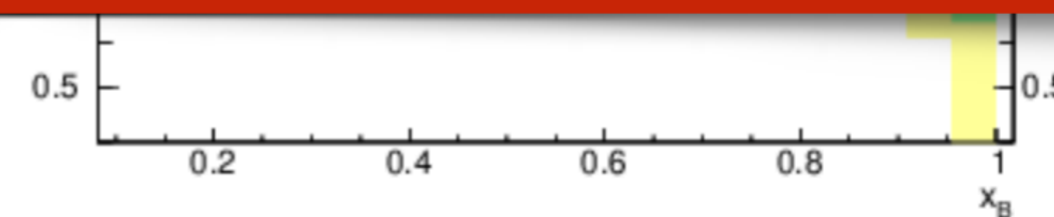
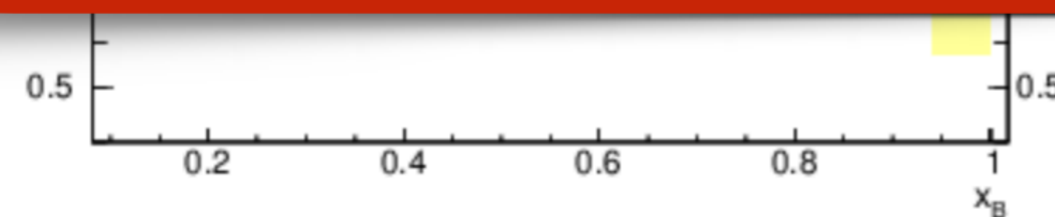
Customize

MC PLOTS = **Gitlab** repository

You can clone it, implement new analyses, etc.

Could be adapted with **suite of Belle II comparisons?**

**Main contact:** [natalia.korneeva@cern.ch](mailto:natalia.korneeva@cern.ch)



Download as: [.pdf](#) [.eps](#) [.png](#) [.script.tgz](#) #  
OPAL experiment: [data](#) | [article paper](#)  
Herwig 7 (Def): [data](#) | [generator card](#)  
Pythia 8 (Def): [data](#) | [generator card](#)  
Sherpa (Def): [data](#) | [generator card](#)  
Vincia (Def): [data](#) | [generator card](#)

Direct access to all generator cards, data points, MC points, journal paper, etc

- ΔB(Max-Min)
- C parameter
- D parameter
- EEC
- EEC Asymmetry
- M(Heavy Hemisph)
- M(Light Hemisph)
- ΔM(Heavy-Light)
- Planarity
- Sphericity
- Thrust
- 1-Thrust
- Thrust Major
- Thrust Minor
- Thrust Oblateness
- Charm and Bottom ▾
- f<sub>weak</sub>**
- Mean of f<sub>weak</sub>
- B multiplicity
- D multiplicity
- D\* multiplicity
- Λ<sub>b</sub> multiplicity
- D\* spectrum

Extra Slides



# Examples with Pythia 8

[Reweighting MC Predictions & Automated Fragmentation Variations in Pythia 8, [2308.13459](#)]

## Transverse Fragmentation Function (Gaussian)



$$\frac{1}{2\pi\sigma_{p_T}^2} \exp\left(-\frac{(\Delta p_x)^2 + (\Delta p_y)^2}{2\sigma_{p_T}^2}\right)$$

StringPT:sigma

variations

Example

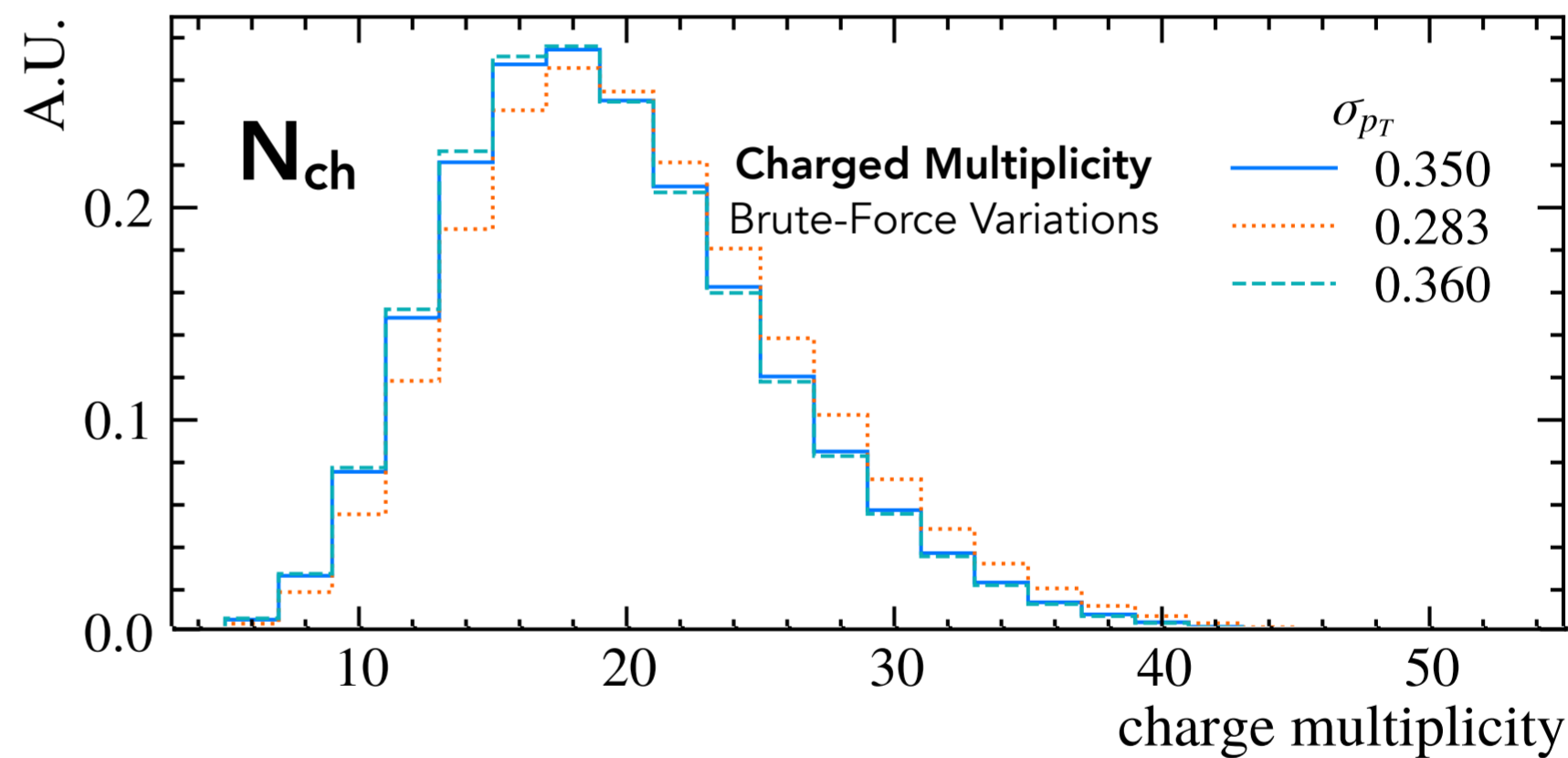
### Reweighting Methodology:

For each  $p_T$  (Box-Muller transform):

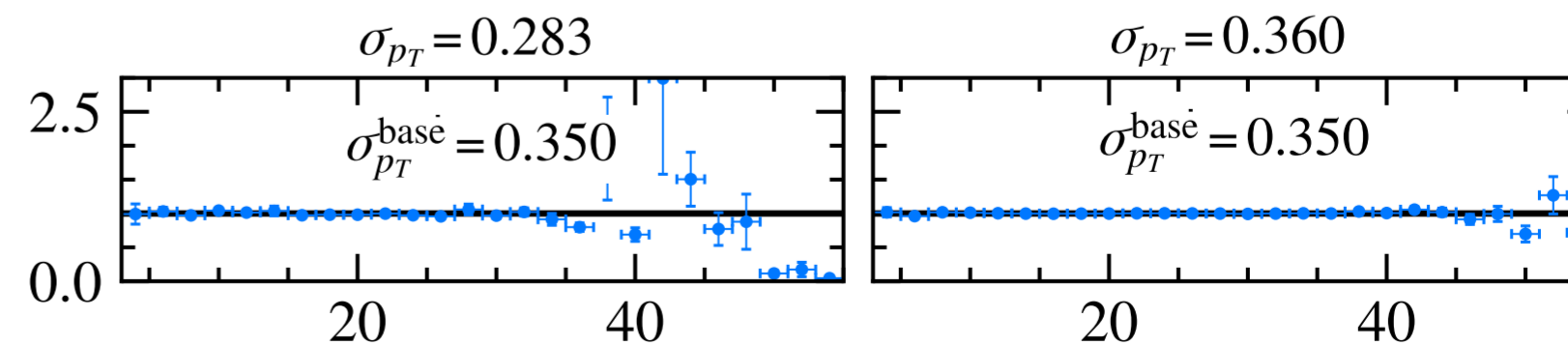
$$w' = \frac{\sigma^2}{\sigma'^2} \exp\left(-\kappa \left(\frac{\sigma^2}{\sigma'^2} - 1\right)\right)$$

$\kappa = (n_1^2 + n_2^2)/2$  and  $n_i$  are normally distributed random variates

Probability Distribution



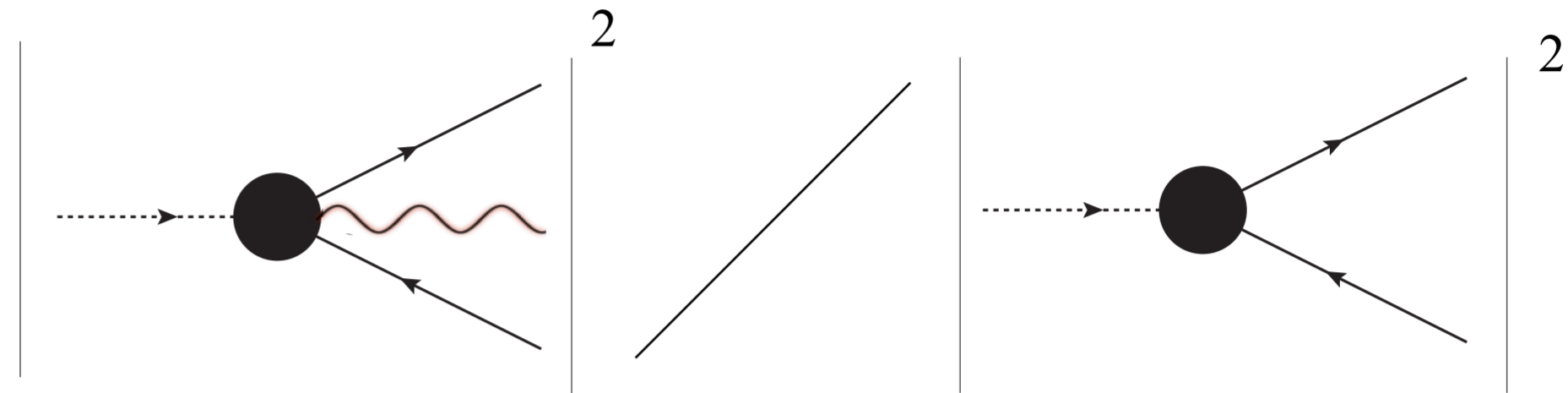
Weighted  
Brute - Force



# 1. Types of (QED) Showers

## Simple case:

neutral scalar  $\rightarrow$  2 charged fermions  
 = **A single QED dipole**



**LO QED**

$$\propto \frac{2s_{e^-e^+}}{s_{e^-}\gamma s_{\gamma e^+}} + \frac{1}{M_0^2} \left( \frac{s_{\gamma e^+}}{s_{e^-}\gamma} + \frac{s_{e^-}\gamma}{s_{\gamma e^+}} + 2 \right)$$

eikonal term                      collinear terms

PYTHIA

**DGLAP**

$e^-$ -collinear limit

$e^+$ -collinear limit

$$\frac{P_{e^- \rightarrow e^- \gamma}(z_1)}{s_{1\gamma}} + \frac{P_{e^+ \rightarrow e^+ \gamma}(z_2)}{s_{2\gamma}}$$

VINCIA

**Antenna**

All Singular Terms

$$\frac{2s_{e^-e^+}}{s_{e^-}\gamma s_{\gamma e^+}} + \frac{1}{M_0^2} \left( \frac{s_{\gamma e^+}}{s_{e^-}\gamma} + \frac{s_{e^-}\gamma}{s_{\gamma e^+}} \right)$$

Soft limit

HERWIG, SHERPA, PHOTOS

**YFS**

$$\frac{2s_{e^-e^+}}{s_{e^-}\gamma s_{\gamma e^+}}$$

**Note:** this is (intentionally) oversimplified. Many subtleties (recoil strategies, gluon parents, initial-state partons, and mass terms) not shown.

# Beyond 2-body Systems: QED Multipoles

## PYTHIA QED

Determines a “best” set of dipoles. No genuine multipole effects.

I.e., interference beyond dipole level only treated via “principle of maximal screening”

Works as a parton shower evolution (+ MECs) ► interleaved with QCD, MPI, ...

## YFS QED [Yennie-Frautschi-Suura, 1961 ► several modern implementations]

Allows to take full (multipole) soft interference effects into account

“Scalar QED”; no spin dependence.

I.e., starts from purely soft approximation; collinear terms not automatic

Is not a shower; works as pure afterburner, adding a number of photons to a final state with predetermined kinematics; no interleaving

## VINCIA QED [Kleiss-Verheyen, 2017 ► Brooks-Verheyen-PS, 2020]

Allows to take full (multipole) soft interference effects into account

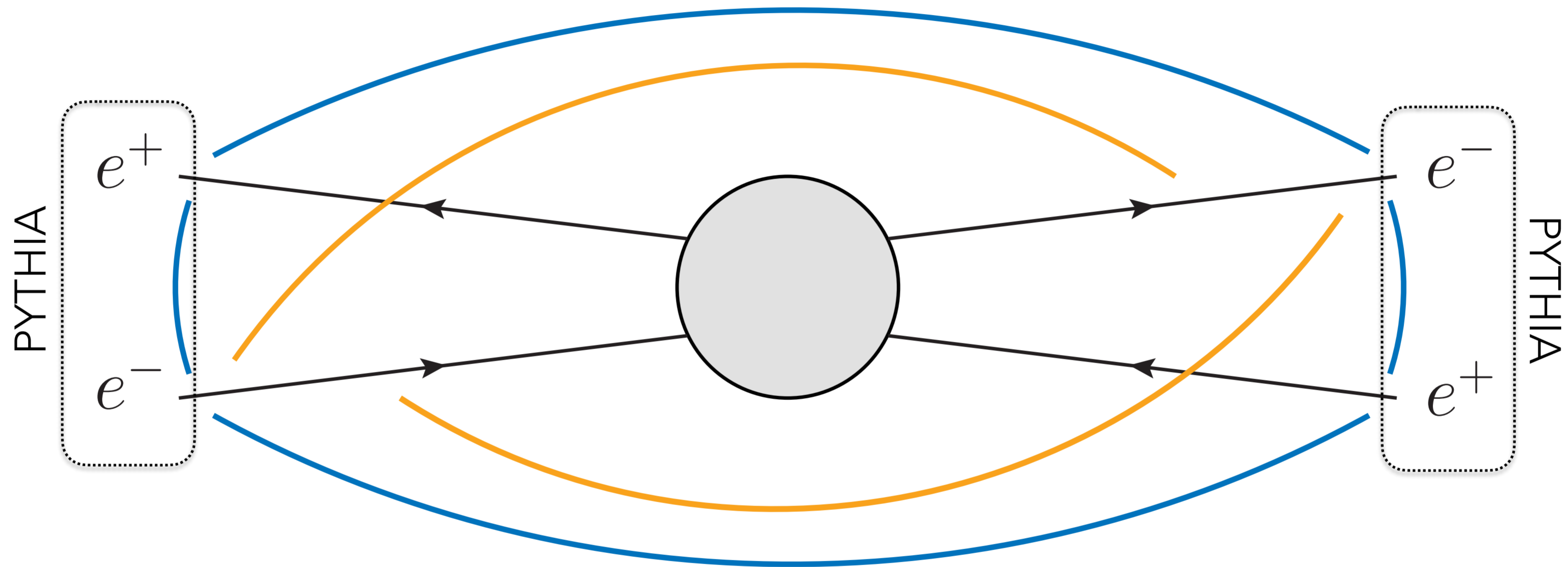
Not limited to scalar QED; includes spin dependence

I.e., starts from antenna approximation; including collinear terms

Works as a parton shower evolution; can be interleaved (+ MECs).

# What's the problem?

**Example: Quadrupole final state (4-fermion:  $e^+e^+e^-e^-$ )**

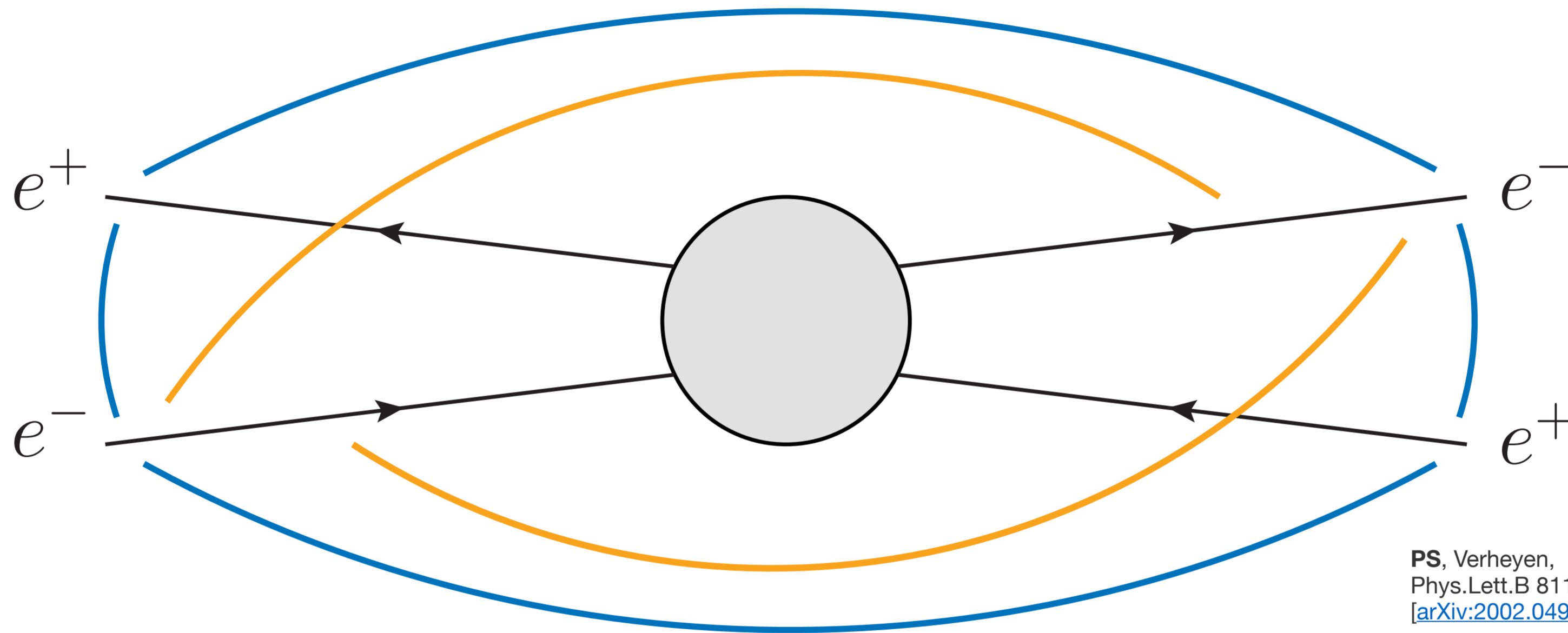


**Why was this not done as a shower before?**

The orange terms are negative ➤ negative weights (+ big cancellations)  
YFS gets around that by not being formulated as a shower (& no spin dependence)  
Utilises that the sum is always non-negative.

# What does VINCIA do differently?

Example: Quadrupole final state (4-fermion:  $e^+e^+e^-e^-$ )



PS, Verheyen,  
Phys.Lett.B 811 (2020) 135878  
[\[arXiv:2002.04939\]](https://arxiv.org/abs/2002.04939)

**Sectorize phase space:** for each possible photon emission kinematics  $p_\gamma$ , find the 2 charged particles with respect to which that photon is softest  $\blacktriangleright$  "Dipole Sector"

**Use dipole kinematics** for that sector, but sum **all** the positive and negative *antenna* terms (w spin dependence) to find the **coherent emission probability**.

# Further Details

## Antenna phase-space factorisation is exact, also for massive particles

+ Universal mass corrections are included in the eikonals

➤ Should have extremely faithful representation of “dead cone” effect (radiation from massive particles strongly damped for  $\theta_\gamma \lesssim E/m$ ) [Gehrmann-de Ridder, Ritzmann, PS, 2012]

Also automatically includes  $\gamma \rightarrow e^+e^-, \mu^+\mu^-, \dots$  splittings (not in PHOTOS? YFS?)

➤ First steps towards application of VINCIA QED to Hadron Decays

Honours project of Giacomo Morgante (Monash, 2023, in collaboration with Warwick)

+ Can incorporate Matrix-Element Corrections [Giele, Kosower, PS, 2011, + more recent]

**Not implemented yet.** Techniques known; worked out focusing on QCD

Will affect tails of hard radiation (process-dependent non-singular terms), so this is potentially an important still missing feature. Also: Form Factors, VMD contributions, BRs, ...

+ Can be interleaved with event evolution, e.g., with Resonance Decays