## Fractals, Strings, and Particle Collisions

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## Quantum Chromodynamics (QCD)

## The theory of quarks and gluons; the strong nuclear force

The elementary interactions are encoded in the Lagrangian EFT $\rightarrow$ Feynman Diagrams $\rightarrow$ Perturbative Expansions (in $\boldsymbol{\alpha}_{s}$ )

THE BASIC ELEMENTS OF RCD: QUARKS AND GLUONS

$$
g_{s}^{2}=4 \pi \alpha_{s}
$$

$$
\psi_{q}^{j}=\left(\begin{array}{l}
\psi_{1} \\
\psi_{2} \\
\psi_{3}
\end{array}\right)
$$



$$
\mathcal{L}=\bar{\psi}_{q}^{i}\left(i \gamma^{\mu}\right)\left(D_{\mu}\right)_{i j} \psi_{q}^{j}-m_{q} \bar{\psi}_{q}^{i} \psi_{q i}-\frac{1}{4} F_{\mu \nu}^{a} F^{a \mu \nu}
$$

$$
D_{\mu i j}=\delta_{i j} \partial_{\mu}-i g_{s} T_{i j}^{a} A_{\mu}^{a} \underset{\substack{m_{q}: \\ \text { (Figs + QCD Cork condensates) }}}{\substack{\text { Cluon-Field Kinetic Terms } \\ \text { and Sel-Itheractions }}}
$$

Gauge Covariant Derivative: makes $L$ invariant under $\mathrm{SU}(3)_{\mathrm{C}}$ rotations of $\Psi_{q}$

$$
F_{\mu \nu}^{a}=\partial_{\mu} A_{\nu}^{a}-\partial_{\nu} A_{\mu}^{a}+g_{s} f^{a b c} A_{\mu}^{b} A_{\nu}^{c}
$$

## More than just a (fixed-order perturbative) expansion in $\alpha_{\text {s }}$

## Two sources of fascinating multi-particle structures

Scale Invariance (apparent from the massless Lagrangian)
Confinement (win \$1,000,000 if you can prove)


Jets (the fractal of perturbative QCD) $\leftrightarrow$ amplitude structures in quantum field theory $\leftrightarrow$ factorisation \& unitarity. Precision jet (structure) studies.


Strings (strong gluon fields) $\leftrightarrow$ quantum-classical correspondence. String physics. String breaks. Dynamics of hadronization phase transition.


Hadrons $\leftrightarrow$ Spectroscopy (incl excited and exotic states), lattice QCD, (rare) decays, mixing, light nuclei. Hadron beams $\rightarrow$ multiparton interactions, diffraction, ...

## Ulterior Motives for Studying QCD

There are more things in heaven and earth, Horatio, than are dreamt of in your philosophy

$$
\text { Run } 2 \text { now underway ... }
$$

$$
\text { Almost twice the energy ( } 13 \mathrm{TeV} \text { vs } 8 \mathrm{TeV} \text { ) }
$$

Higher intensities ... (at least until last Friday)

LHC Run 1: still no explicit "new physics"
$\rightarrow$ we're still looking for deviations from SM
Accurate modelling of QCD improve searches \& precision

$$
\begin{aligned}
& \mathcal{L}=-\frac{1}{4} F_{\mu \nu} F^{\mu \nu} \\
& \frac{\overline{\mathrm{b}}}{\frac{0}{2}}+i \bar{\psi} \phi \psi+h . c \text {. } \\
& +\bar{\psi}_{i} y_{i j} \psi_{i} \phi+h . c . \\
& +\left.\phi_{r} \phi\right|^{2}-V(\phi)
\end{aligned}
$$

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\begin{aligned}
& \mathcal{L}=-\frac{1}{4} F_{\mu \nu} F^{\mu \nu} \\
& \frac{\bar{\circ}}{\frac{0}{\delta}}+i \bar{\psi} \phi \psi+h \cdot c \text {. } \\
& +\bar{\psi}_{i} y_{i j} \psi_{i} \phi+h . c . \\
& +\left.b_{r} \phi\right|^{2}-V(\phi)
\end{aligned}
$$



Large Hadron Collider: Weasel causes shutdown © 29 Apn 2016 Europe


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Accurate modelling of QCD improve searches \& precision

## ATLAS Li EXPERIMENT

Run Number: 162620, Event Number: 16060241



## QCD in the Ultraviolet

The "running" of $\alpha_{s}$ :

$$
Q^{2} \frac{\partial \alpha_{s}}{\partial Q^{2}}=-\alpha_{s}^{2}\left(b_{0}+b_{1} \alpha_{s}+b_{2} \alpha_{s}^{2}+\ldots\right)
$$



$$
b_{0}=\frac{11 C_{A}-2 n_{f}}{12 \pi} \quad C_{A}=3 \text { for } \mathrm{SU}(3)
$$

At high scales $\mathrm{Q} \gg 1 \mathrm{GeV}$
Coupling $\alpha_{s}(\mathrm{Q}) \ll 1$
Perturbation theory in $\alpha_{s}$ should be reliable: LO, NLO, NNLO, ...
E.g., in event shown on previous slide:

- 1st jet: $p_{T}=520 \mathrm{GeV}$
- 2nd jet: $p_{T}=460 \mathrm{GeV}$
- 3rd jet: $p_{T}=130 \mathrm{GeV}$
- 4th jet: $p_{T}=50 \mathrm{GeV}$


## The Infrared Strikes Back

## Naively, QCD radiation suppressed by $\alpha_{s} \approx 0.1$

Truncate at fixed order $=$ LO, NLO, $\ldots$
E.g., $\sigma(X+j e t) / \sigma(X) \propto \alpha_{s}$

Example: Pair production of SUSY particles at $\mathrm{LHC}_{14}$, with $\mathrm{Msusy} \approx 600 \mathrm{GeV}$

| LHC - |  | ehn, Rainwater, PS PLB645(2007)217 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FIXED ORDER PQCD | $\sigma_{\text {tot }}[\mathrm{pb}]$ | $\tilde{g} \tilde{g}$ | $\tilde{u}_{L} \tilde{g}$ | $\tilde{u}_{L} \tilde{u}_{L}^{*}$ | $\tilde{u}_{L} \tilde{u}_{L}$ | TT |
| $p_{T, j}>100 \mathrm{GeV}$ | oj | 4.83 | 5.65 | 0.286 | 0.502 | 1.30 |
| inclusive $\mathbf{X}+$ | $\rightarrow$ | 2.89 | 2.74 | 0.136 | 0.145 | 0.73 |
| inclusive $\mathrm{X}+2$ "jets" | $\rightarrow \sigma_{2 j}$ | 1.09 | 0.85 | 0.049 | 0.039 | 0.26 |
|  |  |  |  |  |  |  |
| $p_{T, j} \ngtr 50 \mathrm{GeV}$ | $\begin{aligned} & \sigma_{0 j} \\ & \sigma_{1 j} \end{aligned}$ | 4.83 | 5.65 | 0.286 | 0.502 | 1.30 |
|  |  | 5.90 | 5.37 | 0.283 | 0.285 | 1.50 |
|  | $\sigma_{2 j}$ | 4.17 | 3.18 | 0.179 | 0.117 | 1.21 |

```
\sigma for X + jets much larger than
    naive estimate
    \mp@subsup{\sigma}{50}{}~\mp@subsup{\sigma}{\mathrm{ tot tells us that there will }}{\mathrm{ "always" be a }~50-GeV jet }
```

(Computed with SUSY-MadGraph)

All the scales are high, $\mathrm{Q} \gg 1 \mathrm{GeV}$, so perturbation theory should be $\mathrm{OK} \ldots$

## Jets have fractal substructure

see PS, Introduction to QCD, TASI 2012, arXiv:1207.2389
Most bremsstrahlung is driven by divergent propagators
$\rightarrow$ simple structure

## Gauge amplitudes factorize

 in singular limits ( $\rightarrow$ universal "conformal" or "fractal" structure)

## Partons ab

$\rightarrow$ collinear:

$$
\begin{gathered}
\mathrm{P}(\mathrm{z})=\text { Altarelli-Parisi splitting kernels, with } \mathrm{z}=\mathrm{E}_{\mathrm{a}} /\left(\mathrm{E}_{\mathrm{a}}+\mathrm{E}_{\mathrm{b}}\right) \\
\left|\mathcal{M}_{F+1}(\ldots, a, b, \ldots)\right|^{2} \xrightarrow{a \| b} g_{s}^{2} \mathcal{C} \frac{P(z)}{2\left(p_{a} \cdot p_{b}\right)}\left|\mathcal{M}_{F}(\ldots, a+b, \ldots)\right|^{2}
\end{gathered}
$$

Gluon j
$\rightarrow$ soft:

$$
\left|\mathcal{M}_{F+1}(\ldots, i, j, k \ldots)\right|^{2} \xrightarrow{j_{g} \rightarrow 0} g_{s}^{2} \mathcal{C} \frac{\left(p_{i} \cdot p_{k}\right)}{\left(p_{i} \cdot p_{j}\right)\left(p_{j} \cdot p_{k}\right)}\left|\mathcal{M}_{F}(\ldots, i, k, \ldots)\right|^{2}
$$

+ scaling violation: $g_{s}{ }^{2} \rightarrow 4 \pi \alpha_{s}\left(\mathrm{Q}^{2}\right)$


## Jets have fractal substructure

Can apply this many times $\rightarrow$ nested factorizations $\rightarrow$ iteratively build up fractal structure


Can be cast as a differential evolution in the resolution scale, dProb/dQ ${ }^{2}$
It's a quantum fractal: P is probability to resolve another jet as we decrease the scale Eventually, it becomes more unlikely not to resolve a jet, than to resolve one
That's what the $\mathrm{X}+\mathrm{jet}$ cross sections were trying to tell us earlier: $\sigma(X+j e t)>\sigma(X)$

## Monte Carlo Event Generators: <br> Divide and Conquer

Factorization $\rightarrow$ Split the problem into many (nested) pieces

+ Quantum mechanics $\rightarrow$ Probabilities $\rightarrow$ Random Numbers

$$
\mathcal{P}_{\text {event }}=\mathcal{P}_{\text {hard }} \otimes \mathcal{P}_{\text {dec }} \otimes \mathcal{P}_{\mathrm{ISR}} \otimes \mathcal{P}_{\mathrm{FSR}} \otimes \mathcal{P}_{\mathrm{MPI}} \otimes \mathcal{P}_{\mathrm{Had}} \otimes \ldots
$$



Hard Process \& Decays:
Use process-specific (N)LO matrix elements
$\rightarrow$ Sets "hard" resolution scale for process: Qmax
ISR \& FSR (Initial \& Final-State Radiation):
Universal DGLAP equations $\rightarrow$ differential evolution, $d P / \mathrm{dQ}^{2}$, as function of resolution scale; run from Qmax to Qconfinement ~ 1 GeV (More later)
MPI (Multi-Parton Interactions)
Additional (soft) parton-parton interactions: LO matrix elements
$\rightarrow$ Additional (soft) "Underlying-Event" activity (Not the topic for today)
Hadronization
Non-perturbative model of color-singlet parton systems $\rightarrow$ hadrons

## This is just the physics of Bremsstrahlung



The harder they get kicked, the harder the
fluctations that continue to become strahlung
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## From Legs to Loops

## Unitarity: sum(probability) $=1$

Kinoshita-Lee-Nauenberg:
(sum over degenerate quantum states = finite: infinities must cancel!)

Neglect non-singular piece, $F \rightarrow$ "Leading-Logarithmic" (LL) Approximation
$\rightarrow$ Can also include loops-within-loops-within-loops ...
$\rightarrow$ Bootstrap for approximate All-Orders Quantum Corrections!

Parton Showers: reformulation of pQCD corrections as gain-loss diff eq.
Iterative (Markov-Chain) evolution algorithm, based on universality and unitarity
With evolution kernel $\sim \frac{\left|\mathcal{M}_{n+1}\right|^{2}}{\left|\mathcal{M}_{n}\right|^{2}}$ (or soff/collinear approx thereof)
Generate explicit fractal structure across all scales (via Monte Carlo Simulation)
Evolve in some measure of resolution $\sim$ hardness, virtuality, 1/time $\ldots \sim$ fractal scale

+ account for scaling violation via quark masses and $g_{s}{ }^{2} \rightarrow 4 \pi \alpha_{s}\left(Q^{2}\right)$


## Parton Showers are based on $1 \rightarrow 2$ splittings


E.g., PYTHIA (also HERWIG, SHERPA)
I.e., each parton undergoes a sequence of splittings

Dipole coherence effects can be included via "angular ordering" or via "dipole radiation functions" ( $\sim$ dipole partitioned into 2 monopole terms) Recoil effects needed to impose (E,p) conservation ("local" or "global")

At Monash, we develop an Antenna Shower, in which splittings are fundamentally $2 \rightarrow 3$ (+ working on $2 \rightarrow 4 \ldots$ )

Each colour dipole/antenna undergoes a sequence of splittings

+ Intrinsically includes dipole coherence (leading $\mathrm{N}_{\mathrm{C}}$ )
+ Lorentz invariance and explicit local (E,p) conservation
+ The non-perturbative limit of a colour dipole is a string piece Roots in Lund ~ mid-80ies: Gustafson \& Petterson, Nucl.Phys. B306 (1988) 746
What's new in our approach?
Higher-order perturbative effects can be introduced via calculable corrections in an elegant and very efficient way
+ Writing a genuine antenna shower also for the initial state evolution


## New: Hadron Collisions

Example taken from: Ritzmann, Kosower, PS, PLB718 (2013) 1345

## Example: quark-quark scattering in hadron collisions

Consider one specific phase-space point (eg scattering at $45^{\circ}$ )
2 possible colour flows: $a$ and $b$


Figure 4: Angular distribution of the first gluon emission in $q q \rightarrow q q$ scattering at $45^{\circ}$, for the two different color flows. The light (red) histogram shows the emission density for the forward flow, and the dark (blue) histogram shows the emission density for the backward flow.

[^0]
## VINCIA: Markovian pQCD*

*) pQCD : perturbative QCD


"Higher-Order Corrections To Timelike Jets" GeeKS: Giele, Kosower, Skands, PRD 84 (2011) 054003
"An Introduction to PYTHIA 8.2"
Sjöstrand et al., Comput.Phys.Commun. 191 (2015) 159

## Matrix-Element Corrections for ISR



## Matrix-Element Corrections for ISR

Work done by my PhD student Nadine Fischer (from whom I also stole these slides)

CMS, $\Delta \phi(\mathrm{Z}, \mathrm{JI}), \sqrt{s}=7 \mathrm{TeV}$
LHC: pp $\rightarrow$ Z + jet(s)


Angle between $Z$ and the hardest jet

## Matrix-Element Corrections for ISR



## Matrix-Element Corrections for ISR



## Matrix-Element Corrections for ISR



## Matrix-Element Corrections for ISR



## + Future Applications (why other people care)

## Example: The Top Quark

Heaviest known elementary particle:
$\mathrm{m}_{\mathrm{t}} \sim 187 u\left(\sim \mathrm{~m}_{\mathrm{Au}}\right)$
Lifetime: $10^{-24} \mathrm{~s}$
Complicated decay chains:

$$
\begin{gathered}
t \rightarrow b W^{+} \quad \bar{t} \rightarrow \bar{b} W^{-} \\
W \rightarrow\left\{q \bar{q}^{\prime}, \ell \nu\right\} \\
\text { quarks } \rightarrow \text { jets } \\
\text { b-quarks } \rightarrow \text { b-jets } \\
m_{t}^{2} \approx\left(p_{b}+p_{W^{+}}\right)^{2} \\
\approx\left(p_{b-\mathrm{jet}}+p_{q-\mathrm{jet}}+p_{\bar{q}-\mathrm{jet}}\right)^{2}
\end{gathered}
$$

Accurate jet energy calibrations $\rightarrow \mathrm{m}_{\mathrm{t}}$
Analogously for any process / measurement involving coloured partons


## Decays of coloured massive particles is the most important remaining step

## The Ultimate Limit: Wavelengths $>10^{-15} \mathrm{~m}$

## Quark-Antiquark Potential

As function of separation distance

~ Force required to lift a 16-ton truck

## String Breaks

## In QCD, strings can (and do) break!

(In superconductors, would require magnetic monopoles) In QCD, the roles of electric and magnetic are reversed Quarks (and antiquarks) are "chromoelectric monopoles" There are at least two possible analogies $\sim$ tunneling:

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(In superconductors, would require magnetic monopoles) In QCD, the roles of electric and magnetic are reversed Quarks (and antiquarks) are "chromoelectric monopoles" There are at least two possible analogies $\sim$ tunneling:


## The "Lund" String

- Quarks $\rightarrow$ String Endpoints
- Gluons $\rightarrow$ Transverse Excitations (kinks)

snapshots of string position
$\overline{\mathrm{q}}(\bar{b})$
strings stretched from q (or वव) endpoint via a number of gluons to $\bar{q}$ (or qq) endpoint

Gluon = kink on string, carrying energy and momentum


String Breaks
by Tunneling (Schwinger Type)


- Probability of string break constant per unit area $\rightarrow$ AREA LAW
- Breakup vertices causally disconnected $\rightarrow$ order is irrelevant $\rightarrow$ iterative algorithm


## Colour Confusion

## Between which partons do confining potentials arise?

$\mathrm{e}^{+} \mathrm{e}^{-}$: too easy
(still quite simple even after including bremsstrahlung etc.)

At $\mathrm{e}^{+} \mathrm{e}^{-}$colliders (eg LEP) : generally good agreement between measured particle spectra and models based on parton/antenna showers + strings
Basically a single 3-3bar system, very close to the original lattice studies motivating the string model.
(+ extensions to WW reasonable to $\sim \mathrm{O}\left(1 / \mathrm{N}_{\mathrm{c}}{ }^{2}\right)$ )
$\rightarrow$ re-use same models as input for LHC (universality) ?

Proton-Proton (LHC)
A lot more colour kicked around (\& also colour in initial state)

Include "Beam Remnants"
Still might look relatively simple, to begin with

(+baryon beam remnants $\rightarrow$ "string junctions")
String-fragmentation of junctions: Sjöstrand \& Skands Nucl.Phys. B659 (2003) 243

But no law against several parton-parton interactions


In fact, can easily be shown to happen frequently Included in all (modern) Monte Carlo models But how to make sense of the colour structure?

## Colour: What's the Problem?

(including MPI: Multiple Parton-Parton Interactions ~ the "underlying event")

## Without Colour Reconnections

Each MPI hadronizes independently of all others


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(including MPI: Multiple Parton-Parton Interactions ~ the "underlying event")

## Without Colour Reconnections

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## Colour Reconnections

(including MPI: Multiple Parton-Parton Interactions ~ the "underlying event")

With Colour Reconnections MPI hadronize collectively

See also Ortiz et al., Phys.Rev.Lett. 111 (2013) 4, 042001
Highly interesting theory questions now. Is there collective flow in pp? Or not?

If yes, what is its origin?
Is it stringy, or hydrodynamic? (or ...?)

Beam Direction

## String-Length Minimisation E.g., PYTHIA, HERWIG Or Thermal? E.g., EPOS

Or Higher String Tension?
E.g., DIPSY rope

## What are "Colour Reconnections"?

Simple example: $e^{+} e^{-} \rightarrow W^{+} W^{-} \rightarrow$ hadrons Intensely studied at LEP2.

CR implied a non-perturbative uncertainty on the W mass measurement, $\triangle \mathrm{MW} \sim 40 \mathrm{MeV}$
CR constrained to $\sim 10 \% \sim 1 / \mathrm{NC} 2$
Simple two-string system. What about pp?

## Several modelling attempts

Based on "just" minimising the string action


String interactions (Khoze, Sjostrand)
Generalized Area Law (Rathsman et al.)
Colour Annealing (Skands et al.)
Gluon Move Model (Sjostrand et al.)
More recently: $\mathrm{SU}(3)_{C}$ group multiplet weights
Dipole Swing (Lonnblad et al.)
String Formation Beyond Leading Colour (Skands et al.)


## What do we see?

## Plots from mcplots.cern.ch (powered by LHC@home)



## What do we see?

<pT> vs Number of Particles


<pT> vs Particle Mass


Average pT increases with particle multiplicity and (faster than predicted) with particle mass

## Fundamental Questions

(Reflections upon yesterday's curry dinner ...)

## Multiple Strings: String interactions?

Like Type I Superconductor?
Like Type II Superconductor? Something else?


Potential between two triplets:
antitriplet is attractive (diquarks); sextet is repulsive
We can treat anti-triplet via $C R \rightarrow$ junction-junction structure But we do nothing for the sextet


Figure 1. The ratios of the string tensions of flux tubes for various $\mathrm{SU}(3)$ representations, $d_{D}=\sigma_{D} / \sigma_{\mathbf{3}}$ for the GL parameters $\kappa=1,3$ and 9 (represented by crosses, each case connected by lines to guide the eye). The ratios of eigenvalues of the quadratic Casimir operators are shown as black bars. For comparison the lattice data of Ref. [2] are also plotted (diamonds with error bars). Boldface numbers and brackets $[p, q]$ denote the dimension and the Dynkin indices of each representation $D$, respectively

+ Newer results from Cardoso, Cardoso, Bicudo seem to support Casimir scaling (Type II): arXiv:1102.1542


## Quo Vadis?

## All sights are on Run 2 of the LHC

Next order of precision for jet rates and structure Aid precision measurements and enhance discovery reach Vast multi-jet phase spaces to explore with LHC Merging and MHV corrections (S. Prestel, A. Lifson, N. Fischer)


Beyond the Leading-Logarithmic approximation (with post doc Hai Tao Li)

+ systematic and automated theory uncertainties
Part of being precise is knowing how precise. Our job to give an answer.
Automated uncertainty bands in both VINCIA and PYTHIA 8 (Mrenna+Skands)


## Strings

Understand the physics of colour reconnections
What are the dynamics of multi-string environments?

Get this research going in Australia

Phenomenology: Modern revisions of the Lund string model
What measurements are crucial to shed more light?
Possible to get more information from lattice? Multi-string systems?

## New research at Monash



PRECISION LHC PHENOMENOLOGY PYTHIA \& VINCIA
NLO Event Generators
QCD STRINGS, HADRONISATION

## SUPPORT LHC EXPERIMENTS,

 ASTRO-PARTICLE COMMUNITY, AND FUTURE ACCELERATORS +OUTREACH AND Citizen Science+ Partnerships: Warwick Alliance, MCnet, CoEPP New joint research program with Warwick ATLAS, on developing and testing advanced colllider-QCD models. Opportunities for PhD students based at Monash + exchange to UK/CERN.

MCnet is an EU Marie Curie "Innovative Training Network" (ITN) on MC generators for LHC (Herwig, Pythia, Sherpa). Funded last week!



[^0]:    Note: coherence also influences the Tevatron top-quark forwardbackward asymmetry: see PS, Webber, Winter, JHEP 1207 (2012) 151

