Fractals, Strings, and Particle Collisions Peter Skands (Monash University)



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Quantum Chromodynamics (QCD)

THE THEORY OF QUARKS AND GLUONS; THE STRONG NUCLEAR FORCE

The **elementary** interactions are encoded in the **Lagrangian** QFT \rightarrow Feynman Diagrams \rightarrow Perturbative Expansions (in α_s)



$$\mathcal{L} = \bar{\psi}_{q}^{i} (i\gamma^{\mu}) (D_{\mu})_{ij} \psi_{q}^{j} - m_{q} \bar{\psi}_{q}^{i} \psi_{qi} - \frac{1}{4} F^{a}_{\mu\nu} F^{a\mu\nu}$$

$$D_{\mu ij} = \delta_{ij} \partial_{\mu} - ig_{s} T^{a}_{ij} A^{a}_{\mu} \quad {}^{\text{m}_{q}: \text{ Quark Mass Terms}}_{\text{(Higgs + QCD condensates)}} \qquad \text{Gluon-Field Kinetic Terms}$$

$$Gauge \text{ Covariant Derivative: makes } L_{\text{invariant under SU(3)}_{C} \text{ rotations of } \psi_{q}} \qquad F^{a}_{\mu\nu} = \partial_{\mu} A^{a}_{\nu} - \partial_{\nu} A^{a}_{\mu} + g_{s} f^{abc} A^{b}_{\mu} A^{c}_{\nu}$$

Two sources of fascinating multi-particle structures

Scale Invariance (apparent from the massless Lagrangian) Confinement (win \$1,000,000 if you can prove)



Jets (the fractal of perturbative QCD) \leftrightarrow amplitude structures in quantum field theory \leftrightarrow factorisation & unitarity. Precision jet (structure) studies.



Strings (strong gluon fields) ↔ quantum-classical correspondence. String physics. String breaks. Dynamics of hadronization phase transition.



Hadrons ↔ Spectroscopy (incl excited and exotic states), lattice QCD, (rare) decays, mixing, light nuclei. Hadron beams → multiparton interactions, diffraction, ...

Ulterior Motives for Studying QCD

There are more things in heaven and earth, Horatio, than are dreamt of in your philosophy

Shakespeare, Hamlet.

$$J = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$+ i \overline{\psi} \overline{\psi} \psi + h.c.$$

$$+ \overline{\psi} i \overline{\psi} i \overline{\psi} + h.c.$$

$$+ \overline{\psi} i \overline{\psi} i \overline{\psi} - V(\phi)$$

Run 2 now underway ... Almost twice the energy (13 TeV vs 8 TeV) Higher intensities ... (at least until last Friday)

LHC Run 1: still no explicit "new physics" → we're still looking for *deviations* from SM Accurate modelling of QCD **improve** searches & precision

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1st jet: p_T = 520 GeV, η = -1.4, φ = -2.0
2nd jet: p_T = 460 GeV, η = 2.2, φ = 1.0
3rd jet: p_T = 130 GeV, η = -0.3, φ = 1.2
4th jet: p_T = 50 GeV, η = -1.0, φ = -2.9

QCD in the Ultraviolet



Full symbols are results based on N3LO QCD, open circles are based on NNLO, open triangles and squares on NLO QCD. The cross-filled square is based on lattice QCD.



At high scales Q >> 1 GeV

Coupling $\alpha_s(Q) \ll 1$

Perturbation theory in α_s should be **reliable**: LO, NLO, NNLO, ...

E.g., in event shown on previous slide:

- 1st jet: $p_T = 520 \text{ GeV}$
- 2nd jet: $p_T = 460 \text{ GeV}$
- 3rd jet: p_T = 130 GeV
- 4th jet: $p_T = 50 \text{ GeV}$

The Infrared Strikes Back

Naively, QCD radiation suppressed by $\alpha_s \approx 0.1$

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Truncate at fixed order = LO, NLO, ...
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E.g., $\sigma(X+jet)/\sigma(X) \propto \alpha_s$

LHC - sps1a - m~600 GeV		Plehn, Rainwater, PS PLB645(2007)217					
FIXED ORDER pQCD	$\sigma_{\rm tot}[{\rm pb}]$	$ ilde{g} ilde{g}$	$\tilde{u}_L \tilde{g}$	$\tilde{u}_L \tilde{u}_L^*$	$\tilde{u}_L \tilde{u}_L$	TT	
$p_{T,j} > 100 \text{ GeV}$	σ_{0j}	4.83	5.65	0.286	0.502	1.30	σ for X + jets much larger than naive estimate
inclusive X + 1 "jet"	$\rightarrow \sigma_{1j}$	2.89	2.74	0.136	0.145	0.73	
inclusive X + 2 "jets" -	$\rightarrow \sigma_{2j}$	1.09	0.85	0.049	0.039	0.26	
$p_{T,j} > 50 \text{ GeV}$	σ_{0j}	4.83	5.65	0.286	0.502	1.30	$\sigma_{50} \sim \sigma_{tot}$ tells us that there will
	σ_{1j}	5.90	5.37	0.283	0.285	1.50	"always" be a ~ 50-GeV jet "inside" a 600-GeV process
	σ_{2j}	4.17	3.18	0.179	0.117	1.21	

Example: Pair production of SUSY particles at LHC₁₄, with $M_{SUSY} \approx 600$ GeV

(Computed with SUSY-MadGraph)

All the scales are high, Q >> 1 GeV, so perturbation theory **should** be OK ...

Jets have fractal substructure

see PS, Introduction to QCD, TASI 2012, arXiv:1207.2389



Jets have fractal substructure

Can apply this many times \rightarrow nested factorizations \rightarrow iteratively build up fractal structure



Can be cast as a differential **evolution** in the resolution scale, dProb/dQ²

It's a *quantum* fractal: P is **probability** to resolve another jet as we decrease the scale Eventually, it becomes more unlikely **not** to resolve a jet, than to resolve one

That's what the X+jet cross sections were trying to tell us earlier: $\sigma(X+jet) > \sigma(X)$

Monte Carlo Event Generators: Divide and Conquer

Factorization → Split the problem into many (nested) pieces

+ Quantum mechanics → Probabilities → Random Numbers

 $\mathcal{P}_{\mathrm{event}} \;=\; \mathcal{P}_{\mathrm{hard}} \,\otimes\, \mathcal{P}_{\mathrm{dec}} \,\otimes\, \mathcal{P}_{\mathrm{ISR}} \,\otimes\, \mathcal{P}_{\mathrm{FSR}} \,\otimes\, \mathcal{P}_{\mathrm{MPI}} \,\otimes\, \mathcal{P}_{\mathrm{Had}} \,\otimes\, \dots$



Hard Process & Decays:

Use process-specific (N)LO matrix elements

→ Sets "hard" resolution scale for process: Q_{MAX}



ISR & FSR (Initial & Final-State Radiation):

Universal DGLAP equations \rightarrow differential evolution, dP/dQ², as function of resolution scale; run from Q_{MAX} to Q_{Confinement} ~ 1 GeV (More later)



MPI (Multi-Parton Interactions)

Additional (soft) parton-parton interactions: LO matrix elements

→ Additional (soft) "Underlying-Event" activity (Not the topic for today)



Hadronization

Non-perturbative model of color-singlet parton systems \rightarrow hadrons

This is just the physics of Bremsstrahlung



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From Legs to Loops

see PS, Introduction to QCD, TASI 2012, arXiv:1207.2389

Unitarity: sum(probability) = 1



→ Can also include loops-within-loops-within-loops ...
 → Bootstrap for approximate All-Orders Quantum Corrections!

Parton Showers: reformulation of pQCD corrections as gain-loss diff eq. Iterative (Markov-Chain) evolution algorithm, based on universality and unitarity With evolution kernel ~ $\frac{|\mathcal{M}_{n+1}|^2}{|\mathcal{M}_n|^2}$ (or soft/collinear approx thereof) Generate explicit fractal structure across all scales (via Monte Carlo Simulation) Evolve in some measure of *resolution* ~ hardness, virtuality, 1/time ~ fractal scale + account for scaling violation via quark masses and $g_s^2 \rightarrow 4\pi\alpha_s(Q^2)$

Our Research



Parton Showers are based on 1→2 splittings



E.g., PYTHIA (also HERWIG, SHERPA)

I.e., each **parton** undergoes a sequence of splittings

Dipole coherence effects can be included via "angular ordering" or via "dipole radiation functions" (~dipole partitioned into 2 monopole terms) Recoil effects needed to impose (E,p) conservation ("local" or "global")

At Monash, we develop an **Antenna Shower**, in which splittings are fundamentally $2 \rightarrow 3$ (+ working on $2 \rightarrow 4...$)



E.g., **VINCIA** (also ARIADNE)



Each colour dipole/antenna undergoes a sequence of splittings

- + Intrinsically includes dipole coherence (leading N_C)
- + Lorentz invariance and explicit local (E,p) conservation
- + The non-perturbative limit of a colour dipole is a string piece Roots in Lund ~ mid-80ies: Gustafson & Petterson, Nucl.Phys. B306 (1988) 746

What's new in our approach?

Higher-order perturbative effects can be introduced via calculable corrections in an elegant and very efficient way

+ Writing a genuine antenna shower also for the initial state evolution



COLOUI HOW

sions Ritzmann, Kosower, PS, PLB718 (2013) 1345 dron collisions

attering at 45°)



April 2016 First public release of Vincia 2.0 (LHC) (restricted to massless QCD)



Figure 4: Angular distribution of the first gluon emission in $qq \rightarrow qq$ scattering at 45°, for the two different color flows. The light (red) histogram shows the emission density for the forward flow, and the dark (blue) histogram shows the emission density for the backward flow.

Note: coherence also influences the Tevatron top-quark forwardbackward asymmetry: see PS, Webber, Winter, JHEP 1207 (2012) 151

VINCIA: Markovian pQCD*

Virtual Numerical Collider with Interleaved Antennae

*)pQCD : perturbative QCD





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+ Future Applications (why other people care)

Example: The Top Quark

Heaviest known elementary particle: $m_t \sim 187 \ u \ (\sim m_{Au})$ Lifetime: 10^{-24} s

Complicated decay chains:

 $t \to bW^+ \quad \overline{t} \to \overline{b}W^ W \to \{q\overline{q}', \ell\nu\}$

quarks \rightarrow jets b-quarks \rightarrow b-jets

$$m_t^2 \approx (p_b + p_{W^+})^2$$
$$\approx (p_{b-\text{jet}} + p_{q-\text{jet}} + p_{\bar{q}-\text{jet}})^2$$

Accurate jet energy calibrations $\rightarrow m_t$ Analogously for any process / measurement involving coloured partons



Decays of **coloured massive particles** is the most important remaining step

The Ultimate Limit: Wavelengths > 10⁻¹⁵ m

Quark-Antiquark Potential

As function of separation distance



~ Force required to lift a 16-ton truck

What physical

system has a

String Breaks

In QCD, strings can (and do) break!

(In superconductors, would require magnetic monopoles) In QCD, the roles of electric and magnetic are reversed Quarks (and antiquarks) are "chromoelectric monopoles" There are at least two possible analogies ~ tunneling:

String Breaks

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1) Schwinger Effect

 e^+

Non-perturbative creation of e⁺e⁻ pairs in a strong external Electric field

> Probability from Tunneling Factor

 $\mathcal{P} \propto \exp\left(rac{-m^2 - p_{\perp}^2}{\kappa/\pi}
ight)$

(κ is the string tension equivalent)

ZZ

 \vec{E}

The "Lund" String

- **Quarks** → String Endpoints
- **Gluons** → Transverse Excitations (kinks)





String Breaks by Tunneling (Schwinger Type)



Gluon = kink on string, carrying energy and momentum

- Probability of string break constant per unit area → AREA LAW
- Breakup vertices causally disconnected → order is irrelevant → iterative algorithm

Colour Confusion

Between which partons do confining potentials arise?



even after including bremsstrahlung etc.) At e⁺e⁻ colliders (eg LEP) : generally good agreement between **measured** particle spectra and **models** based on parton/antenna showers + strings

Basically a single **3-3bar** system, very close to the original lattice studies motivating the string model.

(+ extensions to WW reasonable to ${\sim}O(1/N_c{}^2))$

→ re-use same models as input for LHC (universality) ?

Proton-Proton (LHC)

A lot more colour kicked around (& also colour in initial state)

Include "Beam Remnants"

Still might look relatively simple, to begin with



(+baryon beam remnants → "string junctions") String-fragmentation of junctions: Sjöstrand & Skands Nucl.Phys. B659 (2003) 243 But no law against *several* parton-parton interactions



In fact, can easily be shown to happen frequently Included in all (modern) Monte Carlo models But how to make sense of the colour structure?

Colour: What's the Problem?

(including MPI: Multiple Parton-Parton Interactions ~ the "underlying event")

Without Colour Reconnections Each MPI hadronizes independently of all others



Colour: What's the Problem?

(including MPI: Multiple Parton-Parton Interactions ~ the "underlying event")

Without Colour Reconnections Each MPI hadronizes independently of all others



Colour Reconnections

(including **MPI**: Multiple Parton-Parton Interactions ~ the "underlying event")



What are "Colour Reconnections"?

Simple example: $e^+e^- \to W^+W^- \to hadrons$

- Intensely studied at LEP2.
 - CR implied a non-perturbative uncertainty on the W mass measurement, $\Delta MW \sim 40 \text{ MeV}$
- CR constrained to ~ 10% ~ 1/NC2
- Simple two-string system. What about pp?

Several modelling attempts

Based on "just" minimising the string action String interactions (Khoze, Sjostrand) Generalized Area Law (Rathsman et al.)

- Colour Annealing (Skands et al.)
- Gluon Move Model (Sjostrand et al.)

More recently: SU(3)_C group multiplet weights Dipole Swing (Lonnblad et al.) String Formation Beyond Leading Colour (Skands et al.)





 $\begin{array}{rcl} 3 \otimes \bar{3} &=& 8 \oplus 1 \\ 3 \otimes 3 &=& 6 \oplus \bar{3} \\ 3 \otimes 8 &=& 15 \oplus 6 \oplus 3 \\ 8 \otimes 8 &=& 27 \oplus 10 \oplus \overline{10} \oplus 8 \oplus 8 \oplus 1 \end{array}$

What do we see?

Plots from <u>mcplots.cern.ch</u> (powered by LHC@home)

Skands et al., Eur.Phys.J. C74 (2014) 2714



What do we see?

<pT> vs Particle Mass

Note:

from RHIC

(200 GeV)

Soft QCD

1.5

1.5

mass [GeV]

<pT> vs Number of Particles



Average pT increases with particle multiplicity and (faster than predicted) with particle mass

Fundamental Questions

(Reflections upon yesterday's curry dinner ...)

Multiple Strings: String *interactions*?





Like Type I Superconductor? Like Type II Superconductor? Something else?

Potential between two triplets: antitriplet is attractive (diquarks); sextet is repulsive We can treat anti-triplet via $CR \rightarrow$ junction-junction structure But we do nothing for the sextet



Figure 1. The ratios of the string tensions of flux tubes for various SU(3) representations, $d_D = \sigma_D/\sigma_3$ for the GL parameters $\kappa = 1$, 3 and 9 (represented by crosses, each case connected by lines to guide the eye). The ratios of eigenvalues of the quadratic Casimir operators are shown as black bars. For comparison the lattice data of Ref. [2] are also plotted (diamonds with error bars). Boldface numbers and brackets [p, q] denote the dimension and the Dynkin indices

of each representation D, respectively

+ Newer results from Cardoso, Cardoso, Bicudo seem to support Casimir scaling (Type II): arXiv:1102.1542

Quo Vadis?

All sights are on Run 2 of the LHC

Next order of precision for jet rates and structure

Aid precision measurements and enhance discovery reach Vast multi-jet phase spaces to explore with LHC Merging and MHV corrections (S. Prestel, A. Lifson, N. Fischer)

Beyond the Leading-Logarithmic approximation (with post doc Hai Tao Li)

+ systematic and automated theory uncertainties
 Part of being precise is knowing how precise. Our job to give an answer.
 Automated uncertainty bands in both VINCIA and PYTHIA 8 (Mrenna+Skands)

Strings

Understand the physics of colour reconnections What are the *dynamics* of multi-string environments? Get this research going in Australia **Phenomenology**: Modern revisions of the Lund string model What measurements are crucial to shed more light? Possible to get more information from lattice? Multi-string systems?



New research at Monash



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PRECISION LHC PHENOMENOLOGY PYTHIA & VINCIA NLO EVENT GENERATORS QCD STRINGS, HADRONISATION SUPPORT LHC EXPERIMENTS, ASTRO-PARTICLE COMMUNITY, AND FUTURE ACCELERATORS +OUTREACH AND CITIZEN SCIENCE

MCnet

+ Partnerships: Warwick Alliance, MCnet, CoEPP

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New joint research program with Warwick ATLAS, on developing and testing advanced colllider-QCD models. **Opportunities for PhD students** based at Monash + exchange to UK/CERN.

See: arXiv:1603.05298



MC*net* is an EU Marie Curie "Innovative Training Network" (ITN) on MC generators for LHC (Herwig, Pythia, Sherpa). *Funded last week!* Starting in 2017 with Monash an associate partner

