### MC Overview



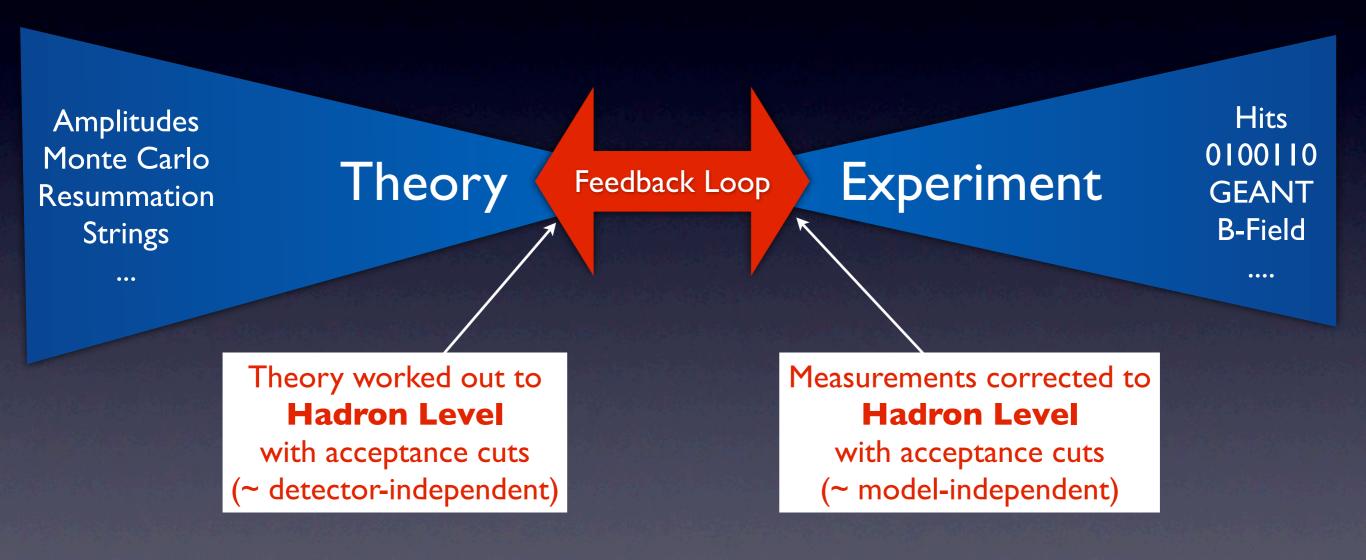
Peter Skands

(CERN-TH)

#### Count what is Countable

### Measure what is Measurable

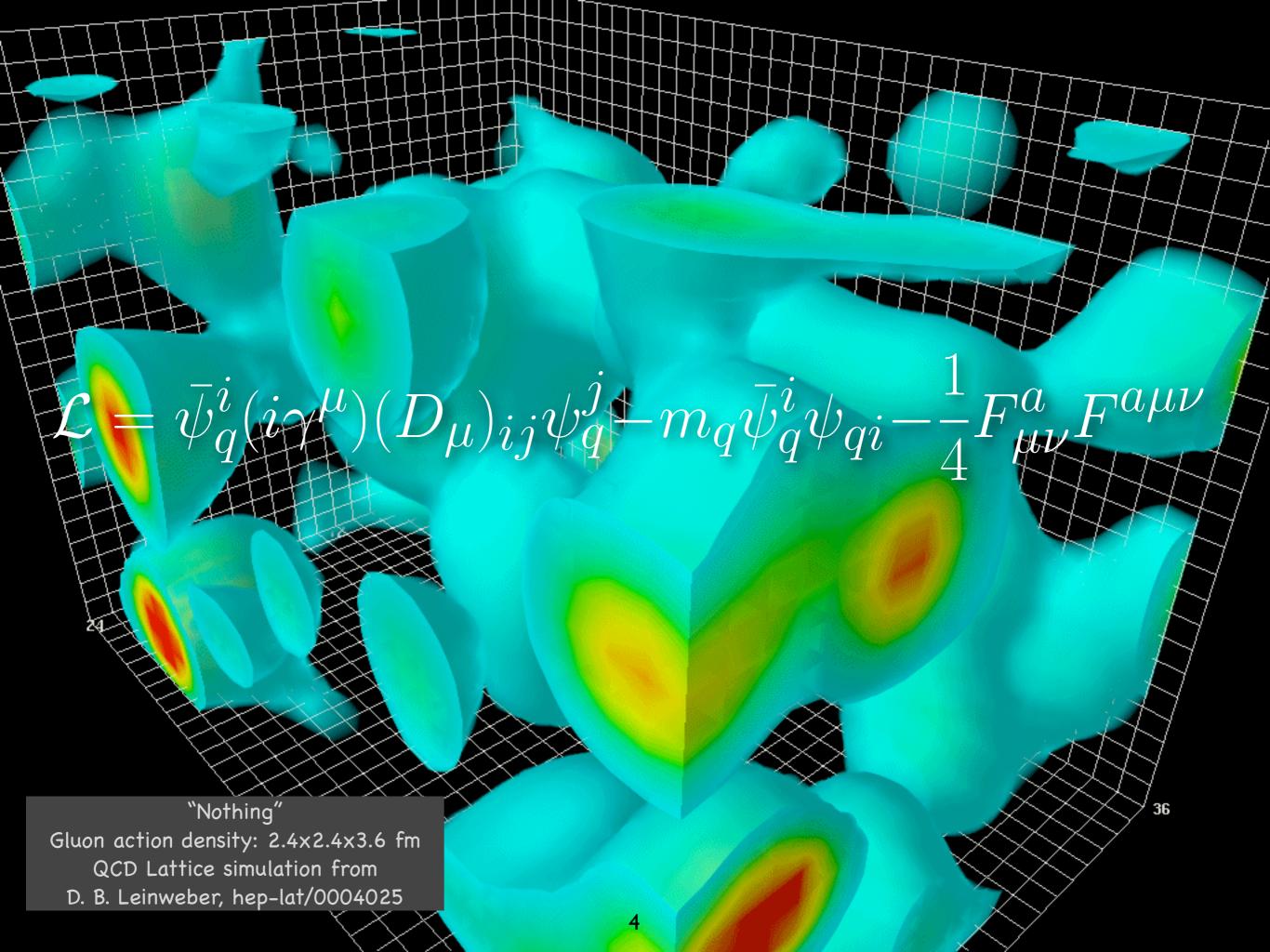
(and keep working up the beam)

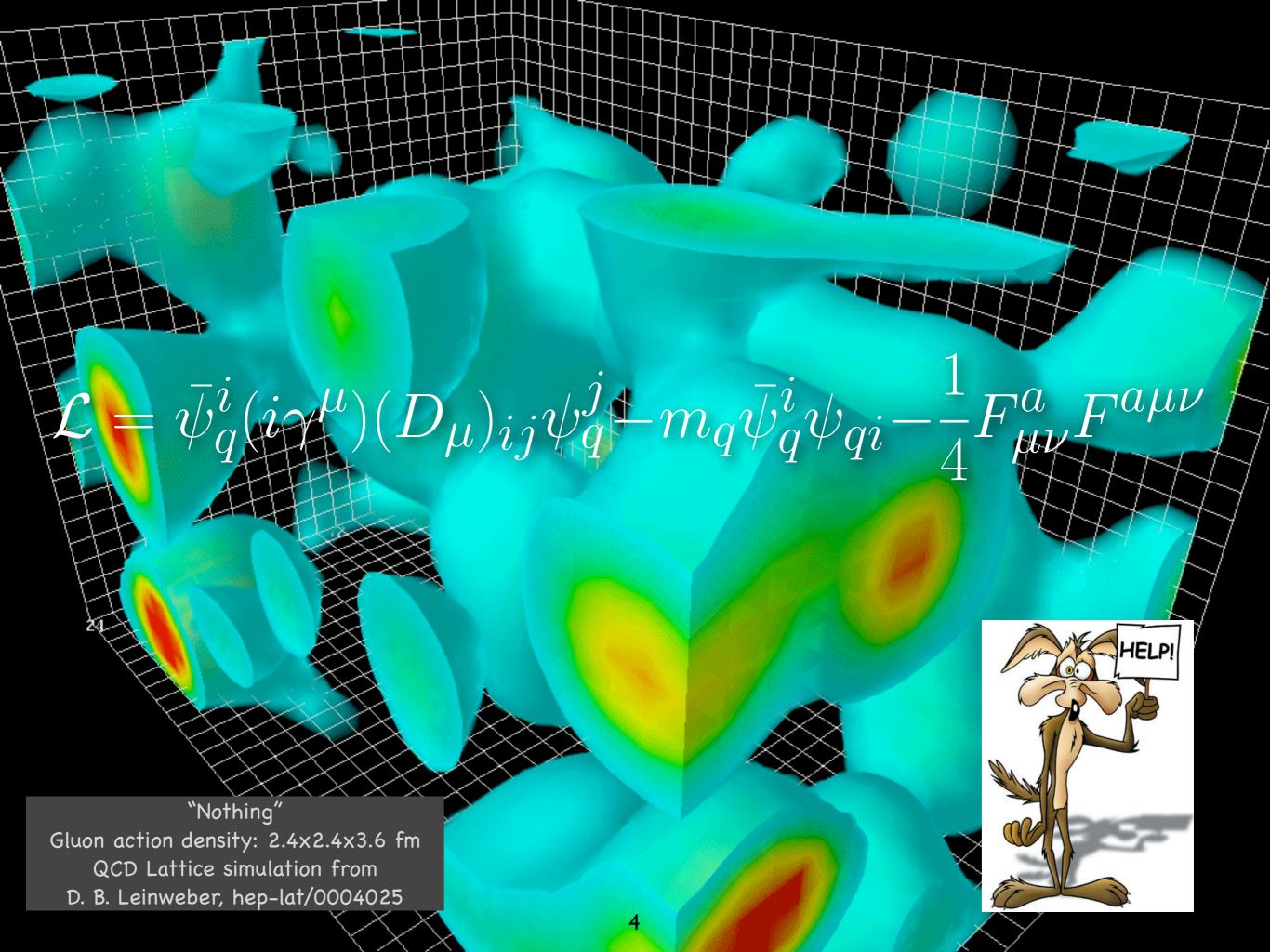


#### THEORY

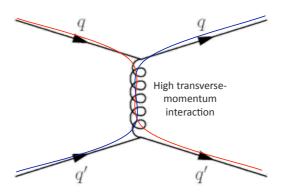
$$\mathcal{L} = \bar{\psi}_{q}^{i}(i\gamma^{\mu})(D_{\mu})_{ij}\psi_{q}^{j} - m_{q}\bar{\psi}_{q}^{i}\psi_{qi} - \frac{1}{4}F_{\mu\nu}^{a}F^{a\mu\nu}$$

+ quark masses and value of  $\alpha_s$ 



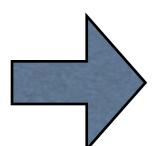


## Perturbation Theory



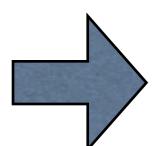
# Perturbation Theory





- Who needs QCD? I'll use leptons
  - Sum inclusively over all QCD
    - Leptons almost IR safe by definition
    - WIMP-type DM, Z', EWSB → may get some leptons



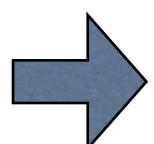


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- At least need well-understood PDFs
- High precision = higher orders → enter QCD (and more QED)
- Isolation → indirect sensitivity to QCD
- Fakes → indirect sensitivity to QCD



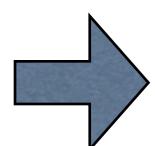


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  - Need to be a lucky chicken ...

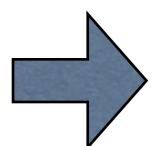




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- Beams = hadrons for next decade (RHIC / Tevatron / LHĆ)
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- The unlucky chicken
  - Put all its eggs in one basket and didn't solve QCD

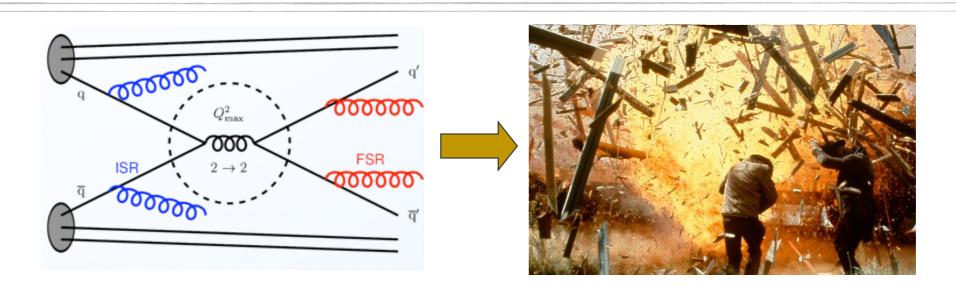


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### Monte Carlo Generators

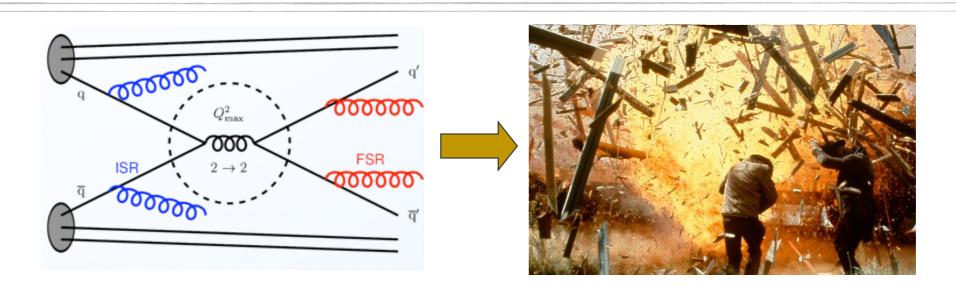


Calculate Everything ≈ solve QCD → requires compromise!

Improve Born-level perturbation theory, by including the 'most significant' corrections

→ complete events → any observable you want

### Monte Carlo Generators



Calculate Everything ≈ solve QCD → requires compromise!

Improve Born-level perturbation theory, by including the 'most significant' corrections

→ complete events → any observable you want

- 1. Parton Showers
- 2. Matching
- 3. Hadronisation
- 4. The Underlying Event



- 2. Finite Terms, "K"-factors
- 3. Power Corrections (more if not IR safe)
- 4. ?

(+ many other ingredients: resonance decays, beam remnants, Bose-Einstein, ...)

roughly

### Main Workhorses

HERWIG, PYTHIA and SHERPA intend to offer a convenient framework for LHC physics studies, but with slightly different emphasis:



#### PYTHIA (successor to JETSET, begun in 1978):

- originated in hadronization studies: the Lund string
- leading in development of multiple parton interactions
- pragmatic attitude to showers & matching
- the first multipurpose generator: machines & processes

#### HERWIG (successor to EARWIG, begun in 1984):

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- large process library with spin correlations in decays



#### SHERPA (APACIC++/AMEGIC++, begun in 2000):

- own matrix-element calculator/generator
- extensive machinery for CKKW matching to showers
- PYTHIA-like MPI model + HERWIG-like hadronization model

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+ WHIZARD (OMEGA): emerging serious tool with focus on BSM

Charges Stopped



Charges Stopped

Associated field (fluctuations) continues

Charges Stopped

ISR ISR

Associated field (fluctuations) continues

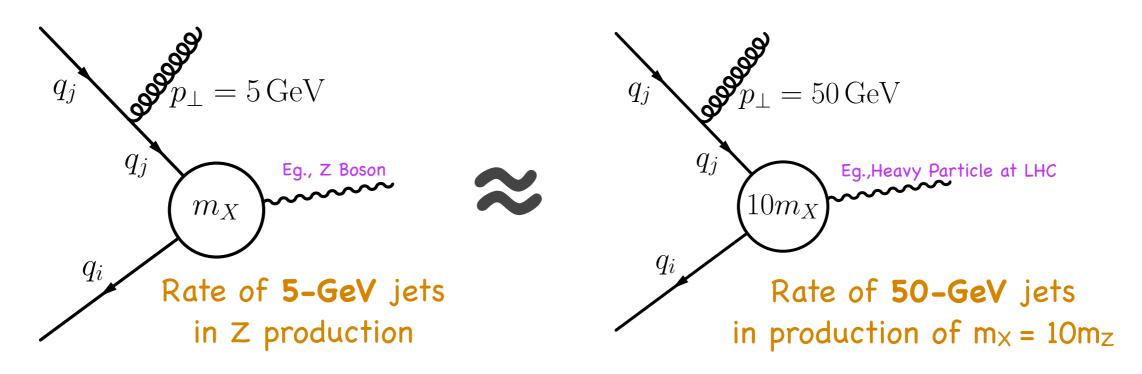
Charges Stopped

ISR ISR

The harder they stop, the harder the fluctations that continue to become strahlung

### Conformal QCD (a.k.a. Bjorken scaling)

Rate of bremsstrahlung jets mainly depends on the RATIO of the jet  $p_T$  to the "hard scale"



Soft/Collinear enhancements DIVERGENT for  $p_T \ll m_X$ 

Plehn, Rainwater, PS: PLB645(2007)217
Plehn, Tait: 0810.2919 [hep-ph]
Alwall, de Visscher, Maltoni:

JHEP 0902(2009)017

## Computing Bremsstrahlung

#### 1. Fixed-order QCD

Perturbation theory must be valid

- $\rightarrow \alpha_s$  must be small
- $\rightarrow$  All Q<sub>i</sub> >>  $\Lambda_{QCD}$

Single-scale: abensence of enhancements from soft/collinear singular (conformal) dynamics

 $\rightarrow$  All  $Q_i/Q_j \approx 1$ 

 $\rightarrow$  All resolved scales >>  $\Lambda_{QCD}$  AND no large hierarchies

### Fixed-Order QCD

#### All resolved scales >> $\Lambda_{QCD}$ AND no large hierarchies

### Trivially untrue for QCD

We're colliding, and observing, hadrons  $\rightarrow$  small scales We want to consider high-scale processes  $\rightarrow$  large scale differences

→ A Priori, no perturbatively calculable observables in hadron-hadron collisions

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→ Initial-State Showers in MC

→ Final-State Showers (+ hadronization) in MC

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$$\frac{\mathrm{d}\sigma}{\mathrm{d}X} = \sum_{a,b} \sum_{f} \int_{\hat{X}_f} f_a(x_a, Q_i^2) f_b(x_b, Q_i^2) \frac{\mathrm{d}\hat{\sigma}_{ab \to f}(x_a, x_b, f, Q_i^2, Q_f^2)}{\mathrm{d}\hat{X}_f} D(\hat{X}_f \to X, Q_i^2, Q_f^2)$$

PDFs: needed to compute inclusive cross sections

→ Initial-State Showers in MC

FFs: needed to compute
(semi-)exclusive cross sections
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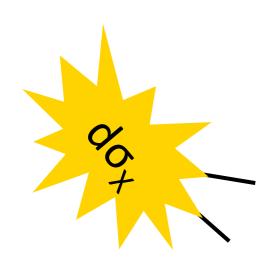
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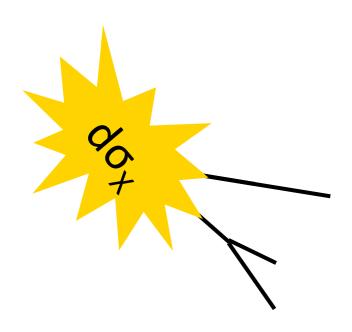
FFs: needed to compute (semi-)exclusive cross sections

→ Final-State Showers (+ hadronization) in MC

All resolved scales >>  $\Lambda_{QCD}$  AND X Infrared Safe

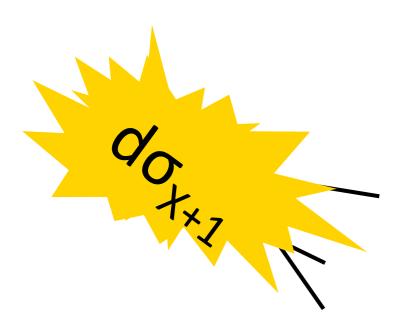






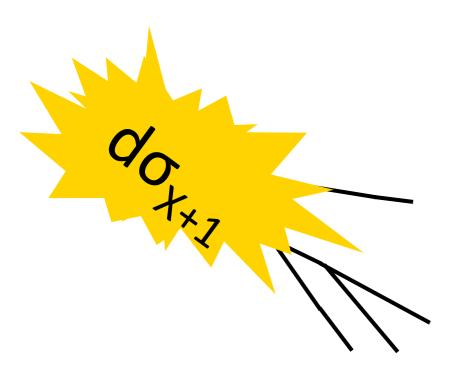
$$\mathrm{d}\sigma_X = \dots$$

$$d\sigma_{X+1} \sim 2g^2 d\sigma_X \frac{ds_{a1}}{s_{a1}} \frac{ds_{1b}}{s_{1b}}$$



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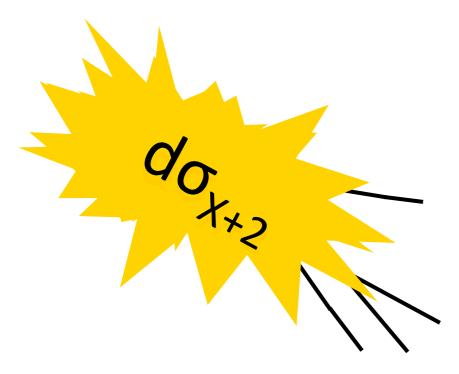
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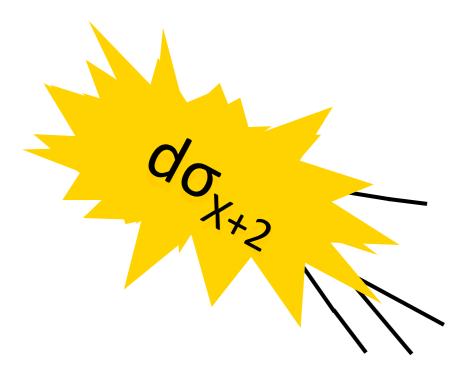
$$d\sigma_{X+2} \sim 2g^2 d\sigma_{X+1} \frac{ds_{a2}}{s_{a2}} \frac{ds_{2b}}{s_{2b}}$$



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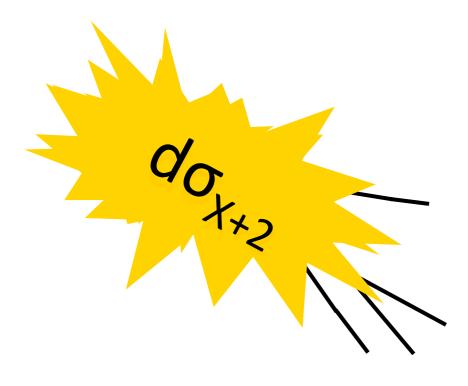


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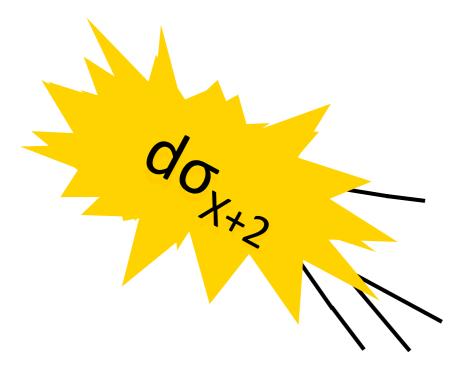
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This gives an approximation to infinite-order tree-level cross sections (here "DLA")



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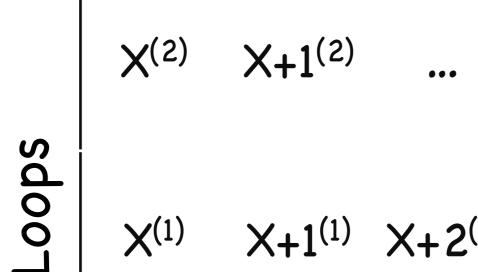
This gives an approximation to infinite-order tree-level cross sections (here "DLA")

But something is not right ...

Total cross section would be infinite ...

## Loops and Legs

#### Summation



The Virtual corrections are missing

$$X^{(1)}$$
  $X+1^{(1)}$   $X+2^{(1)}$   $X+3^{(1)}$ 

Born  $X+1^{(0)}$   $X+2^{(0)}$   $X+3^{(0)}$ 

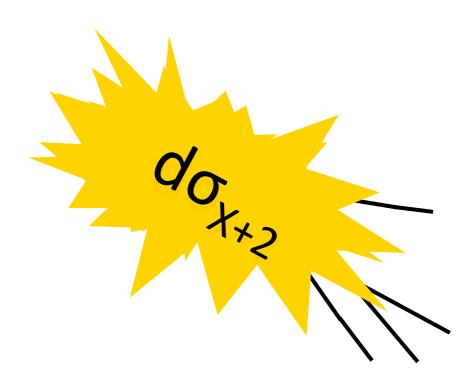
Universality (scaling)

Jet-within-a-jet-within-a-jet-...

•••

Legs

### Resummation



### Unitarity

KLN:

$$Virt = -Int(Tree) + F$$

In LL showers : neglect F

$$\mathrm{d}\sigma_X = \dots$$

$$d\sigma_{X+1} \sim 2g^2 d\sigma_X \frac{ds_{a1}}{s_{a1}} \frac{ds_{1b}}{s_{1b}}$$

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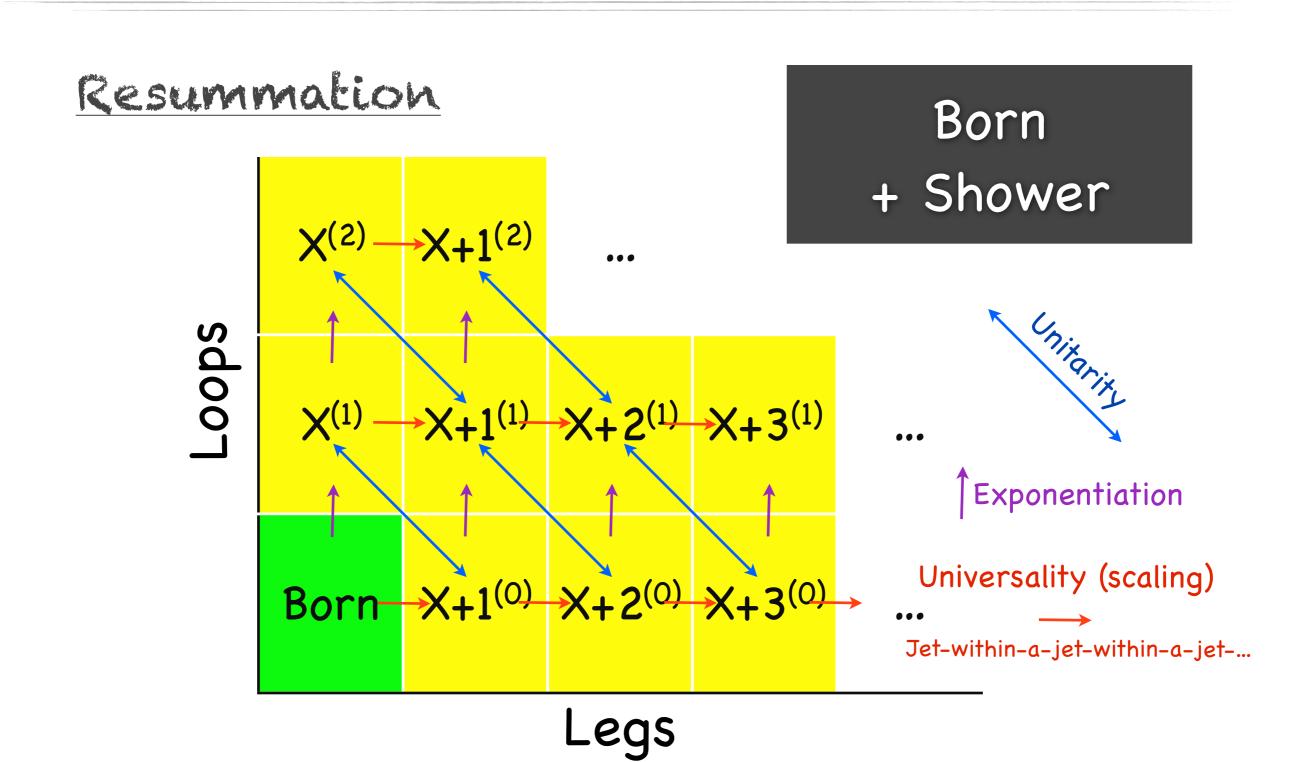
#### Imposed by Event evolution:

When (X) branches to (X+I): Gain one (X+I). Loose one (X).

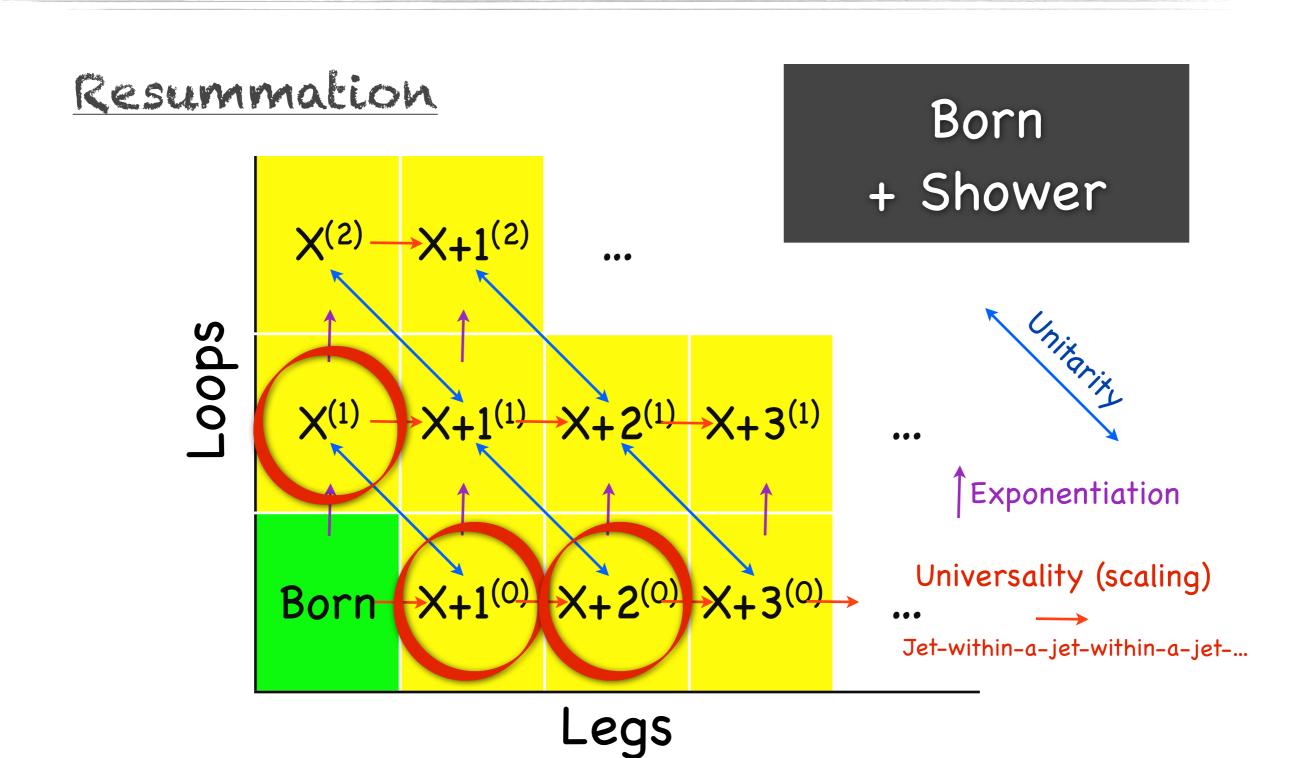
$$\sigma_{X+1}(Q) = \sigma_{X;incl} - \sigma_{X;excl}(Q)$$

→ includes both real and virtual corrections (in LL approx)

## Bootstrapped pQCD



## Bootstrapped pQCD



# Matching

► A (Complete Idiot's) Solution – Combine

```
1. [X]<sub>ME</sub> + showering
```

2. 
$$[X + 1 \text{ jet}]_{ME}$$
 + showering

3. ...

Run generator for X (+ shower)

Run generator for X+1 (+ shower)

Run generator for ... (+ shower)

Combine everything into one sample

# Matching

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  - 1. [X]<sub>ME</sub> + showering
  - 2.  $[X + 1 \text{ jet}]_{ME}$  + showering
  - 3. ...

Doesn't work

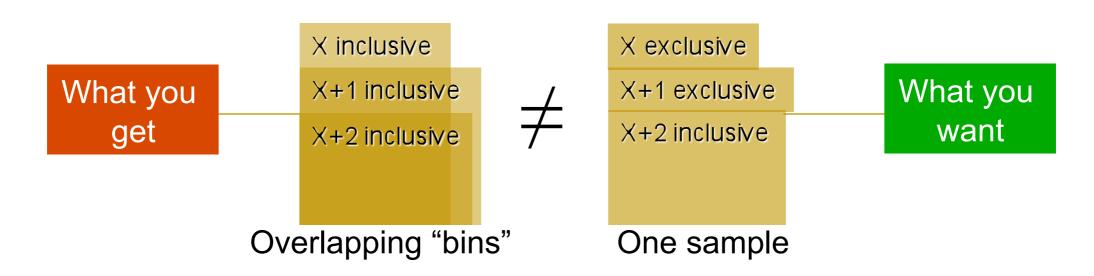
- [X] + shower is inclusive
- [X+1] + shower is also inclusive

Run generator for X (+ shower)

Run generator for X+1 (+ shower)

Run generator for ... (+ shower)

Combine everything into one sample



Shower off X already contains LL part of all X+n

$$d\sigma_{X+1} \sim 2g^2 d\sigma_X \frac{ds_{a1}}{s_{a1}} \frac{ds_{1b}}{s_{1b}}$$

Adding back full ME for X+n would be overkill

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Adding back full ME for X+n would be overkill



**Solution I: "Additive"** (most widespread)

Seymour, CPC90(1995)95 + many more recent ..

Add event samples, with modified weights

$$w_X = |M_X|^2$$

$$w_{X+1} = |M_{X+1}|^2 - Shower\{w_X\}$$

$$w_{X+n} = |M_{X+n}|^2 - Shower\{w_X, w_{X+1}, ..., w_{X+n-1}\}$$

Only CKKW and MLM

HERWIG: for X+I @ LO (Shower = 0 in dead zone of angular-ordered shower)

MC@NLO: for X+I @ LO and X @ NLO (note: correction can be negative)

CKKW & MLM: for all X+n @ LO (force Shower = 0 above "matching scale" and add ME there) SHERPA (CKKW), ALPGEN (MLM + HW/PY), MADGRAPH (MLM + HW/PY), PYTHIA8 (CKKW-L from LHE files), ...

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- Shower off Xalready contains LL part of all X+n
- $d\sigma_{X+1} \sim 2g^2 d\sigma_X \frac{ds_{a1}}{ds_{1b}}$
- Adding back full ME for X+n would be overkill



### Solution 2: "Multiplicative"

One event sample

$$w_X = |M_X|^2$$

+ Shower

Make a "course correction" to the shower at each order

$$R_{X+1} = |M_{X+1}|^2 / Shower\{w_X\}$$

+ Shower

$$R_{X+n} = |M_{X+n}|^2 / Shower \{w_{X+n-1}\}$$

+ Shower

Only VINCIA

PYTHIA: for X+I @ LO (for color-singlet production and ~ all SM and BSM decay processes)

POWHEG: for X+I @ LO and X @ NLO (note: positive weights) POWHEG Box HERWIG++



VINCIA: for all X+n @ LO and X @ NLO (only worked out for decay processes so far)

### SPEED: milliseconds / Event



MS/EVENT	MS/EVENT			Matched through:		
Monte Carlo	Strategy	<b>Z</b> →3	<b>Z</b> →4	<b>Z</b> →5	<b>Z</b> →6	
Pythia 8 Initialization time ~ 0	TS	0.22	$Z \rightarrow qq \ (q=udscb) + shower.$ Matched and unweighted. Hadronization off  gfortran/g++ with gcc v.4.4 -O2 on single 3.06 GHz processor with 4GB  memory			
Vincia (sector, $Q_{match} = 5 \text{ GeV}$ ) Initialization time $\sim 0$	GKS	0.26	0.50	1.40	6.70	
Sherpa $(Q_{match} = 5 \text{ GeV})$ Initialization time =	CKKW (expect similar scaling for MLM)	5.15* 1.5 minutes	53.00* 7 minutes	220.00* 22 minutes	400.00* 2.2 hours	

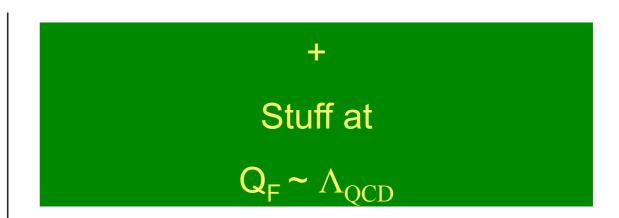
Generator Versions: Pythia 6.425 (Perugia 2011 tune), Pythia 8.150, Sherpa 1.3.0, Vincia 1.026 (without uncertainty bands, NLL/NLC=OFF)

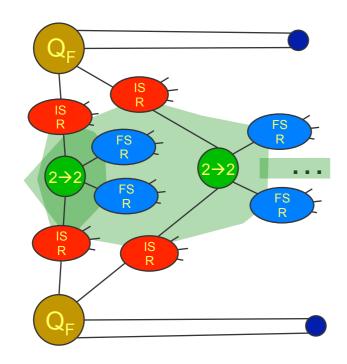
Efficient Matching with Sector Showers

J. Lopez-Villarejo & PS: JHEP 1111 (2011) 150

### Additional Sources of Particle Production

 $Q_F >> \Lambda_{QCD}$  ME+ISR/FSR + perturbative MPI





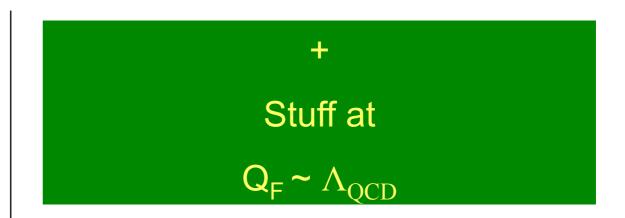
Multiple (perturbative) parton-parton Interactions occurring in each single hadron-hadron collision

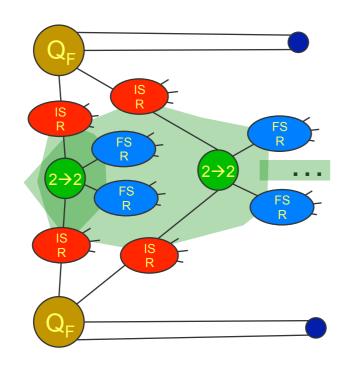
→ underlying event

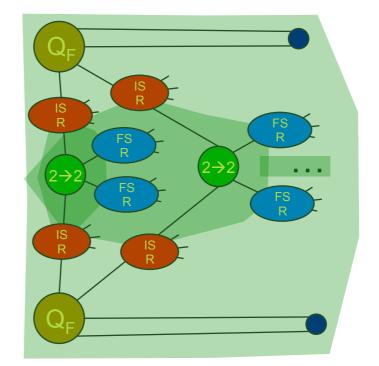
(distinct from pile-up caused by high lumi)

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Multiple (perturbative) parton-parton Interactions occurring in each single hadron-hadron collision → underlying event

(distinct from pile-up caused by high lumi)

Need-to-know issues for IR sensitive quantities (e.g., N<sub>ch</sub>)

#### The problem:

- Given a set of partons resolved at a scale of ~ I GeV (the shower + MPI cutoff), need a "mapping" from this set onto a set of on-shell colour-singlet hadronic states.
- I.e., a fully exclusive fragmentation function defined at  $Q_{Had} \sim I GeV$

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#### MC models do this in three steps

- Map partons onto continuum of highly excited hadronic states (called 'strings' or 'clusters')
- 2. Iteratively map strings/clusters onto discrete set of primary hadrons (string breaks / cluster splittings / cluster decays)
- 3. Sequential decays into **secondary hadrons** (e.g., rho > pi pi, Lambda > n pi0, pi0 > gamma gamma, ...)

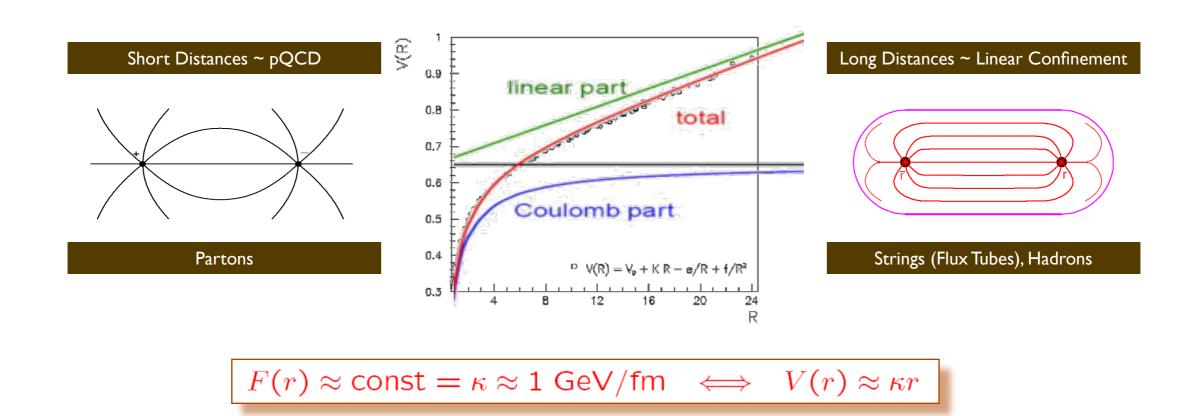
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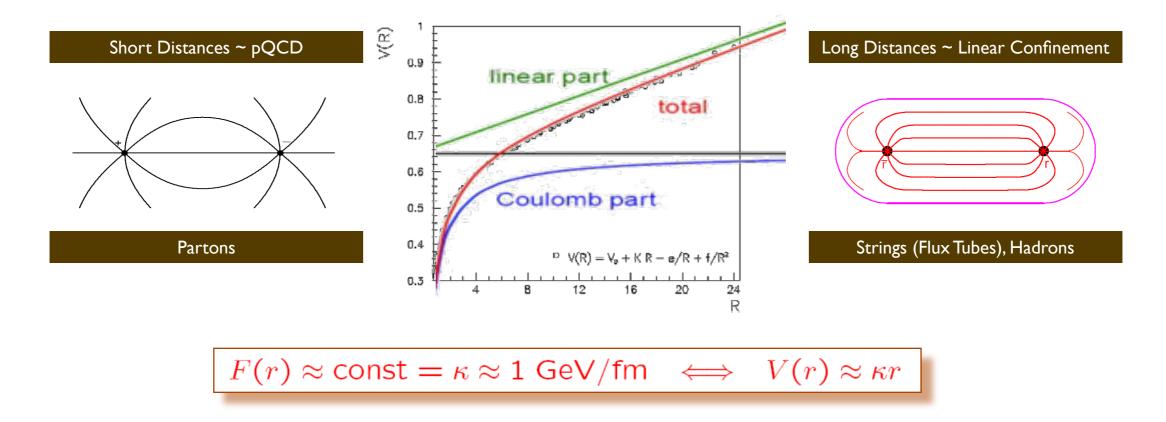
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## From Partons to Strings



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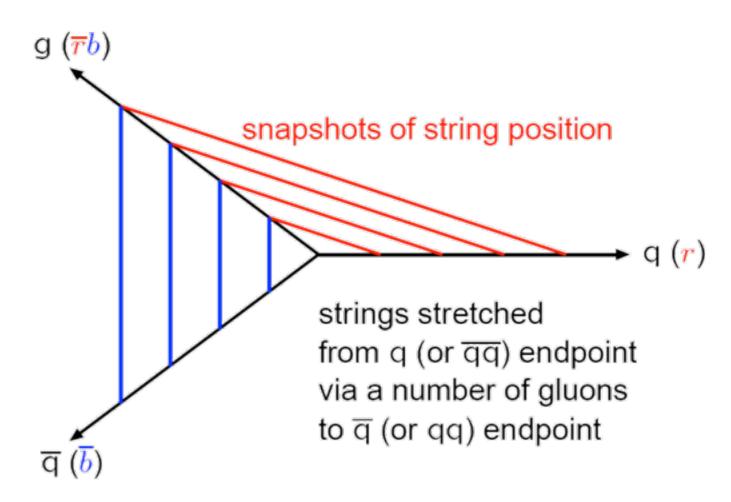
#### Motivates a model:

- Separation of transverse and longitudinal degrees of freedom
- Simple description as I+I dimensional worldsheet string –
   with Lorentz invariant formalism

## The (Lund) String Model

### Map:

- Quarks > String Endpoints
- Gluons > Transverse
   Excitations (kinks)
- Physics then in terms of string worldsheet evolving in spacetime
- Probability of string break constant per unit area > AREA LAW



Gluon = kink on string, carrying energy and momentum

Simple space-time picture

Details of string breaks more complicated

### Conclusions

- QCD Phenomenology is witnessing a rapid evolution: LO & NLO matching, better showers, tuning, interfaces ...
  - Driven by demand for high precision in complex LHC environment with huge phase space
- BSM Physics
  - Generally relies on chains of tools (MC4BSM)
  - Sufficient to reach O(10%) accuracy, with hard work, though must be careful with scale hierarchies, width effects, decay distributions, ...
  - Next machine is a long way off → must strive to build capacity for yet higher precision, to get max from LHC data.
- Ultimate limit set by solutions to pQCD (getting better) and then the really hard stuff
  - Like Hadronization, Underlying Event, Diffraction, ... (& BSM equivalents?)
  - For which fundamentally new ideas may be needed

For more, see the MCnet Review: General-purpose event generators for LHC physics: arXiv:1101.2599